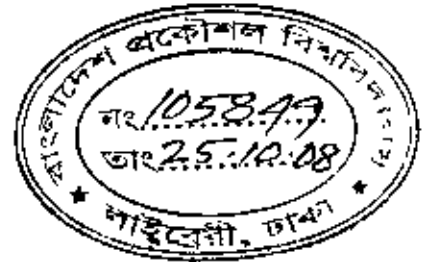


Applicability of Artificial Neural Network in Predicting House Rent

by

Suman Kumar Mitra



MASTER OF URBAN AND REGIONAL PLANNING

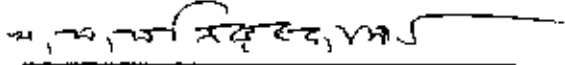
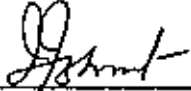
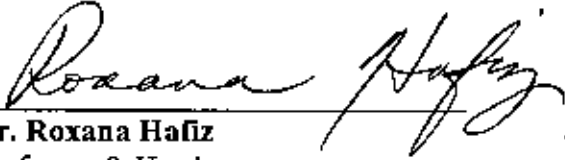
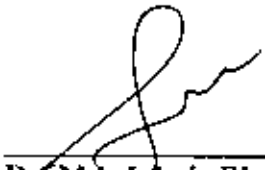


Department of Urban and Regional Planning
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July 2008

The thesis titled, "APPLICABILITY OF ARTIFICIAL NEURAL NETWORK IN PREDICTING HOUSE RENT" submitted by **Suman Kumar Mitra**, Roll No: 100515018P, Session: **October 2005**, has been accepted as satisfactory in partial fulfillment of the requirement for the degree of **MASTER OF URBAN AND REGIONAL PLANNING** on **July 7, 2008**.

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07.7.08

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ABSTRACT

House rent prediction has great importance in real estate development as well as in overall housing situation of a city. The various participants in the real estate market have a substantial interest in the prediction of house rent. Rent models can be an effective tool when empirical data cannot be collected either because of practical constraints of cost, time etc. or when future scenarios are being dealt with. Hedonic price (multiple regression) models have been commonly used to estimate house rent. To address the issue of application of Artificial Neural Network (ANN) in house rent prediction, this study aims to develop an artificial neural network model for house rent prediction. The study will also use the results from a hedonic price model for house rent prediction and compare the predictive power of both models.

The data set used to develop the Neural Network Model consists of a sample of 479 single family and multi-family residential properties available for rent in Rajshahi City. The neural network model built for this data set utilized fourteen independent variables. The neural network models developed in this study are the "best" models that were obtained utilizing a sequential trial and error method. The best model developed with eighty hidden neurons had the R^2 value of 0.621 for sample forecast. The study has demonstrated that neighborhood attributes are the most significant factors in determining the house rent of Rajshahi City. The percentage of area dedicated to community facilities and percentage of area dedicated to commercial use have contributed more to the predictive power of model than the other attributes. So it is seen that land use has a great impact on house rent in Rajshahi City.

The study also empirically compares the predictive power of the artificial neural network model with the hedonic price model on house rent prediction. The comparison was conducted in six stages or cases. The results indicate that the neural network model outperformed the hedonic price model in all of the cases. In this study, the ANN model consistently gave better result than the hedonic price model, although the difference between the two models was not too large. ANN model and hedonic price model both do better when they are trained and tested with the same data set but they performed poorer on out-of-sample forecast. But in both cases ANN model showed better results in comparison to hedonic price model. The study also supports the superiority of ANN model in prediction of outlier holdout sample.

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Chapter 1

INTRODUCTION



Chapter 1: Introduction

1.1 Background of the Study

The housing sector is very much associated with the economic health and wealth of a nation. A high demand for housing would trigger growth in many other economic sectors. For many households, owner-occupied housing is not only a place to live but also the single most important asset in their portfolio. Indeed, in most countries real estate is the greatest component in the private households' wealth. As a consequence, the value of their home has a major impact on households' consumption and savings opportunities. House rents are therefore of great interest to actual and potential home owners but also to real estate developers, banks, policy makers or, in short, the general public.

In Bangladesh most people know the benefit of owning a house, because buying a house is considered the most profitable investment. Most of the house owners of cities like Dhaka, Rajshahi etc. earn money by renting their houses. There is a huge demand for rented houses in urban areas of Bangladesh. House rent in urban areas of Bangladesh is rapidly increasing day by day. The growing rents are of particular problem to the lower income groups, but the issue of rental housing policy is seldom addressed by the public authorities in Bangladesh (Sharmeen, 2007).

House rent prediction has great importance in real estate development as well as in overall housing situation of a city. A reliable prediction of the house rent is important for planners, prospective homeowners, developers, investors, appraisers, tax assessors and other real estate market participants (Limsombunchai *et al.*, 2004). The various participants in the real estate market have a substantial interest in the prediction of house rent. If investors, developers or other participants wish to judge the attractiveness of individual real estate projects, an assessment of the (uncertain) prices and rents in the market segment should constitute an essential element in the decision process. Especially institutional investors, such as pension or investment funds require reliable information regarding house rent and prices. With regard to

questions of asset allocation (i.e. the distribution of a given budget among the main investment sectors, such as stocks, bonds and real estate), information about returns and risk profiles of real estate and their correlation with other types of investment is of central importance. Finally, Public authorities formulate different policy measures, assess holding tax, regulate rents, grant rental allowances, allow tax deduction for mortgage payment, or subsidize the construction of public housing to make housing affordable to all groups of the society on the basis of rent. Rent models can be an effective tool when empirical data cannot be collected either because of practical constraints of cost, time etc. or when future scenarios are being dealt with.

Hedonic price (multiple regression) models have been commonly used to estimate house rent and property values. But this method has received criticism from the academic and practitioner communities. Multiple regression has often produced serious problems for real estate appraisal that primarily result from multicollinearity issues in the independent variables and from the inclusion of outlier properties in the sample (Worzala *et al.*, 1995). Moreover, nonlinearity within the data may make multiple regression an inadequate model for market that requires precise and fast responses (Brunson *et al.* 1994; Do and Grudnitski, 1992). Rossini (1997) points out the disadvantage of hedonic price model in terms of small data sets. Multiple regression has been widely expounded by those who belong to the quantitative school though early use of regression analysis was criticized due to its "black box" approach, in which there was limited discussion of the underlying rationale for the selection of variables and interpretation of outcomes (McGreal *et al.* 1997).

Kang and Reichert (1991) recommended that when a homogeneous property sample exists, hedonic pricing models may be used effectively a priori to determine the adjustment factors that should be used for each independent variable in a manual sales comparison process. Gilson (1992) advocates a more conservative use of hedonic pricing models. Gilson concludes that the regression-derived adjustments should support rather than replace any manually-determined sales comparison price adjustments or even final estimated market values. In fact, most of the related research recommends a critical application of hedonic price techniques. Do and

Grudnitski (1992) claims that although multiple regression alleviates some of the shortcomings of traditional appraisals, often its assessments result in significant appraisal errors. Further, issues such as model specification procedures, multicollinearity, independent variable interactions, heteroscedasticity, non-linearity and outlier data points can seriously hinder the performance of hedonic pricing models in real estate valuations (Lenk et al. 1996). A few studies have investigated the usefulness of hedonic models to determine the value of outlier properties. Borst (1992), Birch et al. (1991) and Isakson (1986) conclude that these models are ineffective estimators of outlier values. They recommend separate, manual analysis for properties that are dissimilar from the prediction model's training data set.

Recently, neural network models, inspired by the neural architecture of the brain, have been developed and successfully applied across a variety of disciplines including psychology, genetics, linguistics, engineering, computer science and economics. Neural networks seem particularly well suited to find accurate solutions in an environment such as residential appraisal, characterized by complex, noisy, irrelevant or partial information or imprecisely defined functional models (Do and Grudnitski, 1992). Artificial neural networks have been offered as a solution to address the criticisms associated with hedonic model approaches. The use of these models is similar to the process utilized in building hedonic pricing models: an artificial neural network model must first be trained from a set of data and the model is then utilized to estimate the prices of new properties from the same market. Supporters of artificial neural networks purport that these models eliminate the non-linearity and outlier problems inherent to the hedonic pricing techniques (Brunson et al. 1994; Do and Grudnitski, 1992; Evans et al. 1992; Tay and Ho, 1991). However, there are limited studies in this area using an artificial neural network technique (Limsombunchai *et al.*, 2004). This study will investigate the applicability of Artificial Neural Network (ANN) in house rent prediction. The primary goal of this research is to develop an artificial neural network model for house rent prediction. The study will also use the results from a hedonic price model for house rent prediction and compare the predictive power of both models.

1.2 Objectives of the Study

The specific objectives of the study are given below:

- To develop an Artificial Neural Network (ANN) model for house rent prediction.
- To assess the relative influence of different attributes on house rent using artificial neural network
- To compare the predictive power of the artificial neural network model with that of a hedonic price model for house rent prediction.

1.3 Scope of the Study

This study investigated several aspects of the use of neural networks as a tool for predicting house rent. In particular, using a database of previous study, the study evaluated the ability of a neural network model to predict the rent of residential properties in a test sample within an acceptable range.

The study compared the importance of different attributes in house rent prediction by using the relative importance values of inputs estimated by the neural network models. Hence the importance of inputs estimated by the neural network model for the particular residential properties are only true for this specific study, not for other residential properties of different areas. Some cases were constructed in this study to test and compare the predictive power of several different neural network models and hedonic price models.

1.4 Limitation of the Study

To compare the ANN model with hedonic price model this study roughly followed the methodology used by Worzala *et al.* (1995). Longitudinal (time-dependent) data analysis is required for more reliable evidence of applicability of neural network in house rent prediction. But this longitudinal method can not be applied in this study

due to unavailability of time series data of house rent. Finally, the house rent could be affected by some other factors (such as quality of the environment, traffic noise and volume, interest rate, employment, income level and other socio-economic characteristics of area) which are not included in the development of the ANN model.

1.5 Organization of the Study

This dissertation comprises of seven chapters. The first chapter presents an introduction with the background and methodology of the study. The second chapter gives an idea of artificial neural network model and its application to the valuation of residential property. The third chapter provides an overview of the selected study area. The fourth chapter consists of study design methodology from selection of variables to determination of the ANN model with an overall description of the variables used in this study. The fifth chapter comprises of the results of developed ANN model and relative contribution of different attributes in house rent prediction. The sixth chapter provides a comparative analysis between ANN model and hedonic price model in predicting house rent. Finally, chapter seven summarizes the important findings of this study and gives some recommendations regarding the application of the model.

Chapter 2

LITERATURE REVIEW

Chapter 2: Literature Review

2.1 Introduction

Hedonic price model has been commonly used to estimate house rent and property value. Recently artificial neural network has been used as an alternative model of hedonic price model approaches. So it is necessary to understand the concept of artificial neural network before applying this model in house rent prediction. The basic notions of the study are presented in this chapter based on an extensive literature review.

2.2 Artificial Neural Network Model

2.2.1. Neural network systems

A neural network system is an artificial intelligence model that replicates the human brain's learning process. The brain's neurons are the basic processing units that receive signals from and send signals to many nervous system channels throughout the human body. When the body senses an input experience, the nervous system carries many messages describing the input to the brain. The brain's neurons interpret the information from these input signals by passing the information through synapses that combine and transform the data. A response is ultimately created when the information processing is complete. Through repetition of stimuli and feedback of responses, the brain learns the optimal processing and response to the stimuli. The brain's actual learning path is still somewhat of a chemical mystery; what is known is that learning does occur and reoccur through the repetition of the input stimuli and the output response(s).

Artificial neural networks were developed utilizing this "black box" concept. Just as a human brain learns with repetition of similar stimuli, a neural network trains itself with historical pairs of input and output data. Neural networks usually operate without an a priori theory that guides or restricts the relationship between the inputs

and the outputs. The ultimate accuracy of the predicted output response, rather than the description of the specific path(s) or relationship(s) between the inputs and the output response, is the goal of the model.

In an artificial neural network, nodes are used to represent the brain's neurons and these nodes are connected to each other in layers of processing. Figure 1 illustrates the three types of layers of nodes: the input layer, the hidden layer or layers (representing the synapses) and the output layer. The input layer contains data from the measures of explanatory or independent variables. This data is passed through the nodes of the hidden layer(s) to the output layer, which represents the dependent variable(s).

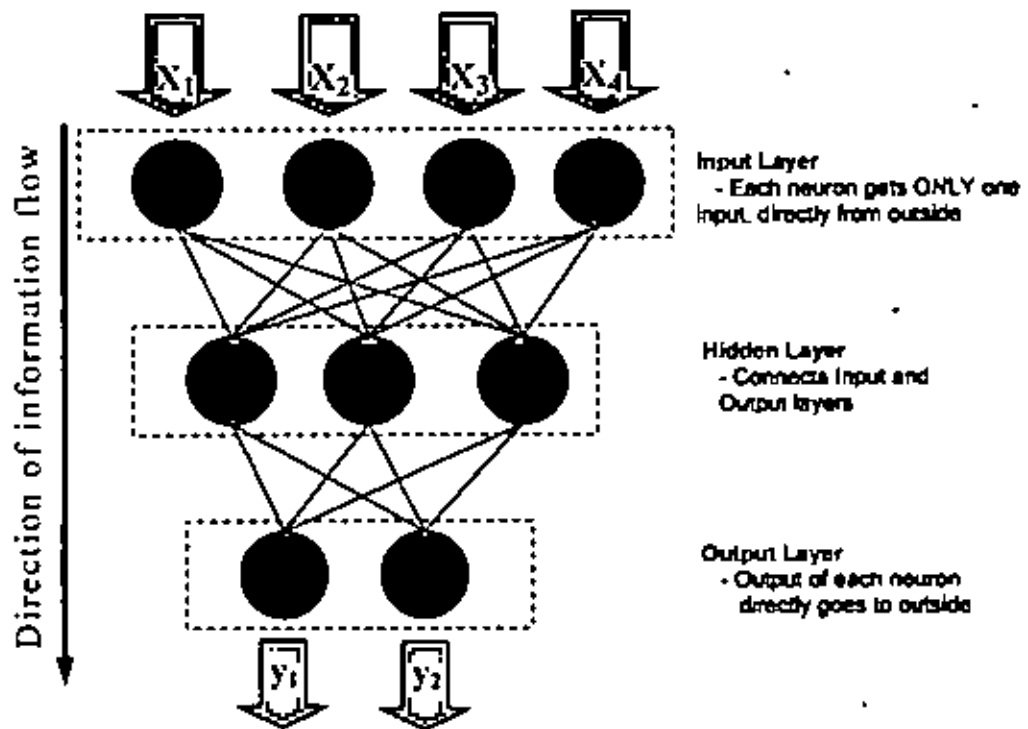


Figure 2.1: Neural Network Structure

The hidden layer(s) contain two processes: the weighted summation functions; and the transformation functions. Both of these functions relate the values from the input data (e.g. the property attributes) to the output measures (e.g. the sales price). The weighted summation function typically used in a feed-forward/back propagation neural network model is:

$$Y_j = \sum_j^n X_i W_{ij}$$

Where X_i is the input values and W_{ij} is the weights assigned to the input values for each of the j hidden layer nodes. A transformation function then relates the summation value(s) of the hidden layer(s) to the output variable value(s) or Y_j . This transformation function can be of many different forms: linear functions, linear threshold functions, step linear functions, sigmoid functions or Gaussian functions. Most software products utilize a regular sigmoid transformation function such as:

$$Y_T = \frac{1}{1 + e^{-y}}$$

This function is preferred due to its non-linearity, continuity, monotonicity, and continual differentiability properties (Borst, 1992; Trippi and Turban, 1993).

In most research, the initial neural network model is created utilizing a training set of input and output data. The most common form of neural network systems are termed "feed-forward" networks and begin with a default of randomly determined weights for each of the nodes in the hidden layer. The software feeds the input measures forward through the hidden layers. At each hidden layer, the information is transformed by a nonlinear transformation function to produce an output measure. The model then compares the model's output to the historical or actual output for discrepancy. If a discrepancy exists, the model works backwards from the output layer back through the hidden layer nodes, adjusting the weights so as to reduce the prediction error. This method of error correction is usually referred to as back-propagation. With each ordered pair of input measures and output responses from the training data set, the neural network repeats these steps until the overall prediction error is minimized. In practice, the neural network stops training when it either

reaches the default level of error or the researcher's pre designated maximum level of allowable error.

A trained neural network model can be tested for accuracy by letting it predict responses from new input measures. The neural network model's predictions can then be compared with the actual output for accuracy. The objective of the neural network is to find the set of weights for the explanatory variables that minimize the error between the neural network output and the actual data (Allen and Zumwalt, 1994). This similarity between neural networks and traditional statistics provides the opportunity for real estate appraisers to consider the use of this technology as a possible alternative to more common statistical techniques, such as multiple regressions (Brunson et al., 1994).

Disadvantages associated with neural networks are the speed of the learning process, the black-box nature of the back propagation training process and interpretation of the learned output. The latter two problems arise from the fact that the internal characteristics of a trained net are simply a set of numbers and therefore very difficult to relate back to the application in a meaningful fashion. In this respect rule induction, the automated process by which a decision tree is built is more explicit with rules identified to distinguish between different records within the data set (McGreal et al., 1997).

2.2.2 Application of neural networks to the valuation of residential property

From the early 1990s it was started to apply neural network technology to the valuation of residential property. Frequently these studies are in the form of comparative analysis, with researchers contrasting the findings and perceived efficiency of neural network models with more tried and tested statistical methods. Given the potential difficulties associated with regression modelling, namely functional form and non-linearity of variables (Adair *et al.*, 1996), neural networks have found a measure of intuitive appeal (Borst, 1992). Indeed, Do and Grudnitski (1992) concluded that a neural network model performs better than a multiple regression model for estimating the value of U.S. residential property. In related research, Do and Grudnitski (1993) utilized neural networks to investigate the

relationship of structure age to property price. Their results demonstrated that structure age has a non-linear effect on price rather than the strict negative monotonic relationship that is typically modelled with the hedonic pricing technique. The authors contend that this result supports the use of a non-linear technique, such as artificial neural networks, to appraise real estate.

Tay and Ho (1991) in a comparable study in Singapore, based on a larger sample (833 properties in the training sample and 222 in the test sample) of data from the apartment sector, reached similar conclusions with a mean absolute error of 3.9 per cent for the neural network model relative to 7.5 per cent for the regression model. In arguing the case for the use of neural networks in the mass appraisal of residential property, Tay and Ho are of the opinion that the network can learn valuation patterns for "true" open market sales in the presence of some "noise" (i.e. non-bona fide sales) as a way of establishing a robust estimator.

Borst (1992) utilized artificial neural networks and tested the predictive effects of data transformation, the exclusion of outliers, and the use of several output layer nodes to represent different price ranges or markets. Borst's neural network model boasted low mean absolute errors (8.7 per cent to 12.4 per cent) and he concluded that this new technique deserves strong consideration in the field of mass valuation.

Within the UK, Evans *et al.* (1992) tested the predictive accuracy of neural networks for estimating residential property prices and although based upon a small data set of 34 properties sold over a six month period, the results showed a reasonable level of accuracy with a mean absolute error of 13.48 per cent. Removal of outliers from both the training and test data resulted in a reduction in the mean absolute error to 5.03 per cent, concurring with Borst's inference that when outliers are removed from data sets, neural network models work well to value property. However, in drawing conclusions, they consider that neural networks are best regarded as a tool to assist, rather than as a system which could replace the valuer, pointing out that accuracy is extremely dependent on the careful choice of data for the training set.

McCluskey (1996) applied neural network technology on a sample of 416 residential properties sold from August 1992 to August 1994 in Northern Ireland, with 375 properties used to train the network. Initial results produced a mean absolute percentage error of 15.7 per cent and a predictive accuracy of 72 per cent, though removal of outliers improved the analysis (mean absolute percentage error of 7.75 per cent and a predictive accuracy of 93.6 per cent) leading McCluskey to conclude that neural networks excel in determining direct and indirect patterns of value related to property attributes. McCluskey's work, based upon data covering a two year period, encompasses an appreciably longer time-span than employed in other comparable studies. Although including a time-based variable, reverse date of sale, McCluskey attaches little significance to this variable apart from reference to the model's ability to learn the underlying pattern of values across property types reflecting both time and locational differences.

Worzala *et al.* (1995) adopt a contrary position and cast some doubt upon the role of neural networks *vis-à-vis* traditional regression analysis models, suggesting that caution is needed when working with neural networks. In undertaking analysis at varying levels of investigation and utilizing different neural network shells, the error magnitude for individual properties was found in some cases to be very significant (up to 70 per cent) and clearly not acceptable for a professional appraisal. Furthermore, the analysis showed that even when using the same data, results from models prepared by different neural network software packages could be inconsistent and do not always outperform regression models. Worzala *et al.* (1995) identify the need for further research regarding the application of neural network software before a final judgment is made concerning suitability to property appraisal/valuation. Indeed, follow-on work from Lenk *et al.* (1997) infers that substantial value estimation errors are possible, with at least one in six properties having value estimates in excess of 15 per cent of the actual price. Furthermore, by illustrating that 70 per cent of the outlier property predictions had estimation errors in excess of 15 per cent, Lenk *et al.* (1997) strongly maintain that outliers should be removed from the data. This position contrasts sharply with that advocated by Tay and Ho.

McGreal *et al.* (1997) evaluated the ability of a neural network model to predict the value of properties in a test sample within a range acceptable for valuation purposes by using a database of market sales. The best models showed that only 80 percent of properties achieve a predicted value within 15 percent of sale price which would be beyond the bounds of acceptability by the valuation profession. Various researchers have commented upon the black box nature of neural networks and the possibility of achieving opposite results with different models or model settings (Worzala *et al.*, 1995). McGreal *et al.* (1997) reinforced this argument with varying outcomes between rule and net based models as the valuation threshold is altered.

2.3 Hedonic Price Model Approach in House Rent Prediction

The hedonic price model, derived mostly from Lancaster's (1966) consumer theory and Rosen's (1974) model, posits that a good possesses a myriad of attributes that combine to form bundles of utility-affecting attributes that the consumer values. In Rosen's approach, residential properties are characterized as a set of complex heterogeneous goods. At the same time, each property or good consists of an inseparable bundle of homogeneous attributes that differ in values and characteristics. The underlying theory for the market of heterogeneous good states that the price of the good is a function of the levels or value of each attribute in the bundle. In the housing market, these attributes are usually structural and site characteristics of a property.

Hedonic price theory assumes that a commodity such as a house can be viewed as an aggregation of individual components or attributes. Consumers are assumed to purchase goods embodying bundles of attributes that maximize their underlying utility functions. Rosen (1974) describes the process in which prices reveal quality variations as relying on producers who "tailor their goods to embody final characteristics described by customers and receive returns for serving economic functions as mediaries". Hedonic price theory originates from Lancaster's (1966) proposal that goods are inputs in the activity of consumption, with an end product of a set of characteristics.

Bundles of characteristics rather than bundles of goods are ranked according to their utility bearing abilities. Attributes (for example, characteristics of a house such as number of bedrooms, number of bathrooms, number of fireplaces, parking facilities, living area and lot size) are implicitly embodied in goods and their observed market prices. The amount or presence of attributes with the commodities defines a set of implicit or "hedonic" prices (Lancaster, 1966). The marginal implicit values of the attributes are obtained by differentiating the hedonic price function with respect to each attribute (McMillan *et al.*, 1980). The advantage of the hedonic methods is that they control for the characteristics of properties, thus allowing the analyst to distinguish the impact of changing sample composition from actual property appreciation.

While the hedonic technique is an acceptable method for accommodating attribute differences in a house price determination model, it is generally unrealistic to deal with the housing market in any geographical area as a single unit. Therefore, it seems more reasonable to introduce geographical information or location factor into a model that allows shifts in the house price level. Frew and Wilson (2000) employ the hedonic price model to examine the relationship between location and property value, in Portland, Oregon, and the authors found that there was a significant relationship between location and property value. Fletcher *et al.* (2000) examine whether it is more appropriate to use aggregate or disaggregate data in forecasting house price using the hedonic analysis. It is found that the hedonic price coefficients of some attributes are not stable between locations, property types and age.

However, it is argued that this can be effectively modeled with an aggregate method. The hedonic price model has also been used to estimate individual external effects (e.g. environmental attribute) on house prices (Limsombunchai *et al.*, 2004).

2.4 Artificial Neural Network Vs Hedonic Price Model in House Rent Prediction

Even though the hedonic price model has been widely recognized, issues such as model specification procedures, multicollinearity, independent variable interactions, heteroscedasticity, non-linearity and outlier data points can seriously hinder the performance of hedonic price model in real estate valuations. The artificial neural network model has been offered as a possible solution to many of these problems, especially when the data patterns show non-linearity (Lenk *et al*, 1997; Owen and Howard, 1998). Tay (1991) using a large sample of data from the apartment sector in Singapore, found that a neural network model performs better than a multiple regression model for estimating value. Do and Grudnitski (1992), Borst (1992) and McCluskey (1996) gave same results in their studies.

Do and Grudnitski (1992) reported significant superior predictive performance by their artificial neural network model when estimating 105 residential property values. Their neural network model results contained twice the number of predicted values within 5 per cent of actual sales price as their hedonic model (40 per cent vs. 20 per cent). Furthermore, the mean absolute error from their neural network model was significantly lower than the mean absolute error from the hedonic model (6.9 per cent vs. 11.3 per cent).

Artificial neural networks have not always produced superior real estate price estimations over hedonic models. Worzala *et al.* (1995) directly challenged the findings of both Do and Grudnitski (1992) and Borst (1992). These researchers were unable to replicate the superiority of the artificial neural network model over the more traditional hedonic model when they applied the methodology of the prior studies to a new data set, even after manipulating the number of hidden layers, the number of nodes within the hidden layer(s), and the hidden layer error threshold levels of their neural network model. In each case tested, their hedonic pricing model either did better than or performed similarly to their best artificial neural network model.

Limsombunchai *et al.* (2004) compared the predictive power of the hedonic price model with an artificial neural network model on house price prediction by using 200 houses information in Christchurch, New Zealand. The results from hedonic price models of this study support the previous findings. Even, if the R^2 of hedonic price models are high (higher than 75%) in sample forecast, the hedonic price models do not outperform neural network models. Moreover, the hedonic price models show poor results on out-of-sample forecast, especially when comparing with the neural network models. The empirical evidence presented in this study supported the potential of neural network on house price prediction. The artificial neural network model can overcome some of the problems related to the data patterns and underlying assumption of the hedonic model (Limsombunchai *et al.*, 2004).

James (1996) points out the advantages of neural networks in terms of small data sets. Neural networks would seem to be a better tool for smaller data sets while regression is clearly superior for larger data sets. Regression is statistically poor with small data sets, a problem not encountered by neural networks (Rossini, 1997). Rossini (1997) supported the superiority of neural networks for small data sets based upon the time required to produce the model. Regression results can be calculated very quickly regardless of the size of the problem while the time needed to produce neural networks seems to increase exponentially with the size of the data set.

Motivated by these conflicting conclusions concerning the usefulness of neural networks to predict value, the premise for this study was to provide further evidence concerning the Do and Grudnitski (1992) and Borst (1992) conclusions that neural network models significantly outperform hedonic price models in house rent prediction.

2.5 Summary

The literature shows that there was mixed success with the ANN method, probably due to different variable inputs and market conditions. While Borst (1992) and McCluskey (1996) stated that the predictive abilities of ANN were well established through investigative studies, James (1996) feels that more work must be done on "real world data sets in order to validate the methods for use in appraisal". Since no such study was performed based on Bangladeshi data, this study seeks to apply the ANN model to Bangladeshi data. The results of this study would go some way to establishing the usefulness of this method to Bangladeshi market condition. On the basis of the concepts and techniques illustrated in literature review the following chapter presents analytical methodology of the study.

Chapter 3
METHODOLOGY
AND STUDY DESIGN

Chapter 3: Methodology and Study Design

3.1 Introduction

To achieve the objectives of the study it is necessary to develop a methodology for the study. The methodology used for developing the neural network model for house rent prediction is described in this chapter. The collection procedure of data, selection criteria of different variables and characteristics of different data are portrayed in the following sections.

3.2 Methodology of the Study

The preliminary step of the study starts with extensive literature survey and review to develop a clear understating of the concepts of artificial neural network and its application for house rent prediction. It also provides familiarity with concepts of hedonic price models. In this stage the objectives of the study have been formulated. Three objectives have been identified for this study. Then, the dependent and independent variables are identified based on the variables used in an already developed hedonic price model. All the data used in this study have been collected from secondary source. Different statistical software is used to prepare inputs of artificial neural network (ANN) model development. For the development of ANN model, a back-propagation neural network software package is used. Finally different statistical analyses are performed using different statistical software for making comparison between ANN model and hedonic price model. Figure 1.1 provides with an overview of the methodological framework discussed above.

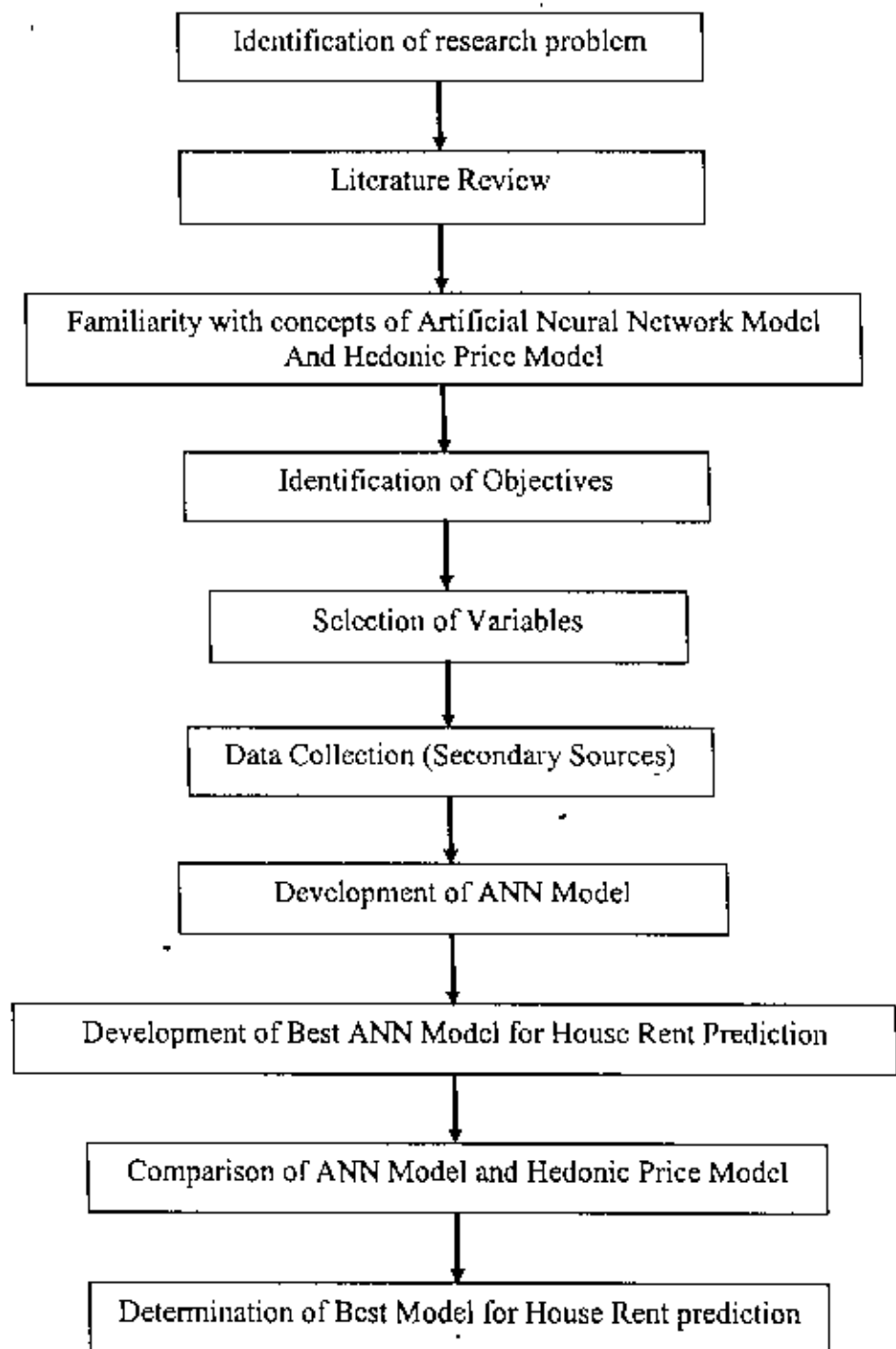


Figure 3.1: Methodological Framework of the Study

3.3 Study Design

3.3.1 Selection of variables and study area

One of the main objectives of this study is to compare the predictive power of artificial neural network (ANN) model with the hedonic price model for house rent prediction. To do this an already developed hedonic price model for house rent prediction of Rajshahi City (Habib, 2004) has been used. To ensure the similarity of the variables of the hedonic price model utilized by Habib (2004), the ANN models in this study have been built using same independent variables and same study area. In hedonic price models three types of attributes are used, namely structural attributes, neighborhood attributes and transportation attributes. In the aforementioned model, these three attributes include fourteen independent variables which are discussed in the following sections. Rajshahi City Corporation area has been selected as the study area of this study to keep the similarity with Habib (2004).

3.3.1.1 Residential asking rental price

To develop the ANN model residential advertised rental prices (in Taka during May 2004 period) have been selected as the dependent variable. There are two major characteristics of the dependent variable used by Habib (2004). The first one is related to the use of rental price instead of selling price or land value. The second one refers to the use of the asking rental price instead of the actual or market rental price.

3.3.1.2 Structural attributes

Prices of properties are frequently related to their structural attributes. Structural attributes include usable living area (in square feet), number of bedrooms and total number of bathrooms. In addition, age of building was used as a proxy for structural quality of house. The use of this proxy variable in hedonic price model was justified on the premise that structures tend to wear out with age or become obsolete, which may reduce the potential marketability of the property (Habib, 2004).

3.3.1.3 Neighborhood attributes

Since measures of neighborhood quality and neighborhood-level externalities are expected to influence residential property rent prices, a set of demographic, land use and amenities at the neighborhood level were included in the study design of Habib (2004). Most of these variables required the use of an elaborate GIS-aided approach to assign neighborhood-level data to each residential property. The hedonic price models were specified with population density as a demographic variable which was measured by persons per acre at each ward (the lower-tier administrative unit of the city corporation investigated). Land use variables includes the percentage of urbanized area dedicated to commercial land uses, residential land uses or community facilities. The percentage of area dedicated to each specific land use at ward level was obtained from Rajshahi Master Plan Project for the year 2004. Both land use and population density data for the wards were assigned to the individual residential properties that fall inside the respective wards (Habib, 2004). As for amenity variables, only the Euclidian distance to nearest drainage network is considered in this study.

3.3.1.4 Transportation attributes

Following most other studies, Habib (2004) selected the accessibility to the central Business District (CBD) as a transportation attribute for developing the hedonic price model. The other transportation attributes include accessibility to the major roads (city arterials from the individual residential properties at Rajshahi, accessibility to the wholesale markets, shopping centers and educational institutions.

Since basic educational institutions are major concerns and necessity at the neighborhood level, only primary schools were considered for accessibility to the educational institutes. Accessibility to the wholesale markets includes three major wholesale shopping agglomerations in the Rajshahi City. Besides retail shopping and commercial markets are considered as the shopping centers. The description of variables is summarized in Table 3.1.

3.3.2 Collection of data

To ensure the similarity of data set of the hedonic price model utilized by Habib (2004), the same data set was used in this study to develop the ANN model. The study was also supported by the GIS database produced by the Rajshahi Master Plan Project.

3.3.3 Development of ANN models

To develop the ANN models a back-propagation neural network software package, *NeuroShell* (Ward Systems Group, Inc.), has been used. The study used SPSS and Microsoft Excel for statistical analysis to compare the two models.

3.4 Data

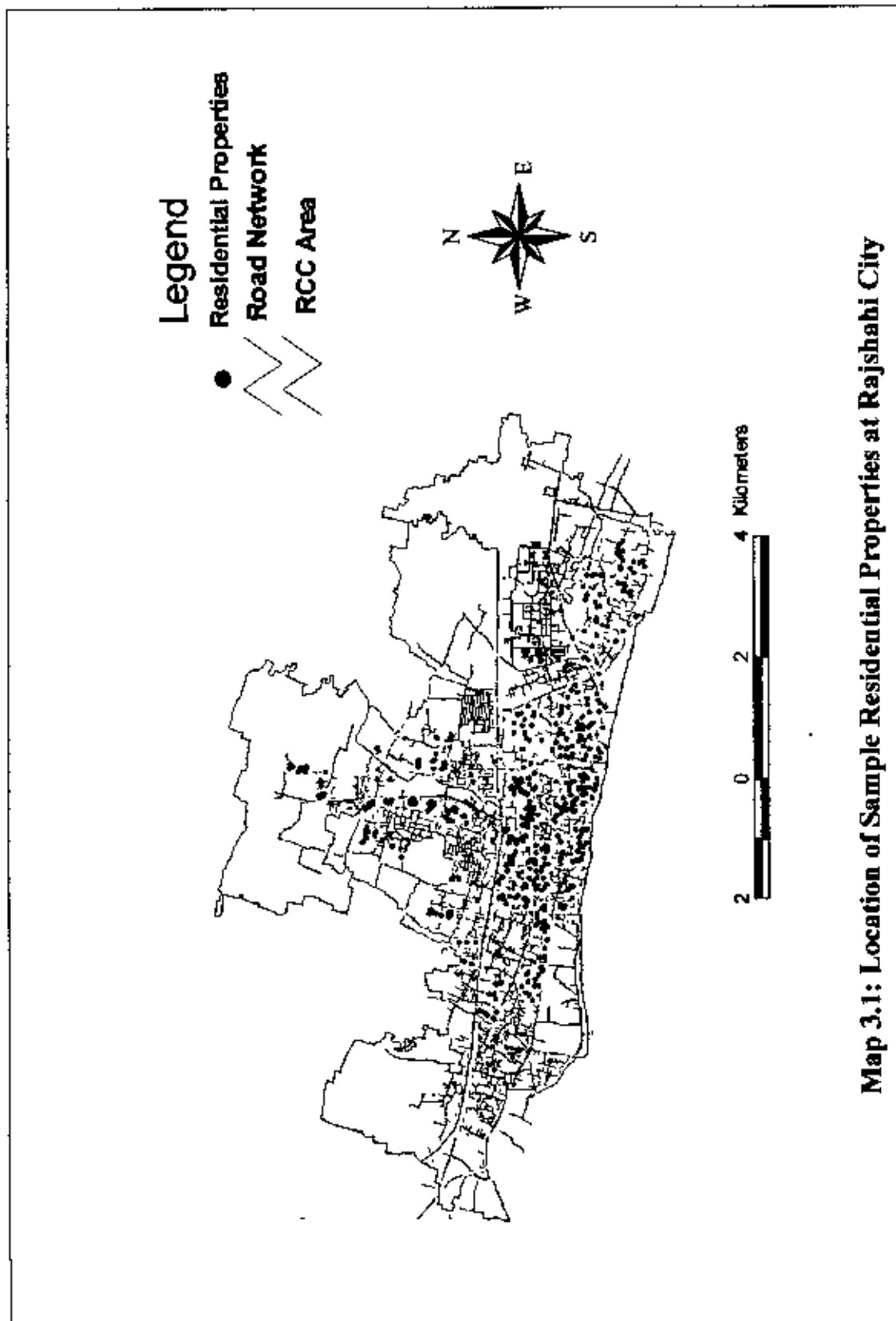
The data set of this study consists of a sample of 479 single-family and multi-family residential properties available for rent which was the final data set for the hedonic price model. In Habib (2000) study, residential properties had been identified through field visual inspection of "To Let" advertisements on properties and/or street electric poles near the residential buildings available for rent. Because such types of advertisements at residential areas were widely used as a formal method to provide information for rent at Rajshahi City. However, few properties had also been identified which were advertised for rent having local knowledge from inhabitants of the area during field surveys in the City. Questionnaire surveys have been carried out by the qualified surveyors (mostly, students of the University of Rajshahi). Information regarding residential advertised rent prices and structural attributes had been collected for all properties available for rent during field survey within the specified RCC area. Although 550 properties were originally surveyed by Habib (2004), 55 properties were discarded during geo-coding operation and 16 survey sheets were lacking substantial structural information. Map 3.1 shows the location of sample residential properties and Map 3.2 shows the monthly asking rent of residential properties.

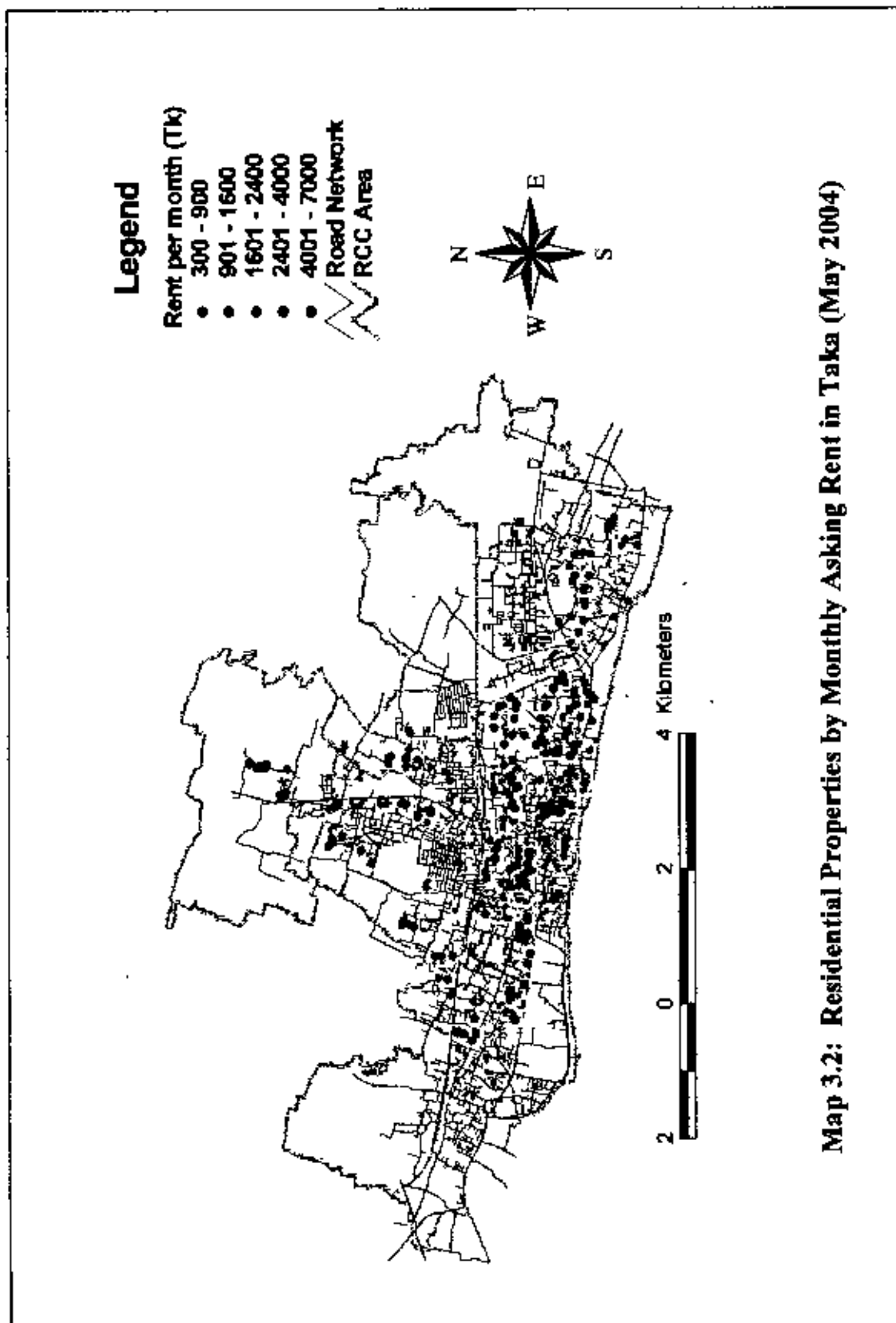
The average usable living area of the sample houses is 1531.96 sq. ft. Number of bedrooms and bathrooms in the houses vary from 1 to 4 and 0 to 3 respectively. The average age of building structures is approximately 19 years (Habib, 2004). Maps 3.3, 3.4, 3.5 and 3.6 show the locations of residential properties with their structural attributes.

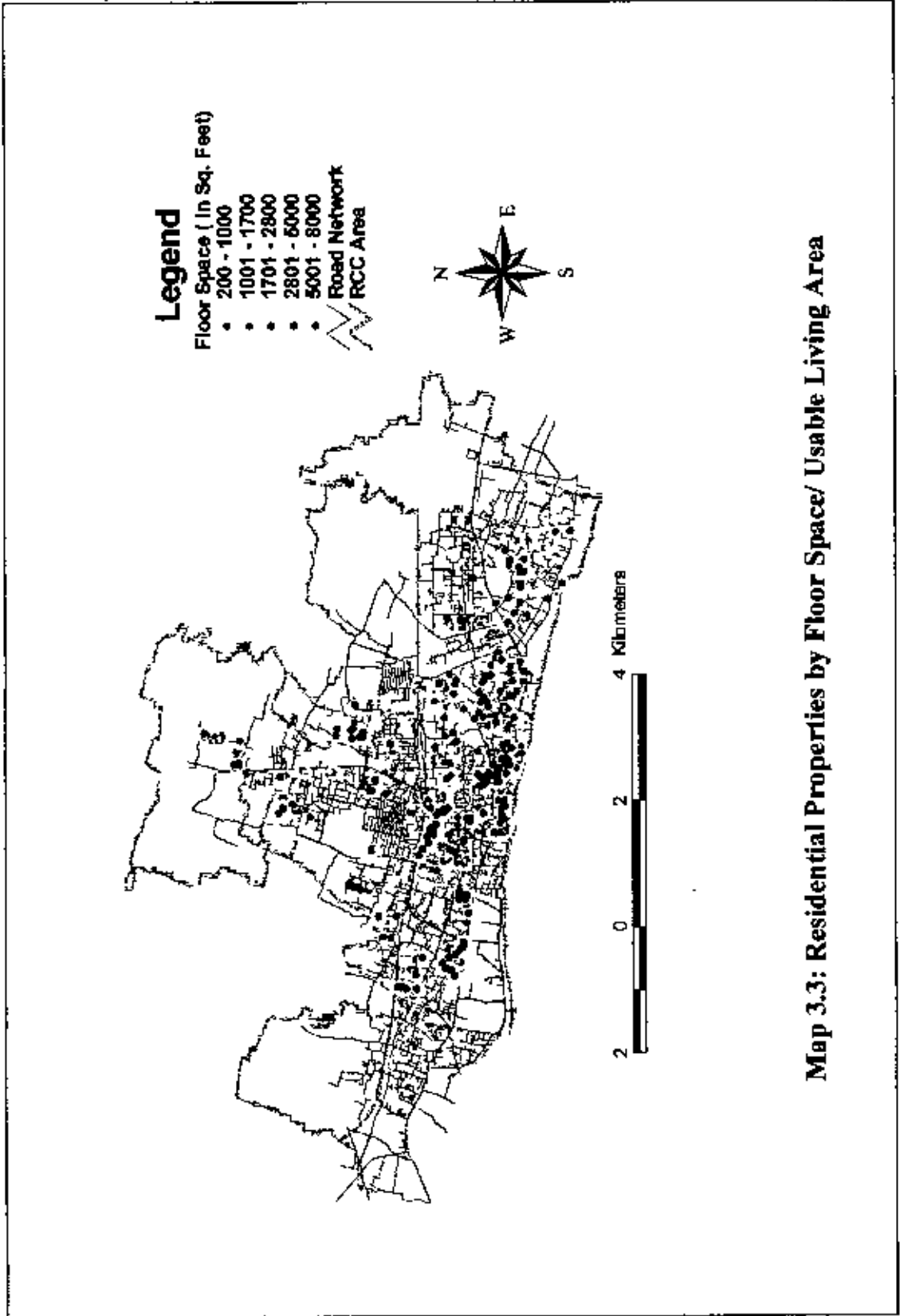
The data for population density was obtained from the Rajshahi Master Plan Project. Map 3.7 shows the population density (persons per acre for the year 2001) by ward which has been prepared with few computational works and assigned to the properties that fall within the respective administrative unit (ward) concerned.

Table 3.1: Description of Variables

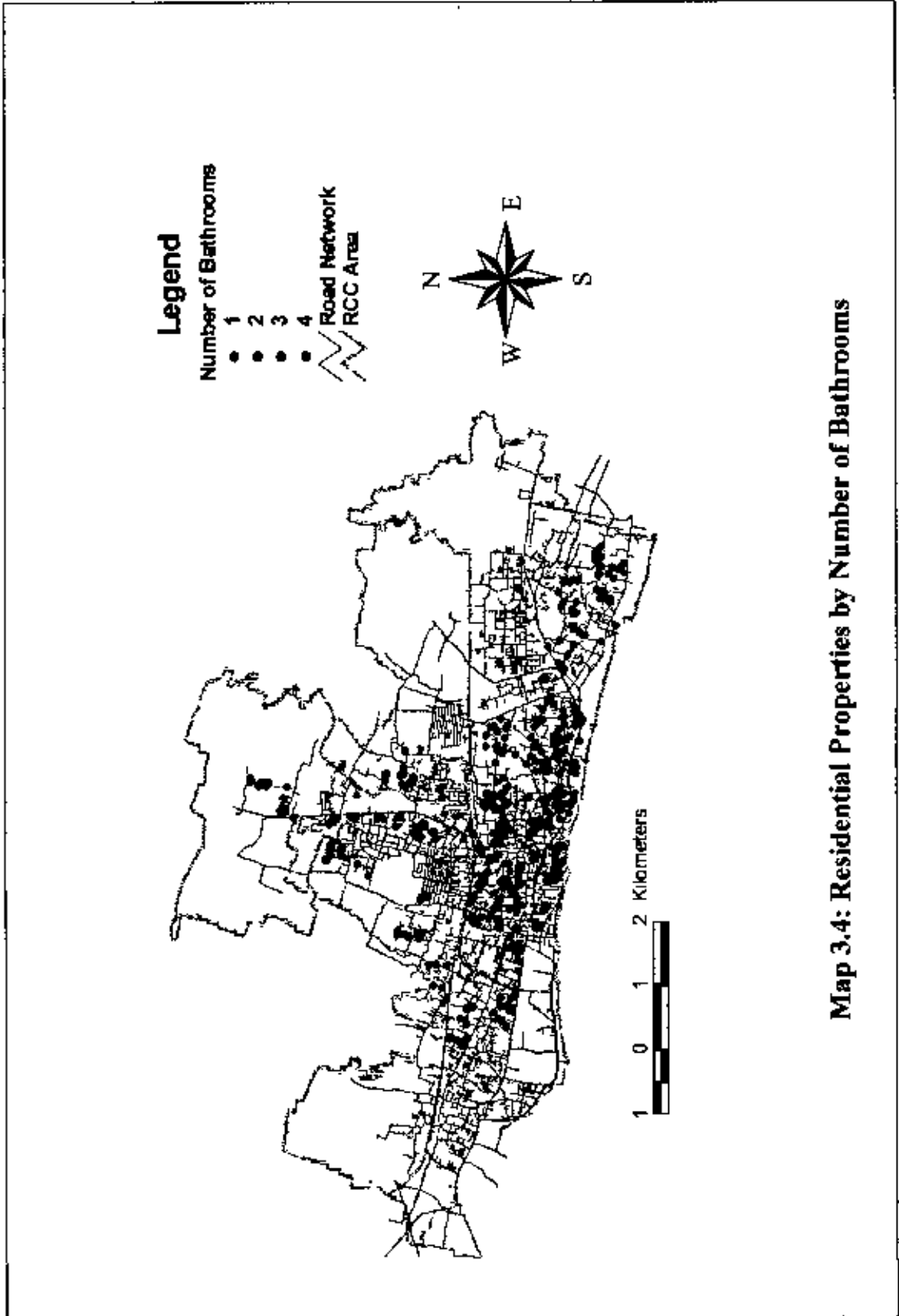
| Variable | Definition | Spatial level of data |
|----------------------------------|---|------------------------------|
| Measures of Value | | |
| RENT | Rent offered price (Tk.) | Property |
| Structural attributes | | |
| FL_SPACE | Usable living area (sq. ft) | Property |
| BEDS | Number of bedrooms | Property |
| BATHS | Number of bathrooms | Property |
| BLD_AGE | Age of residential property structure | Property |
| Neighborhood attributes | | |
| POP_DENS | Population density (persons per acre) | Ward |
| RES_LUSE | Percentage of area dedicated to residential use | Ward |
| COM_LUSE | Percentage of area dedicated to commercial use | Ward |
| COMMU_LU | Percentage of area dedicated to community facilities | Ward |
| DRAINAGE | Euclidian distance from the property to nearest point of drainage network | Property |
| Transportation attributes | | |
| M_RD_ACC | Network access distance from property to major roads | Property |
| CBD_ACC | Network access distance from property to Central Business District (CBD) | Property |
| W_MAR_AC | Network access distance from property to wholesale markets | Property |
| EDU_ACC | Network access distance from property to primary school | Property |
| SHOP_ACC | Network access distance from property to shopping centers | Property |



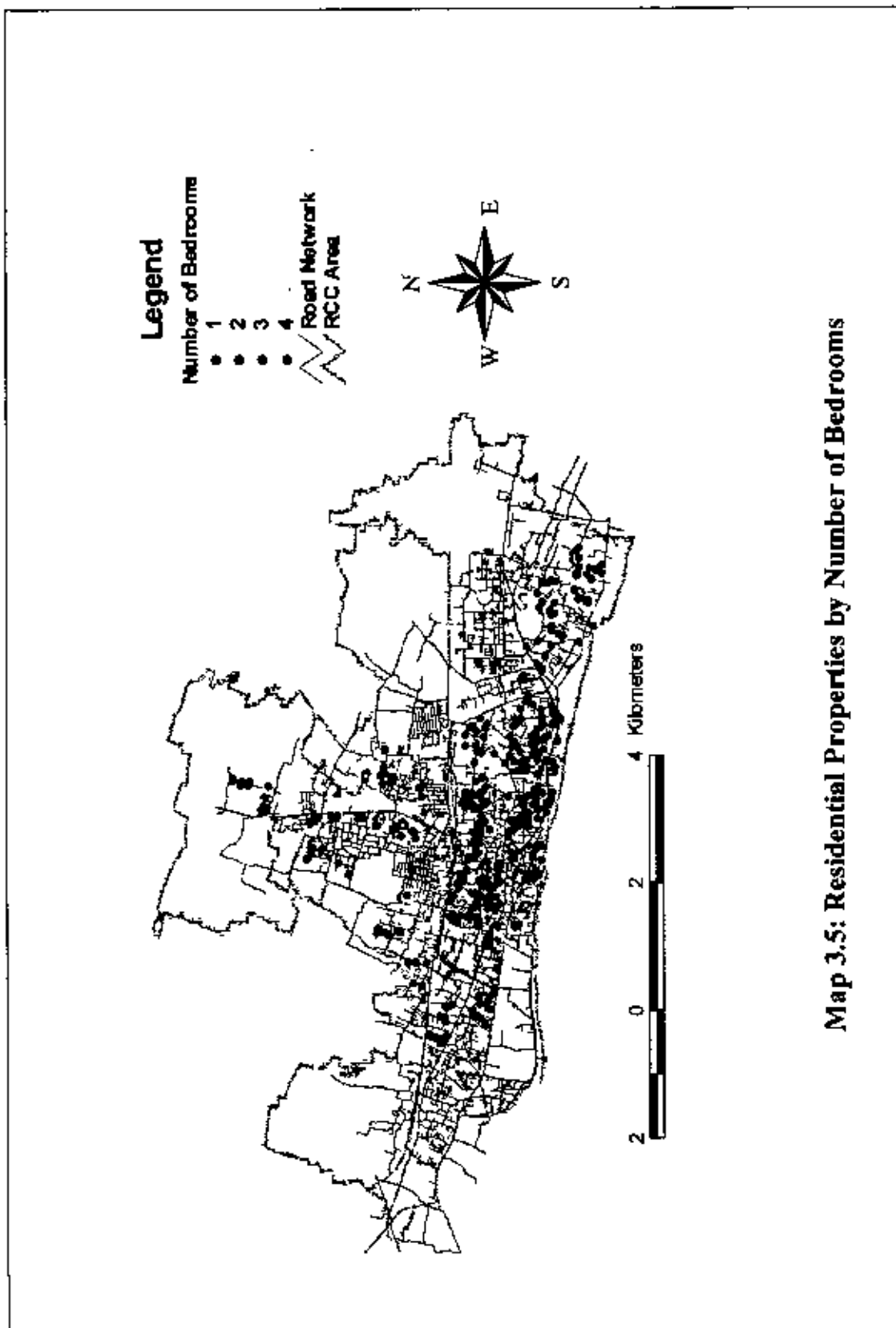




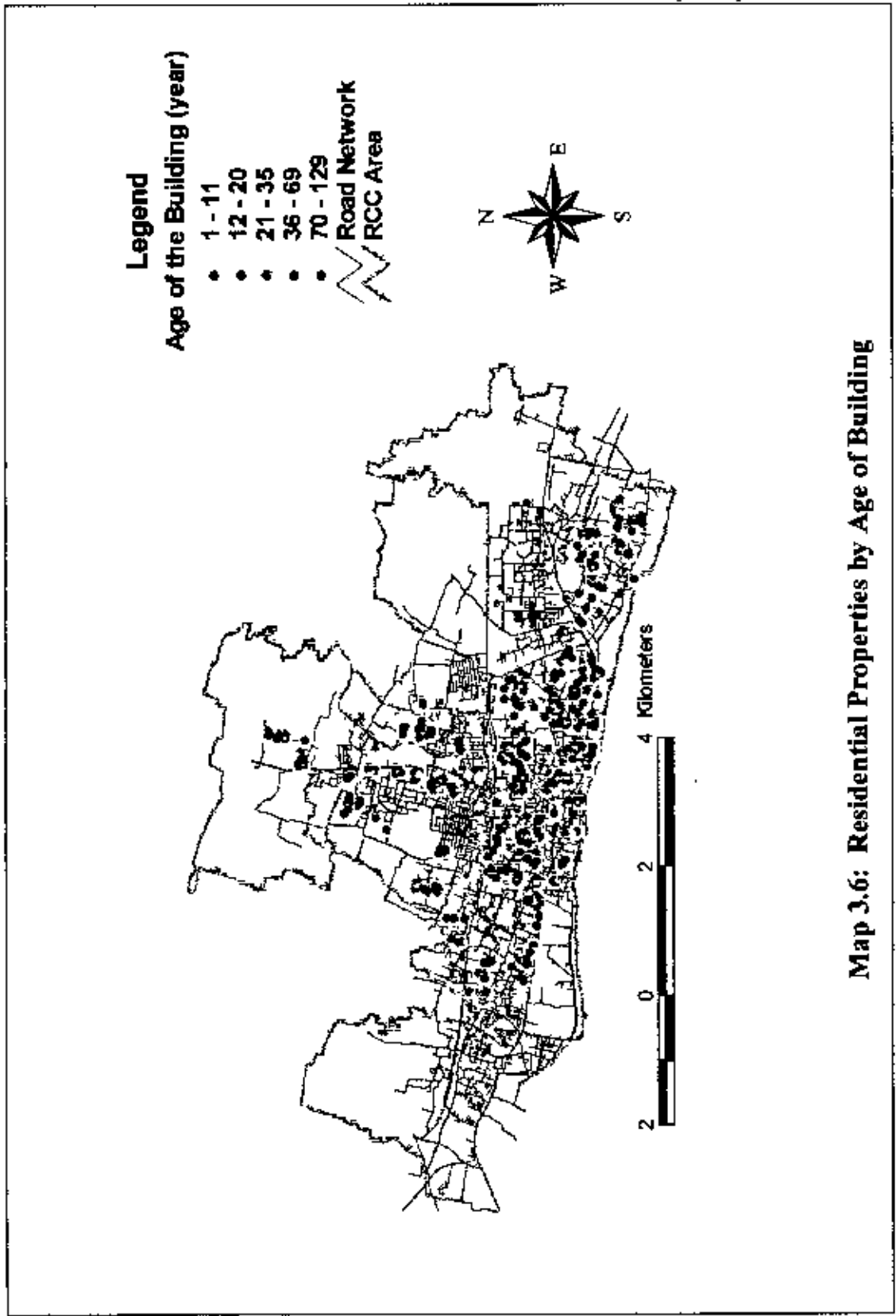
Map 3.3: Residential Properties by Floor Space/ Usable Living Area



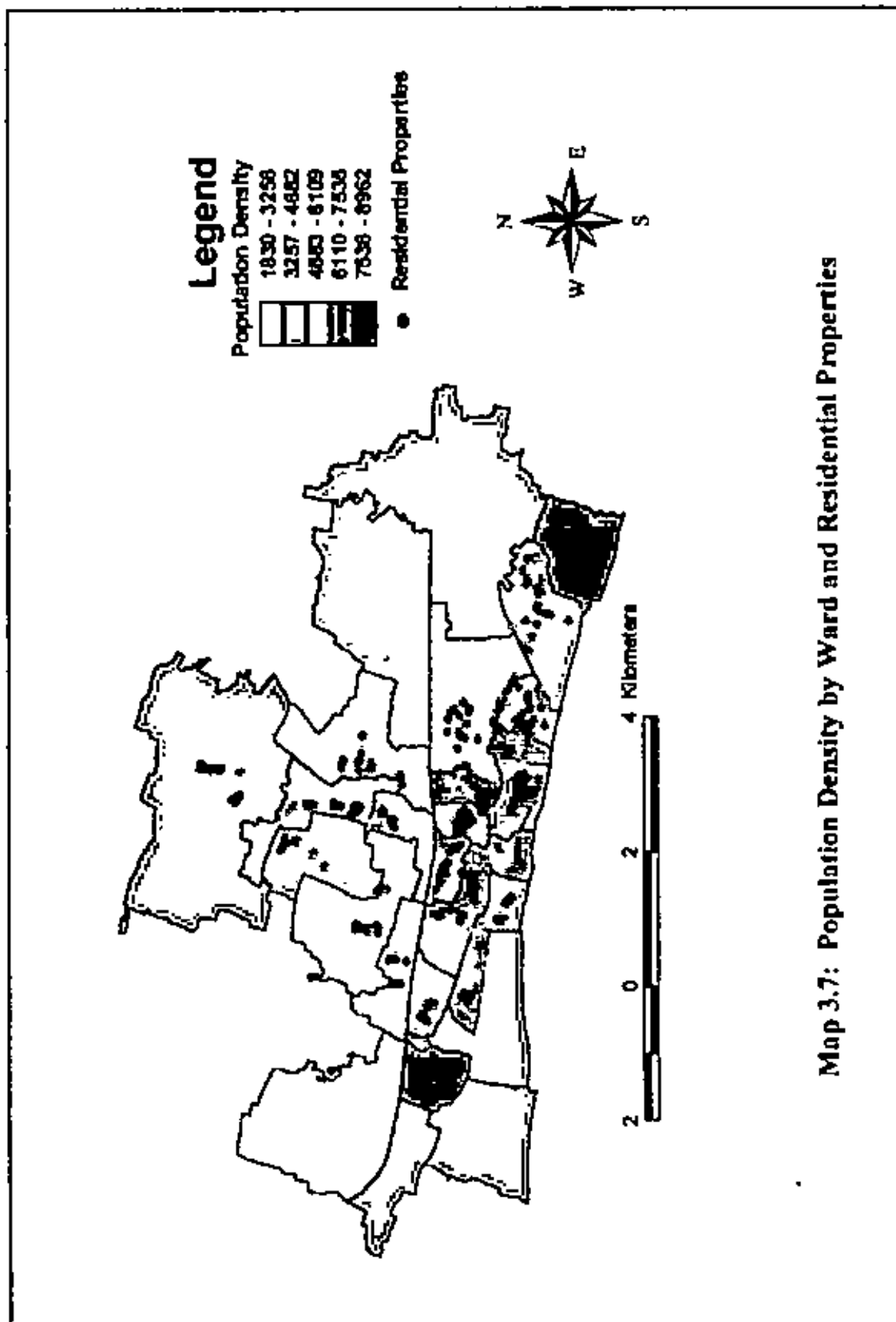
Map 3.4: Residential Properties by Number of Bathrooms



Map 3.5: Residential Properties by Number of Bedrooms



Map 3.6: Residential Properties by Age of Building



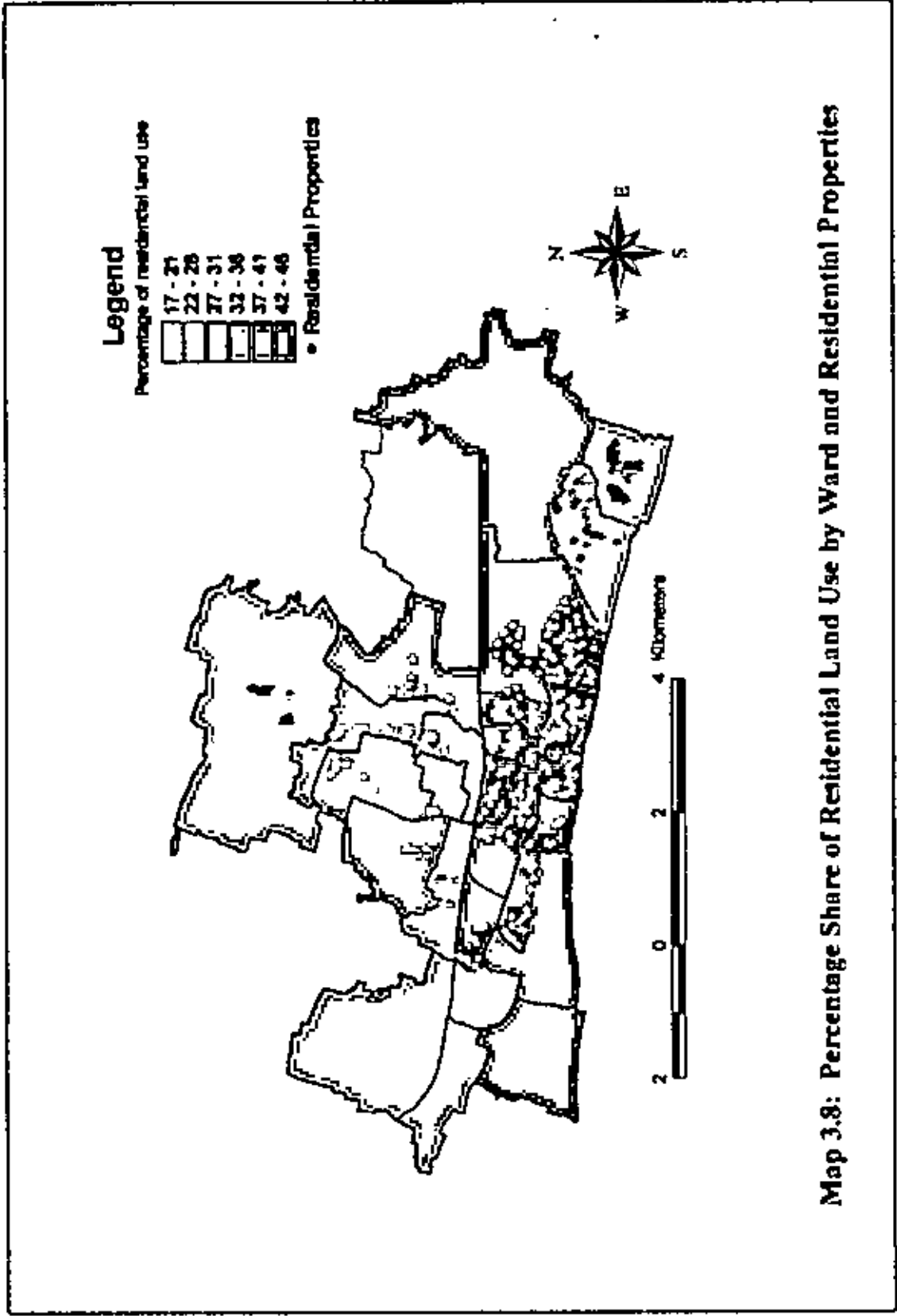
Three types of land use namely residential, commercial and community facilities are considered in this study. The percentage of land use is calculated from the GIS database of Rajshahi Master Plan Project. The percentage share of respective land uses by Strategic Planning Zone (SPZ) defined by Rajshahi Master Plan Project is shown in Table 3.2. All the residential properties are assigned the respective value of the percentage of land uses, which fall within the respective zone (SPZ). Maps 3.8, 3.9 and 3.10 show ward wise percentage share of residential land use, commercial land use and community facilities respectively.

Table 3.2: Percentage share of land uses by SPZ

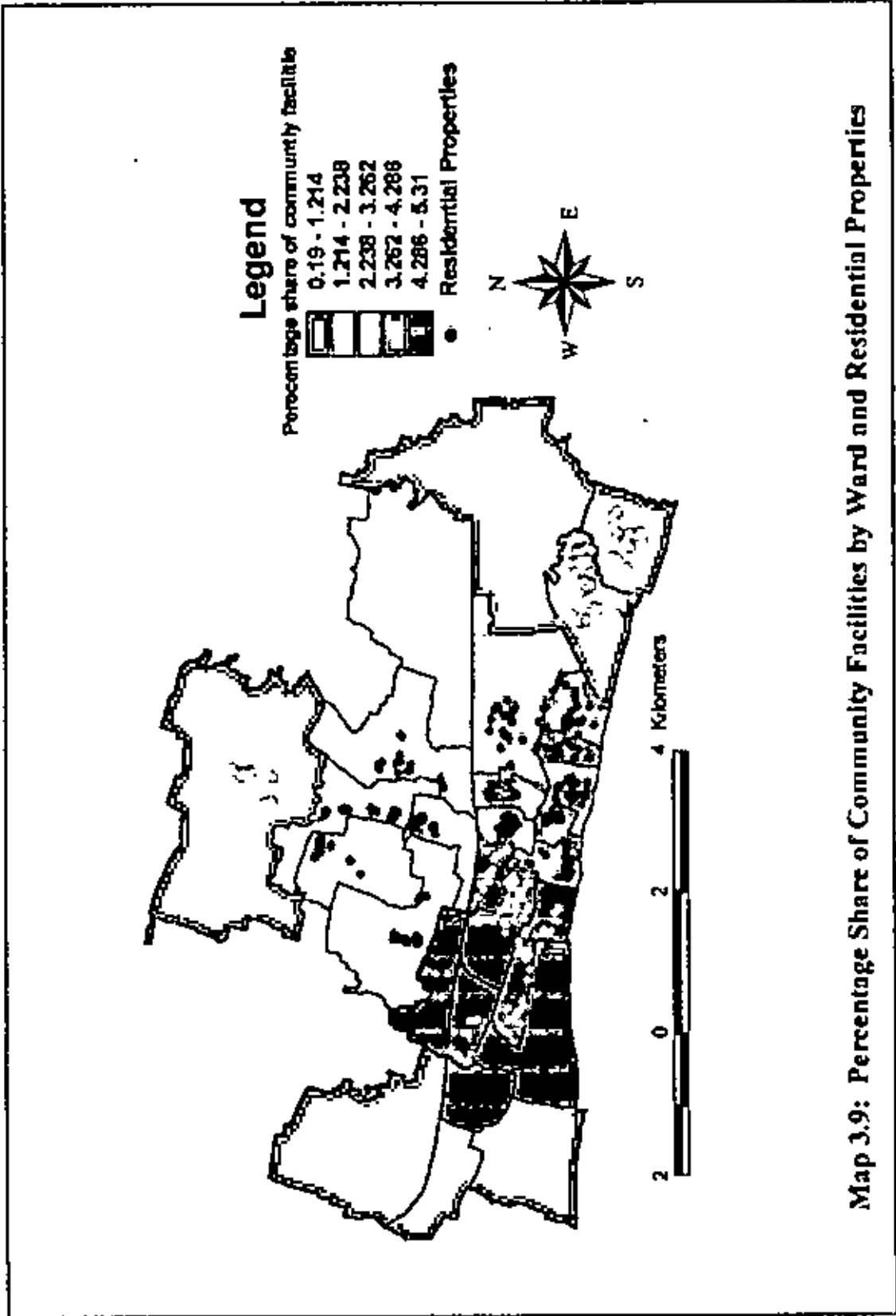
| SPZ No | Ward No | Area in acre | Residential (%) | Commercial (%) | Community facilities (%) |
|--------|--------------------------------|--------------|-----------------|----------------|--------------------------|
| 8 | 17 | 1726.43 | 27.04 | 1.36 | 0.19 |
| 13 | 26 | 1078.29 | 16.46 | 0.43 | 1.3 |
| 14 | 14, 15, 16, 18, 19 & Cant | 2055.54 | 40.56 | 1.83 | 2.21 |
| 15 | 1,2,4 | 1753.66 | 31.11 | 1.65 | 0.75 |
| 17 | 3, 5, 6, 7, 8, 9, 10, 11, 13 | 1679.85 | 45.35 | 8.63 | 5.31 |
| 18 | 12, 20, 21, 22, 23, 24, 25, 27 | 1372.89 | 43.83 | 7.69 | 3.15 |
| 19 | 28, 29, 30 | 2204.33 | 28.41 | 3.54 | 1.03 |

Source: Habib, 2004

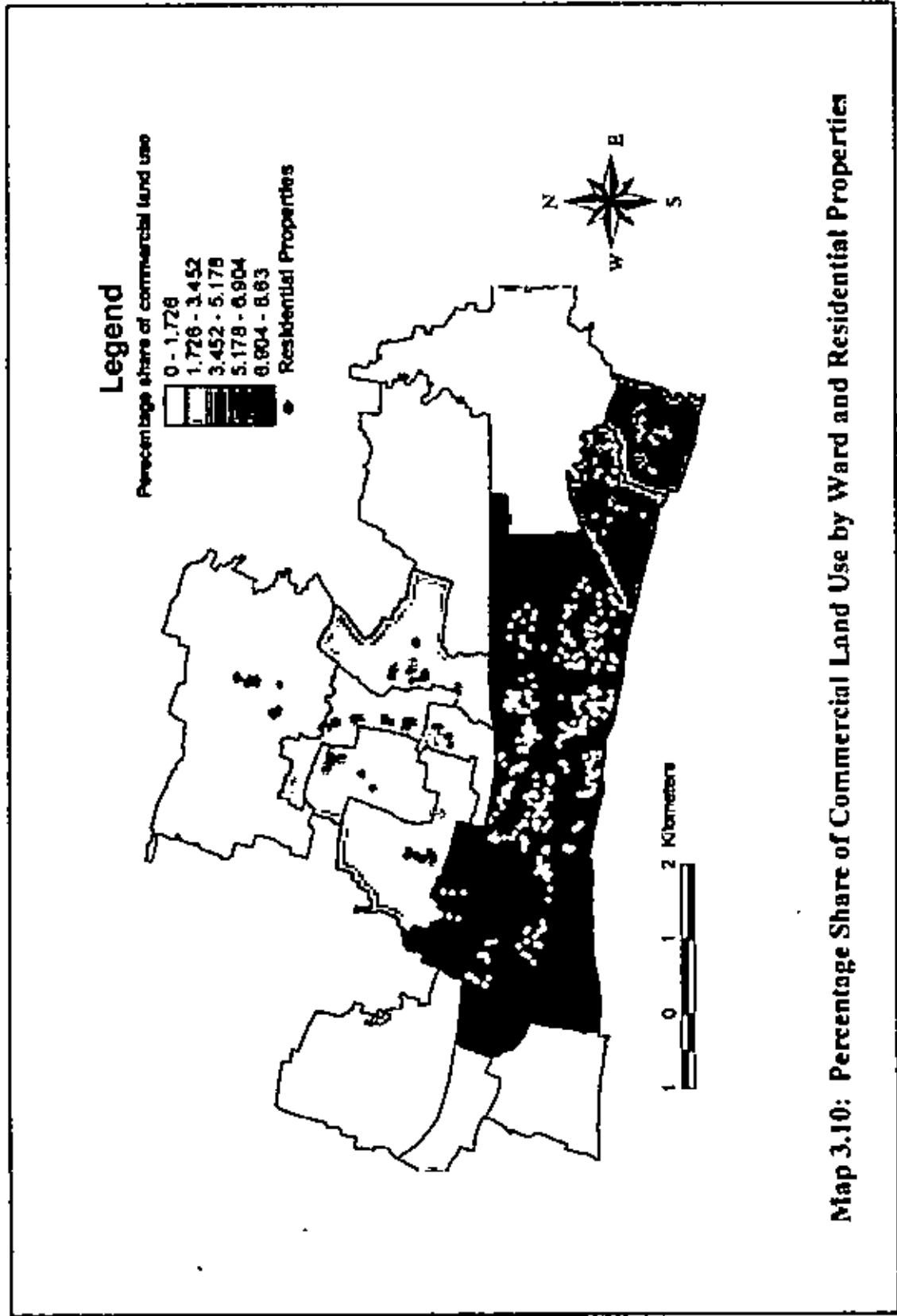
The Saheb Bazar area was considered as the Central Business District (CBD) of Rajshahi City. The area comprises most of the commerce and business centers of the Rajshahi City (Habib, 2004). Map 3.11 shows the point location of the CBD with respect to residential properties. Rani Bazar, Kadirgonj and Saheb Bazar are the major wholesale markets of Rajshahi City (DDC Limited, 2004). Map 3.12 shows the locations of the wholesale markets with respect to the residential properties. The major retail markets and shopping centers of Rajshahi City are New Market, C & B Market, Laxmipur, Upashahar New Market and Horogram markets (Habib, 2004). Map 3.13 shows the location of shopping centers which are considered as shopping centers for this study. The location of primary schools with respect to residential properties is shown in Map 3.14 and Map 3.15 shows the location of residential properties with respect to drainage network.

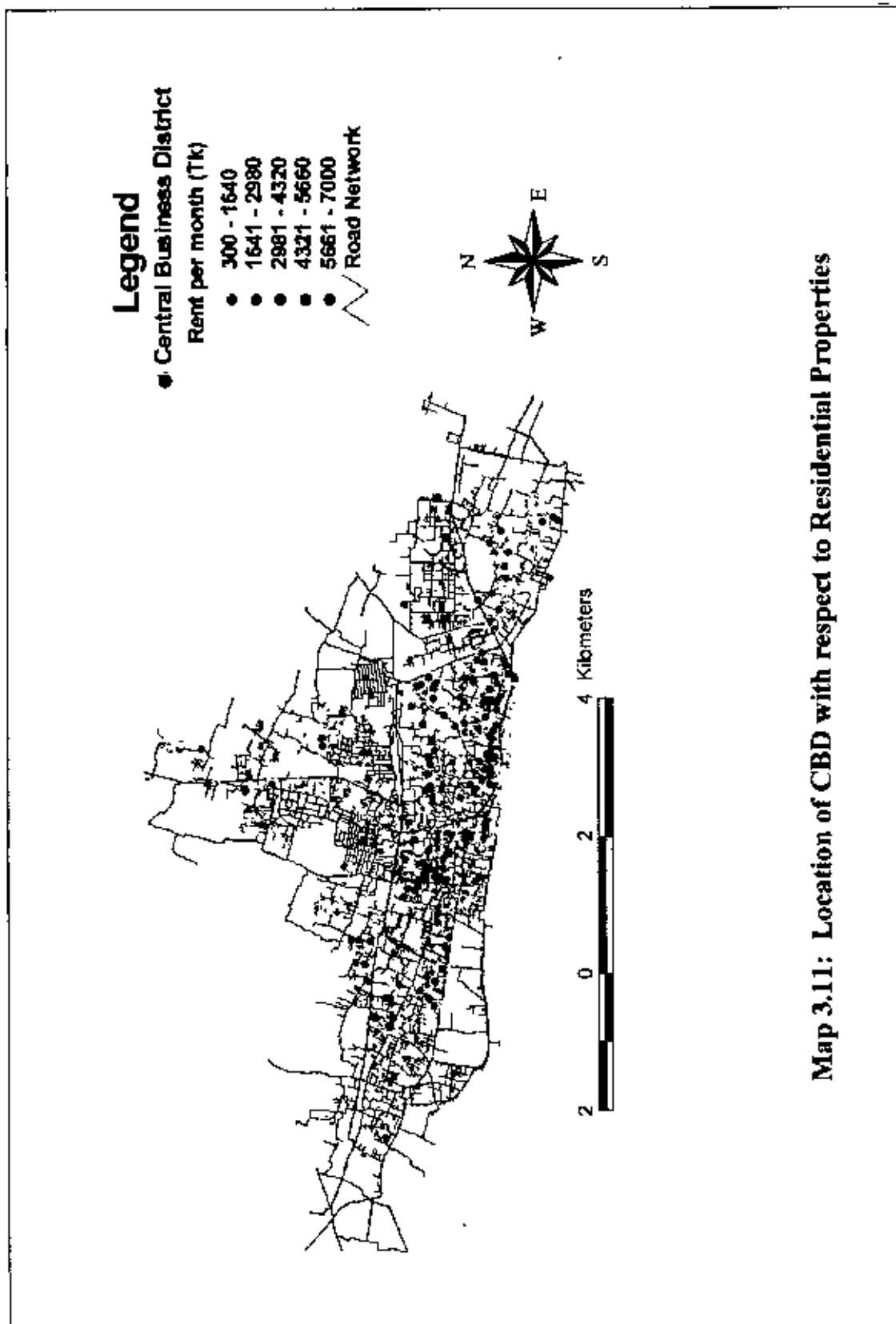


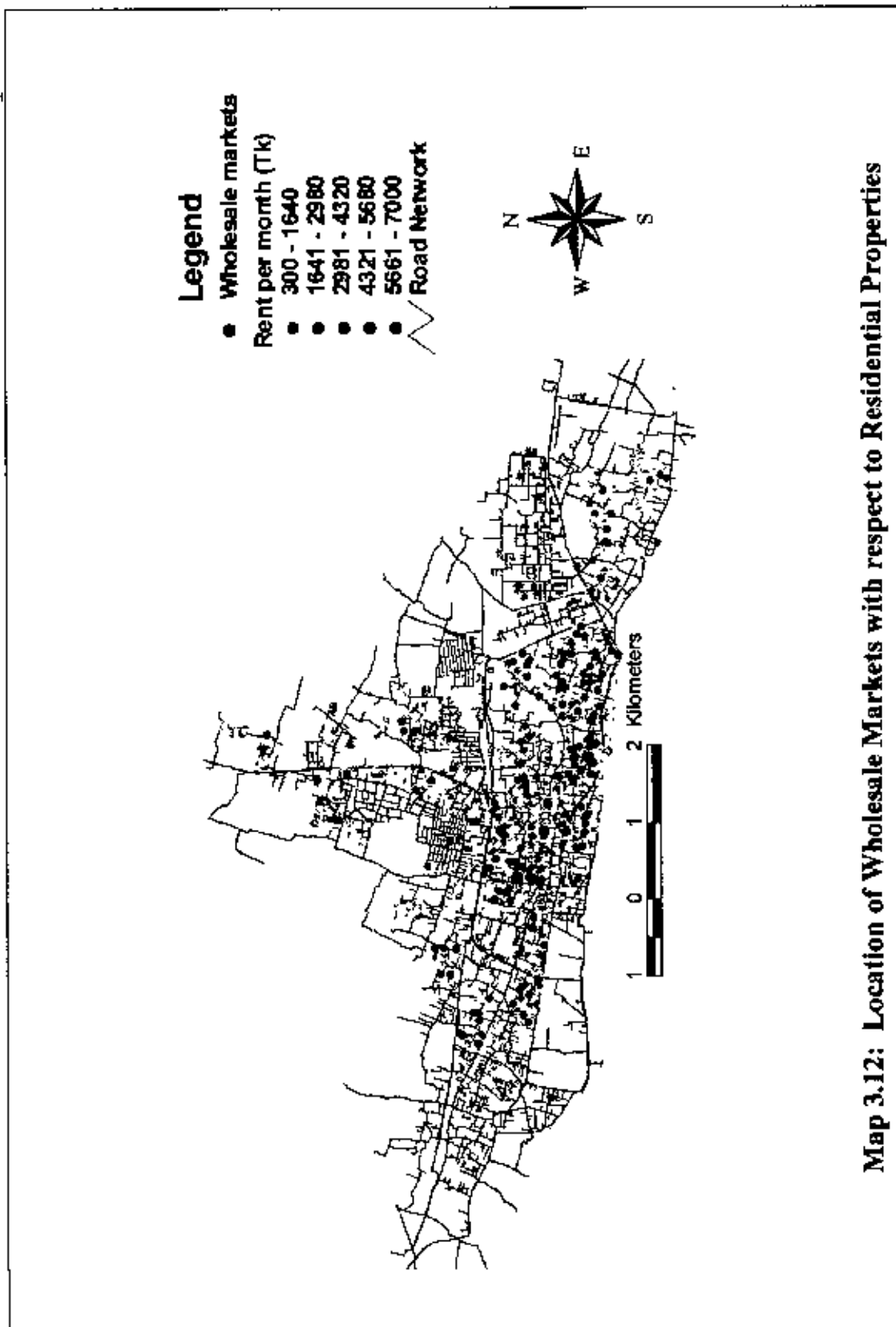
Map 3.8: Percentage Share of Residential Land Use by Ward and Residential Properties

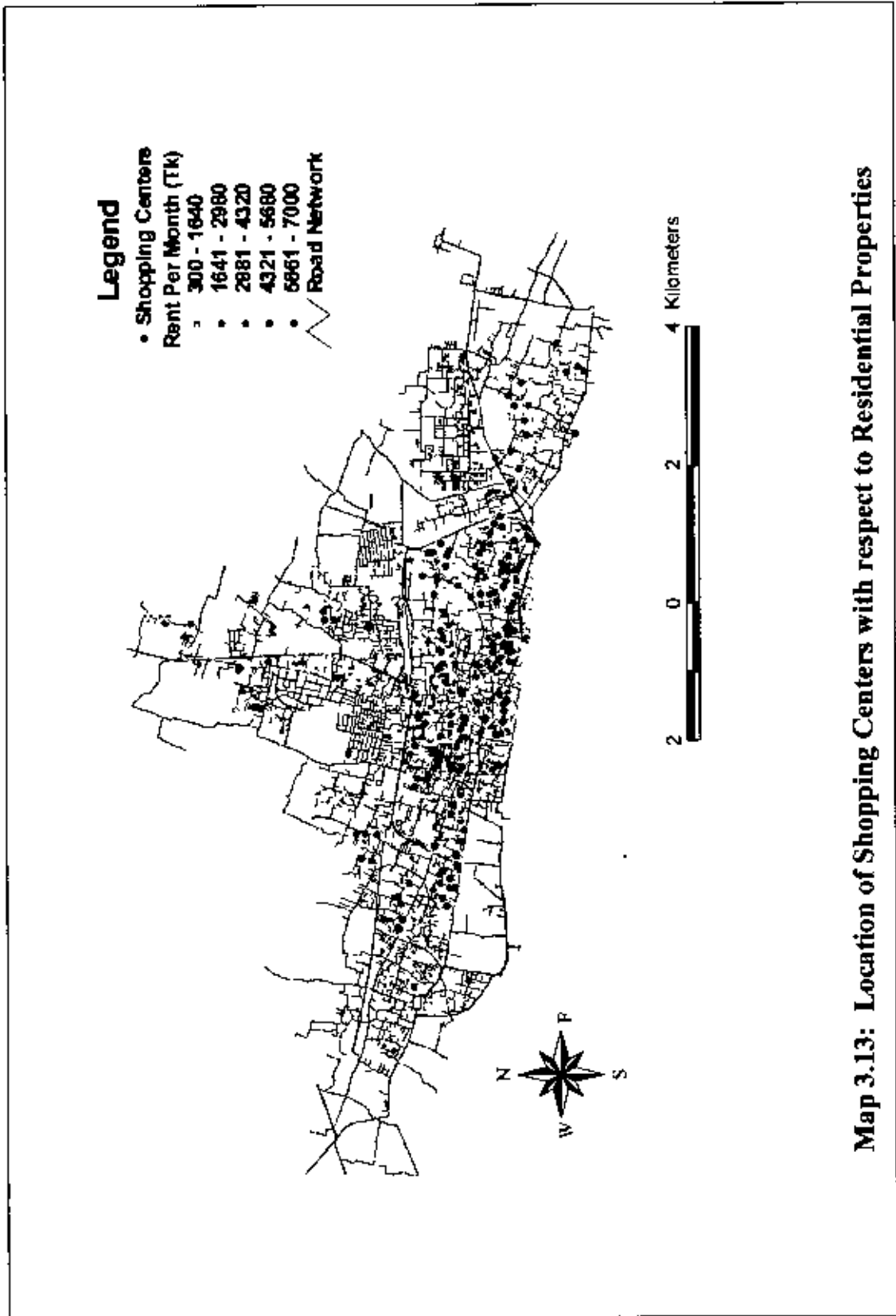


Map 3.9: Percentage Share of Community Facilities by Ward and Residential Properties

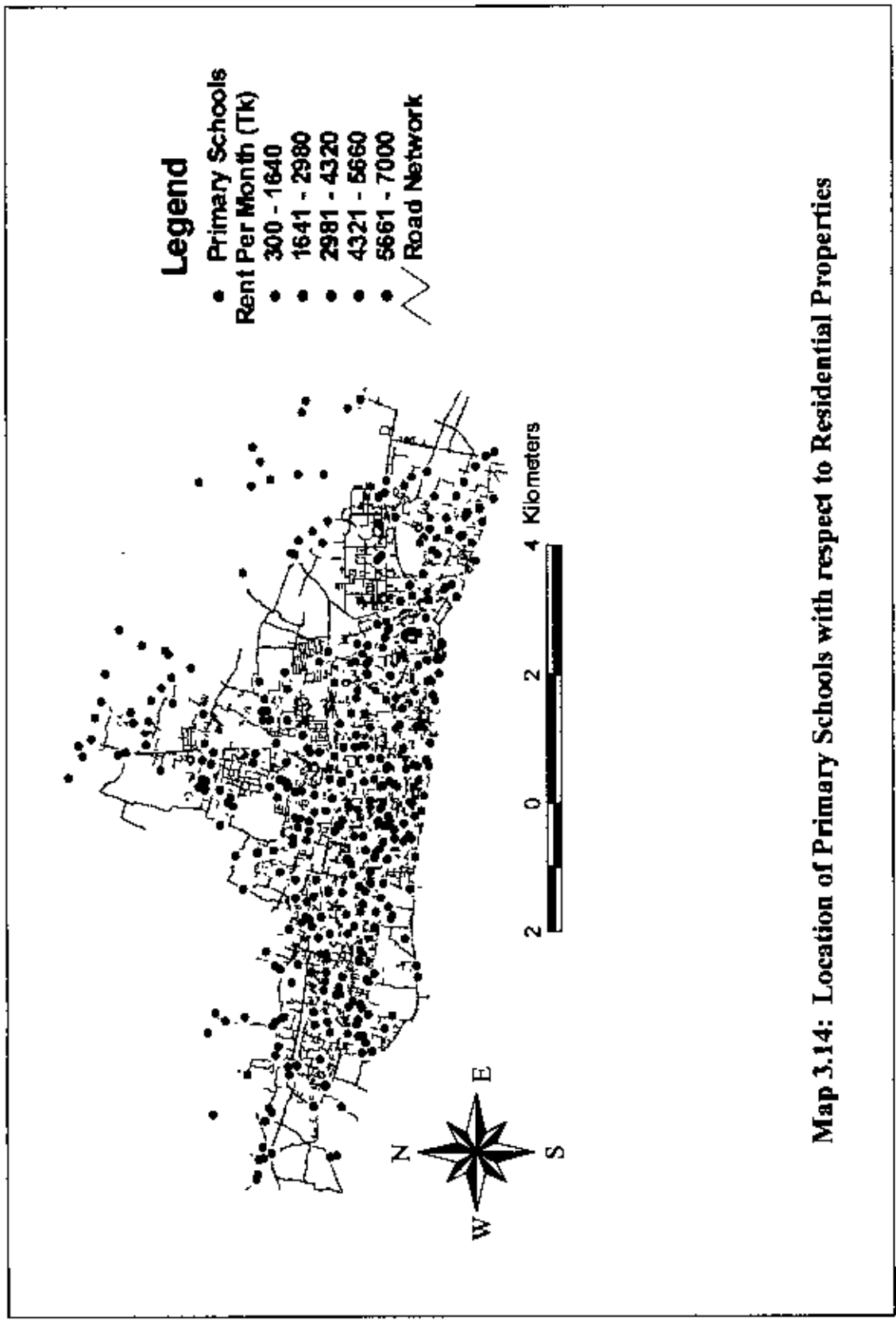




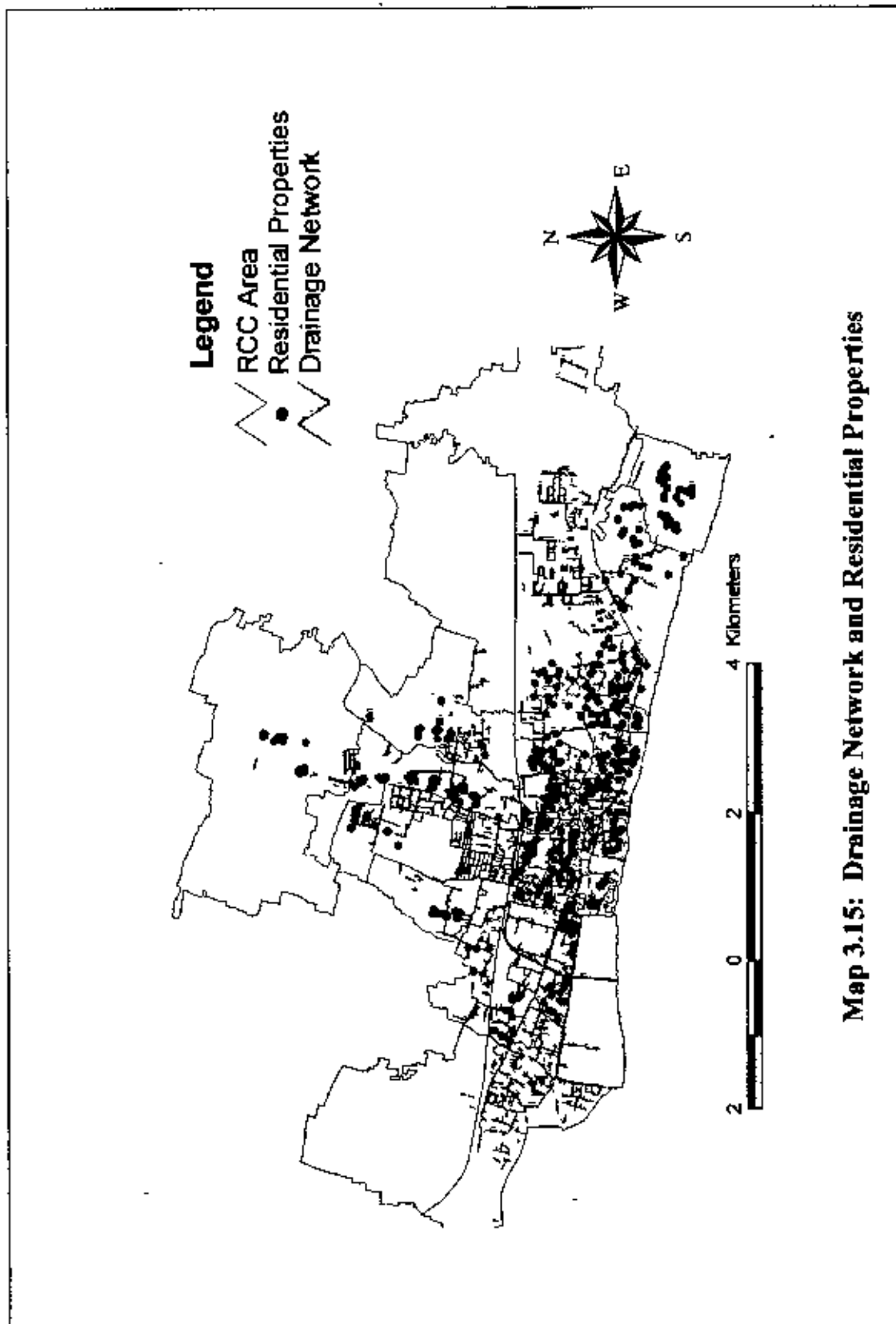




Map 3.13: Location of Shopping Centers with respect to Residential Properties



Map 3.14: Location of Primary Schools with respect to Residential Properties



Map 3.15: Drainage Network and Residential Properties

3.5 Summary

The chapter has given an overview of the data which was used to develop ANN model for house rent prediction of Rajshahi City. The data set used to develop the ANN model consists of a sample of 479 single family and multi-family residential properties available for rent. The ANN models in this study have been built using fourteen independent variables. Rajshahi City Corporation area had been selected as a study area of this study which is described in the following chapter.

Chapter 4
STUDY AREA

Chapter 4: Study Area

4.1 Location

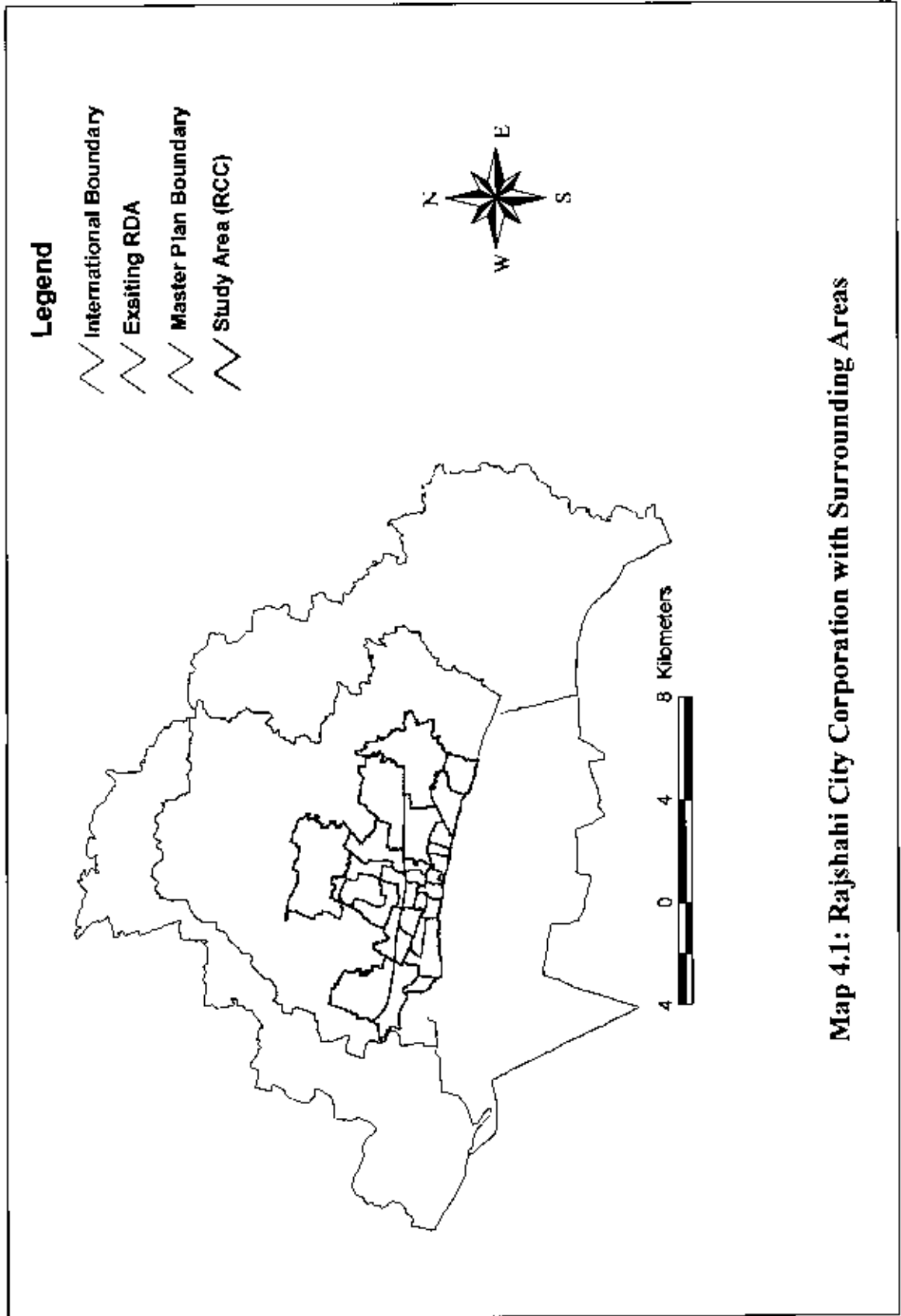
The study area selected for this research is Rajshahi City Corporation (RCC) area. The city is located along the river Padma, between latitude 24°18" N and 24°25" N and longitude 88°33" E and 88°41" E. The area comprises of 51.29 sq. km (19.72 sq. miles) of land with 3.83 lakh population. It is the fourth metropolitan city of the country. The location of the study area in relation to the surrounding areas and administrative units is shown in Map 4.1 and Map 4.2 respectively.

4.2 Historical Background

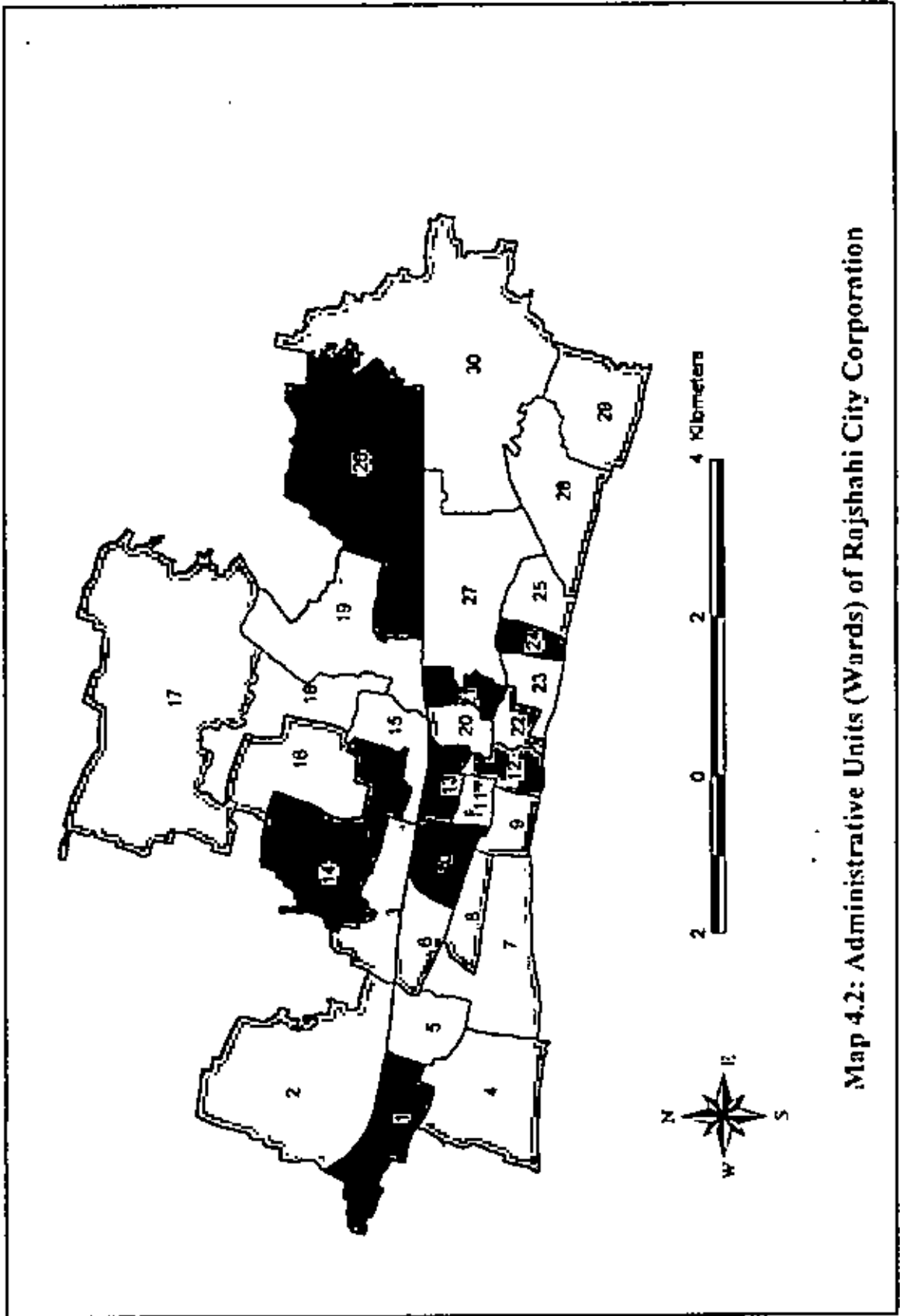
Rajshahi is a divisional city and an important city in the northern region of the country. It was simply a district town prior to 1947 that had become divisional headquarters in 1947. In 1886 during British reign the town gained municipal status and finally achieved the status of City Corporation in 1983. Over the years, it has grown as the administrative headquarters of the Rajshahi Division, and lately flourished as a center of learning. Now it is the 4th largest city in Bangladesh next to Dhaka, Chittagong and Khulna.

4.3 Climate

Rajshahi city has a sub-tropical monsoonal climate. Generally temperature is low in January and varies between 8.8° C to 25.9°C. From February temperature is found to increase up to June and thereafter declines slightly every month from July to August. From September temperature declines rapidly up to January. The people of Rajshahi generally feel the hot-wave during April to May. The mean relative humidity is found to low in March (60.2%) and it is high in August-September (88.4%). High wind speed is observed during April to June. About 77 percent rainfall occurs during June-September and rest 23 percent in the other 8 months.



Map 4.1: Rajshahi City Corporation with Surrounding Areas



Map 4.2: Administrative Units (Wards) of Rajshahi City Corporation

4.4 Land Use Pattern

In the Rajshahi City Corporation area, over 18% land is still being used for agricultural purpose, while about 11% land remains vacant and about 3.52% land belong to char area. Residential use covers about 32%, while road infrastructure covers only 4% of total land.

Water bodies encompass 13.35% that include the Padma River and a large number of ponds. Different educational institutions including Rajshahi Univeristy, Rajshahi University of Engineering and Technology and Rajshahi Medical College encompass about 9% of total area. Industry and commercial land uses together comprise only 4.15% of the RCC land representing the very low profile of economic activities in the City (DDC, 2004).

4.5 Urbanization and Demography

The rate of urbanization and population growth is very low in Rajshahi city compared to other major cities of the country. The population density of the RCC area is only 7,073 persons per sq. km (DDC Limited, 2004).

Presently, the city has a population of 3.83 lakh, which was 2.94 lakh during 1991. In the period of 1981-1991, the population has increased at a rate of 63.36 percent, about 1.14 lakh. However, during 1991-2001, it has increased only 0.88 lakh, accounting for a 30.25 percent rise (DDC Limited, 2004).

The urbanization rate of the northern region (i.e. Rajshahi Division) remained the same throughout the last decade, which was 17.3 percent. The country's annual growth rate of population in the period 1991-2001 was the lowest in Rajshahi SMA (1.87 percent) and fastest in Dhaka SMA (4.26 percent). Every year the capital city Dhaka absorbs an additional population equivalent to the current population of RCC area (DDC Limited, 2004).

4.6 Economy and Employment

Rajshahi presents a case of quasi-urbanization. Its inadequate development of infrastructure facilities, shortage of capital and absence of entrepreneurs are constraints to development of economic base of the city. Its hinterland is predominantly agrarian in character (DDC Limited, 2004).

A few major scattered industries, public sector organizations, academic institutions, informal sector and trade and commerce provide major base for economic activities in the study area. Four growth centers and 12 major hats/bazaars in and around study area exert profound impact on the study area. Informal sector accounts for 19% of total employment in the study area whereas Trade and commerce provides employment for 33.47% of labour force. Other important sectors of employment are Administration and Service (22.37%), farm activities (10.12%) and Non-farm wage labour (13.38%).

Majority of households (61%) of the study area belong to monthly income group of 2,500-6,500 and savings by households are comparatively low in the study area. Labour force in the study area will increase from 299.89 thousand in 2001 to 385.67 thousand in 2021. About 27% of labour force will not find job, if current development trends continue (DDC Limited, 2004).

The city of Rajshahi acts as major employment centre for rural poor and destitutes migrating from its hinterlands. The city provides the base and facilities for industrial and manufacturing activities at a moderate level, and generates various kinds of services in both public and private sectors. It is modal point for transport network and transshipment activities for the adjoining regions and with other parts of the country.

4.7 Transportation

The city of Rajshahi had only a modest growth during the last two decades. In the national context, Rajshahi is well connected with rest of the country by both road and rail. The broad gauge railway line from Rohanpur to Ishurdi, with a link to Chapai-Nowabganj passes through the heart of Rajshahi city and forms part of the main broad gauge system in the country. With the opening of Nalka-Hati Kamrul-Bonpara road, Dhaka is only 5 hours away from the study area. The situation has further improved with the completion of the approach road to Jamuna Bridge through Tangail.

The traffic study conducted in 2002 indicated that none of the major roads in the study area has had any capacity constraints in terms of peak hour flow viz-z-viz design capacity. An Origin-Destination (O-D) survey indicated that 73 to 74% of all incoming and outgoing traffic had the destination or origin within the study area.

In the study area 55% OF daily trips are made by rickshaws/vans and cycles, while another 29% are made on foot. Most the trips (69%) of the study area are related to either home or work, leaving another 15% which are made to schools/college and universities.

4.8 Housing Situation

In the study area most of the housing units (over 90%) come from informal private sources. The NGOs usually operate in low-income communities in rural areas providing finance and services only.

About 44 percent of the households become landowners through inheritance, while over 44% became owners by way of purchase. Land value in the Rajshahi City is very low compared with Dhaka and Khulna. In spontaneous housing areas of the main city land sells between Tk. 90 thousands to Tk. 120 thousands per katha. Land

value in planned areas varies between Tk. 100 thousands to Tk.120 thousands per katha. In the study area there is a housing backlog of 1553 units (1991).

4.9 Market and Shopping Facilities

There are 8 daily bazars in Rajshahi city to serve its 3 lakh 83 thousand population (2001). However, the bazars are not evenly distributed over the city to serve all its inhabitants efficiently. Besides daily markets, the city has a few shopping centers like New Market and Shahab Bazar. There are also some wholesale markets namely Shahab Bazar, Kadirganj Bazar and Rani Bazar etc. in the study area.

4.10 Recreational Facilities

With easy access to satellite TV channels served by cable operators, cinema has lost its attraction in the study area. In Rajshahi City, presently there exist seven cinema halls. Satellite TV channels are possibly most popular and the cheapest means of indoor recreation. The upper income groups of society enjoy their leisure time in clubs. There are a number of clubs in the city. But most of them are for professional people, like Police Club, Jilkahana club, University Club, Doctors' club. There are very few parks and playgrounds in Rajshahi City. There are only three parks which is very inadequate for the city. Estimation shows that RCC area has only 0.41 acres of open space per thousand populations which is very low compared to other major cities (DDC Limited, 2004).

4.11 Postal Facilities

There are 17 post offices within the RCC area. About 30% of these were established during the period of 80s. However, the existing post offices are not well distributed over the city. Among 30 RCC wards only 15 have Post offices. There are 74 post boxes placed at different important locations of the city for collection of letters.

4.12 Municipal Services

4.12.1 Water supply

There are 785 community water stand posts and 85 on-street *dhop* water stands in the city. There are also 3,750 hand tube wells for drinking water supply. The city has eight overhead tanks and three water treatment plants. Ground water is extracted by 45 production tube wells. Till 1995 there were 182 km of water pipelines in the city.

4.12.2 Solid waste management

The city dwellers generate about 200 m. tons of solid waste daily. RCC collects about 142 m. tons of solid waste, the rest littered around. RCC has 17 motorized and 126 non-motorized transports to carry solid waste with 934 staff of different categories engaged in solid waste collection and disposal. Presently there is only one dumping site for the city's solid waste located at Bonogram, Nawdapara. The number of dustbins available is inadequate for the city. RCC does not collect waste from households.

4.12.3 Sanitation and public toilet

According to RCC sources, about 50 percent of the RCC area households have sanitary latrine facilities, of them 30% have latrine with soak pit and 20% have latrines without soak pit. There are about 43 public toilets in the city at important public locations.

4.13 Summary

This chapter carries out brief description of the study area. Rajshahi City Corporation (RCC) area was selected as a study area for this research. Rajshahi is a divisional city and it is the fourth metropolitan city of the country. Residential use covers highest percentage of land of the study area followed by agricultural land use. The rate of urbanization and population growth is comparatively lower in Rajshahi City. The ANN model was developed using the variable data collected from the study area. The development procedure of ANN model and result of the model is discussed in the following chapter.

Chapter 5

DETERMINATION OF ARTIFICIAL NEURAL NETWORK MODEL

Chapter 5: Determination of Artificial Neural Network Model

5.1 Introduction

To address the issue of application of Artificial Neural Network (ANN) in house rent prediction, this chapter illustrates the development procedure of ANN model for house rent prediction of Rajshahi City and discusses the results of the developed model. This chapter attempts to identify some of the independent variables which influence the house rent of Rajshahi City based on the relative influence factor of different attributes. The chapter will also focus on the analysis of elasticity.

5.2 Development of Artificial Neural Network Model

For developing the artificial neural network (ANN) model the relevant data set was separated into two separate subsets namely the "training set" and the "production set". The training set was used to train the neural network model and the production set was used to test the model's performance. The data set used to develop the Neural Network Model consists of a sample of 479 single family and multi-family residential properties available for rent in Rajshahi City. The two samples were created by first sorting the houses by location, then by rent and then by picking every fourth house for the production set. The developed model was trained with 360 residential properties (training set) and their predictability in estimating value was tested with the remaining 119 residential properties (production set). The neural network model built for this data set utilized the following fourteen independent variables: usable living area (FL_SPACE), number of bedrooms (BEDS), number of bathrooms (BATHS), age of residential property structure (BLD_AGE), population density (POP_DENS), percentage of area dedicated to residential use (RES_LUSE), percentage of area dedicated to commercial use (COM_LUSE), percentage of area dedicated to community facilities (COMMU_LU), Euclidian distance from the property to nearest point of drainage network (DRAINAGE), network access distance from property to major roads (M_RD_ACC), network access distance from property to central business district (CBD)(CBD_ACC), network access distance from property to wholesale markets (W_MAR_AC), network access distance from

property to primary school (EDU_ACC), network access distance from property to shopping centers (SHOP_ACC). Table 5.1 details the descriptive statistics of the entire sample and the two subsets for training and testing. From Table 5.1 it can be seen that there were no significant differences between the training and testing data subsets and each is a fair representation of the entire data set.

Table 5.1 Descriptive statistics of entire sample, training set and testing set

| Variables | Mean | | | Maximum | | | Minimum | | |
|-----------|---------------------|--------------------|-------------------|---------------|--------------|-------------|---------------|--------------|-------------|
| | Entire Sample (479) | Training Set (360) | Testing Set (119) | Entire Sample | Training Set | Testing Set | Entire Sample | Training Set | Testing Set |
| RENT | 1961.9 | 1936.2 | 2039.5 | 7000.0 | 7000.0 | 6000.0 | 300.0 | 300.0 | 300.0 |
| FL_SPACE | 1532.0 | 1509.3 | 1600.6 | 8000.0 | 7000.0 | 8000.0 | 200.0 | 200.0 | 300.0 |
| BEDS | 2.6 | 2.6 | 2.7 | 4.0 | 4.0 | 4.0 | 1.0 | 1.0 | 1.0 |
| BATHS | 1.5 | 1.5 | 1.5 | 3.0 | 3.0 | 3.0 | 0.0 | 0.0 | 1.0 |
| BLD_AGE | 18.6 | 18.9 | 17.7 | 129.0 | 129.0 | 94.0 | 1.0 | 1.0 | 2.0 |
| POP_DENS | 64.6 | 64.7 | 64.5 | 161.7 | 161.7 | 161.7 | 7.4 | 7.4 | 7.4 |
| RES_LUSE | 41.2 | 41.2 | 41.2 | 45.4 | 45.4 | 45.4 | 27.0 | 27.0 | 27.0 |
| COM_LUSE | 6.0 | 6.0 | 5.9 | 8.6 | 8.6 | 8.6 | 1.4 | 1.4 | 1.4 |
| COMMU_LU | 3.1 | 3.1 | 3.1 | 5.3 | 5.3 | 5.3 | 0.2 | 0.2 | 0.2 |
| DRAINAGE | 62.7 | 61.8 | 65.4 | 760.1 | 733.9 | 760.1 | 1.3 | 1.3 | 2.5 |
| M_RD_ACC | 920.0 | 926.6 | 899.8 | 2871.5 | 2871.5 | 2663.7 | 48.8 | 48.8 | 175.0 |
| CBD_ACC | 2302.3 | 2305.5 | 2292.5 | 5603.6 | 5603.6 | 5503.3 | 207.5 | 278.8 | 207.5 |
| W_MAR_AC | 1927.0 | 1933.0 | 1908.7 | 5603.4 | 5603.4 | 5395.7 | 82.1 | 82.1 | 183.4 |
| EDU_ACC | 919.3 | 923.1 | 907.8 | 17775.6 | 17775.6 | 2613.5 | 3.1 | 3.1 | 21.7 |
| SHOP_ACC | 1771.1 | 1782.7 | 1735.9 | 5691.1 | 5691.1 | 5483.3 | 88.3 | 88.3 | 114.6 |

5.2.1 Initial model

To develop the neural network model a back-propagation neural network software package, *NeuroShell* (Ward Systems Group, Inc), was used. The neural network results that are reported in this study are the “best” results that were obtained after many different trials. The “best” results were defined as:

- 1) The model that predicted the highest percentage of houses with average absolute errors below 5%

- 2) The model that possesses the lowest percentage of mean absolute error and
- 3) The model that had the highest value the network performance statistic which is better known as R^2 or the coefficient of multiple determinations.

The R^2 is the same statistical indicator which is usually applied to multiple regression analysis. It compares the accuracy of the model to the accuracy of a trivial benchmark model wherein the prediction is just the average of all of the example output values. This R^2 value is also used in the later chapter for comparing the prediction performance of ANN model and hedonic price model.

The problem was to determine the optimal number of hidden layers and the optimal number of nodes to use in each hidden layer for developing the "best" neural network model. The only method available to do this is through trial and error (Worzala et al, 1995). Therefore, in this study a trial and error process was applied to find the optimal artificial neural network model. In this process, seventeen hidden neurons were found to be the optimal number of neurons within the hidden layer for the best ANN model. Table 5.2 details the results of the seven ANN models created during this procedure. The network model created with 17 hidden neurons exhibited superiority in all three performance criteria.

Table 5.2: Alternative ANN models varying the number of hidden neurons

| Model | Number of hidden neurons | R^2 | Percentage mean absolute error | Percentage of houses < 5% absolute error |
|----------------|--------------------------|--------|--------------------------------|--|
| 1 ^a | 17 | 0.5967 | 24.6 | 13.45 |
| 2 | 25 | 0.5593 | 25.1 | 12.6 |
| 3 | 35 | 0.5589 | 25.1 | 12.6 |
| 4 | 43 | 0.5591 | 25.1 | 11.76 |
| 5 | 53 | 0.5575 | 25.1 | 13.45 |
| 6 | 65 | 0.5588 | 25.1 | 13.45 |
| 7 | 78 | 0.5563 | 24.9 | 12.6 |

Note: ^a Indicates the best results

Figure 5.1 shows the neural network structure of the house rent prediction model. The result of the model is shown in Figure 5.2 and Figure 5.3 shows the actual and predicted rent for 119 test properties.

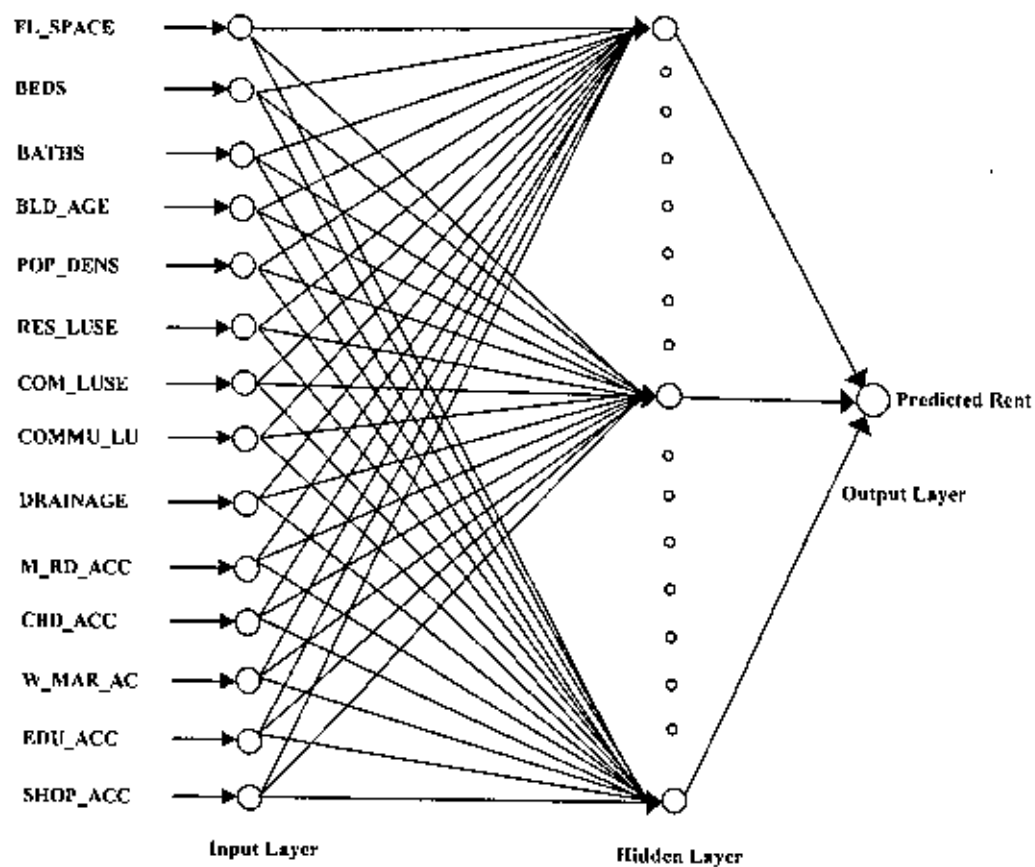


Figure 5.1: Neural Network Structure of House Rent Prediction Model

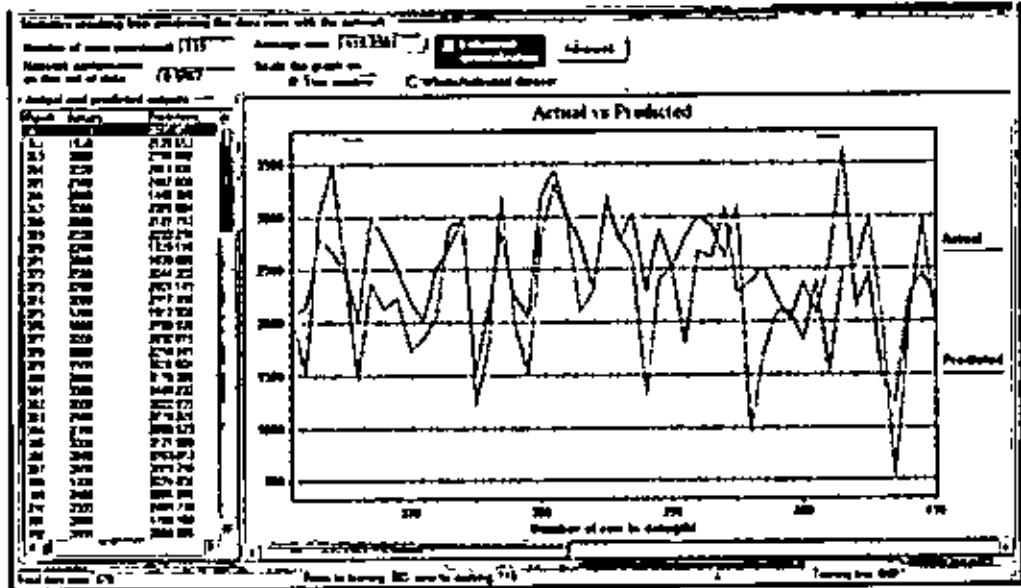


Figure 5.2: Initial neural network model

From Figure 5.2 it is seen that the network performance statistic is better known as R^2 or the coefficient of multiple determinations value of this model was 0.5967. From Figure 5.3 it can be observed that the lines of actual and predicted values are fairly close. The model had a mean absolute error of 24.6% and it predicted 13.45% residential property with average absolute error below 5%.

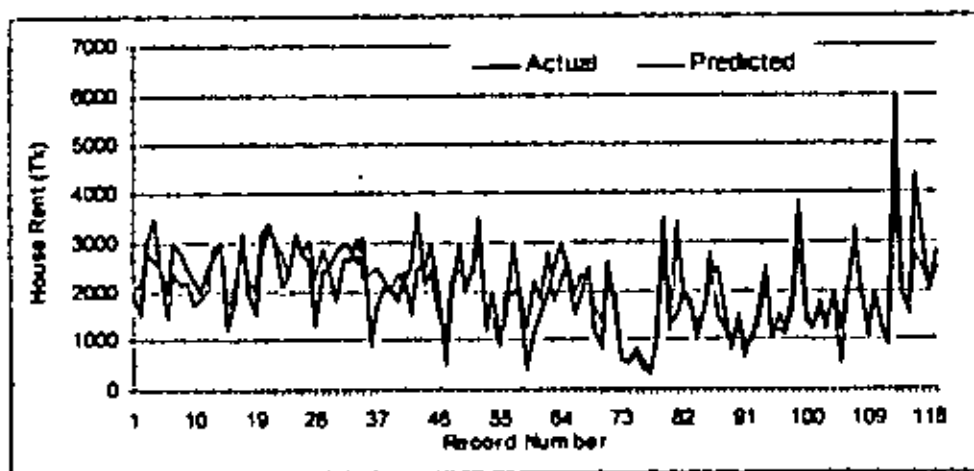


Figure 5.3: Actual and predicted house rent of test sample.

5.2.1.1 Relative Importance of Inputs

The importance of input values are a relative measure of how significant each of the inputs is in the predictive model whose weights range from 0 to 1. Higher values are

associated with more important variables (inputs). The relative contribution factors of different inputs for the initial neural network model (the relative importance of inputs) are given in Table 5.3.

Table 5.3: Relative importance value of inputs

| Variable | Relative Importance value |
|----------|---------------------------|
| CBD_ACC | 0.387 |
| COM_LUSE | 0.155 |
| RES_LUSE | 0.119 |
| COMMU_LU | 0.061 |
| FL_SPACE | 0.055 |
| DRAINAGE | 0.051 |
| POP_DENS | 0.043 |
| BATHS | 0.036 |
| SHOP_ACC | 0.028 |
| BEDS | 0.027 |
| EDU_ACC | 0.019 |
| W_MAR_AC | 0.009 |
| M_RD_ACC | 0.007 |
| BLD_AGE | 0.003 |

The relative contribution factor shows that network access distance from property to central business district (CBD_ACC), percentage of area dedicated to commercial use (COM_LUSE), percentage of area dedicated to residential use (RES_LUSE) are important factors that determine the residential property rent of Rajshahi City whereas network access distance from property to major roads and age of the residential property structure are the less important factors (Figure 5.4). Community facilities has a relatively high impact on house rent compared to usable living area, population density, number of bathrooms, number of bedrooms and amenities around the house area. The result indicates that neighborhood attributes play an important role in house rent determination in Rajshahi City.

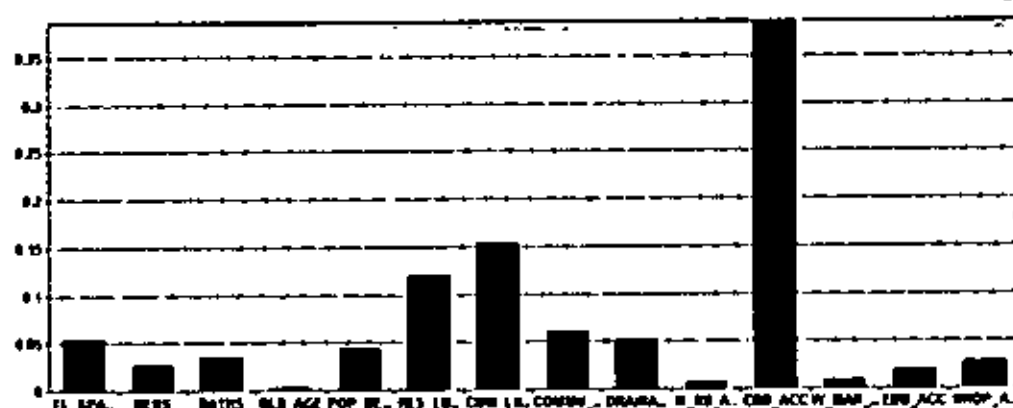


Figure 5.4: Relative Importance of Inputs

5.2.2 Best neural network model

To develop a better neural network model it was decided to eliminate the inputs with low contribution from the model. To do this all the variables with a relative importance value below 0.02 were removed from the model. From the initial model four variables (EDU_ACC, W_MAR_AC, M_RD_ACC, and BLD_AGE) were removed. With the rest of the ten variables the model was trained again. The same trial and error method was used to obtain the best results. Table 5.4 details the results of the seven ANN models created during this procedure. The network model created with 80 hidden neurons exhibited superiority in all three performance criteria.

Table 5.4: Alternative ANN models varying the number of hidden neurons

| Model | Number of hidden neurons | R^2 | Percentage mean absolute error | Percentage of houses < 5% absolute error |
|----------------|--------------------------|--------|--------------------------------|--|
| 1 ^a | 80 | 0.621 | 22.52 | 14.28 |
| 2 | 54 | 0.4953 | 26.12 | 11.76 |
| 3 | 14 | 0.6183 | 25.15 | 12.61 |
| 4 | 43 | 0.5649 | 25.09 | 12.61 |
| 5 | 65 | 0.6065 | 23.98 | 13.45 |
| 6 | 31 | 0.563 | 25.12 | 14.29 |
| 7 | 26 | 0.5632 | 25.12 | 14.29 |

Note: ^a Indicates the best results

The predicting result of new developed model is given in Figure 5.5 and Figure 5.6 shows the actual and predicted house rent for 119 test properties for two ANN models (The data used for Figure 5.6 have been sorted in ascending actual property value). The R^2 value of the new model is 62.10% which is higher than the initial model (59.67%). So the new model can predict the house rent more accurately than the previous one. Table 5.5 illustrates the results of two models. Second neural network model had a mean absolute error of 22.52% while the initial model had 24.61% which would indicate that the second model was a better model for predicting house rent. The maximum absolute error test showed that the second model outperformed the initial model (157.55% compared to 214.23%). Moreover, Figure 5.5 gives the evidence of improvement in accuracy using the new model over the initial model.

Table 5.5: Comparison of predictive power of two ANN models

| Model | Mean Absolute Error (%) | Maximum Absolute Error (%) | Error below 5% (%) | R^2 |
|---------------------------|-------------------------|----------------------------|--------------------|--------|
| Neural Network Model | 24.61 | 214.23 | 13.45 | 0.5967 |
| Best Neural Network Model | 22.52 | 157.55 | 14.28 | 0.6210 |

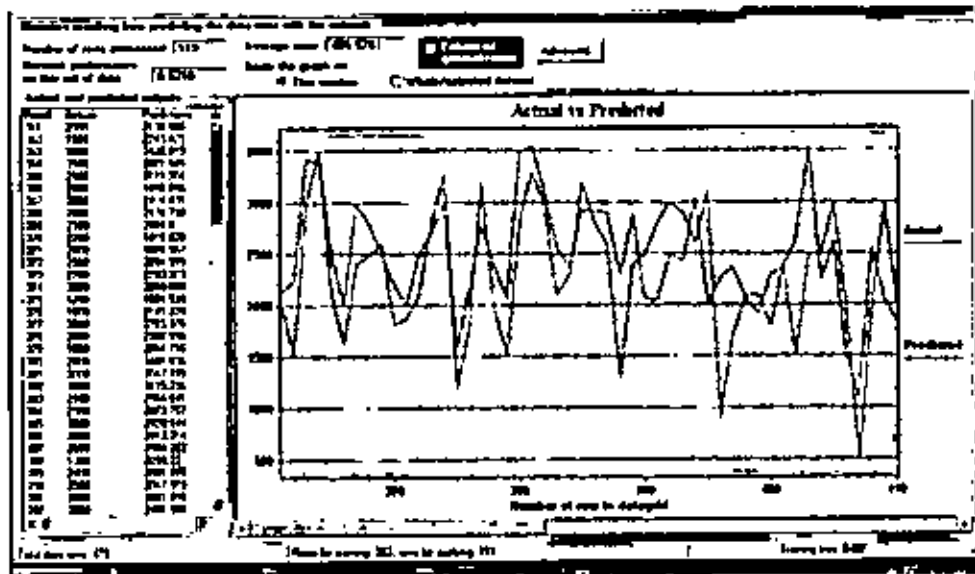


Figure 5.5: Best ANN model

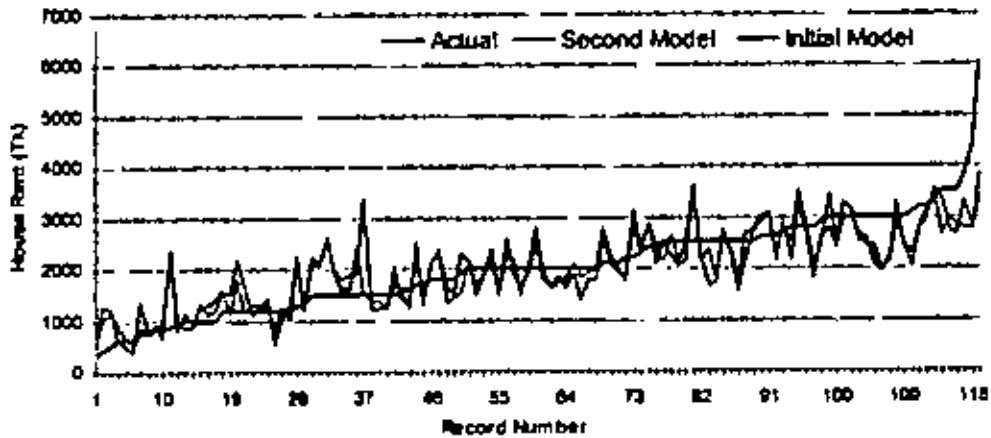


Figure 5.6: Actual and Predicted house rent

5.2.2.1 Relative Importance of Inputs

In the second model the relative importance of inputs has been changed from the initial neural network model. From Figure 5.7, it can be seen that percentage of area dedicated to community facilities and percentage of area dedicated to commercial use became important factors in determining house rent in Rajshahi city whereas usable living area had very little importance. In both models it is seen that land use plays a very important role in determining house rent in Rajshahi City.

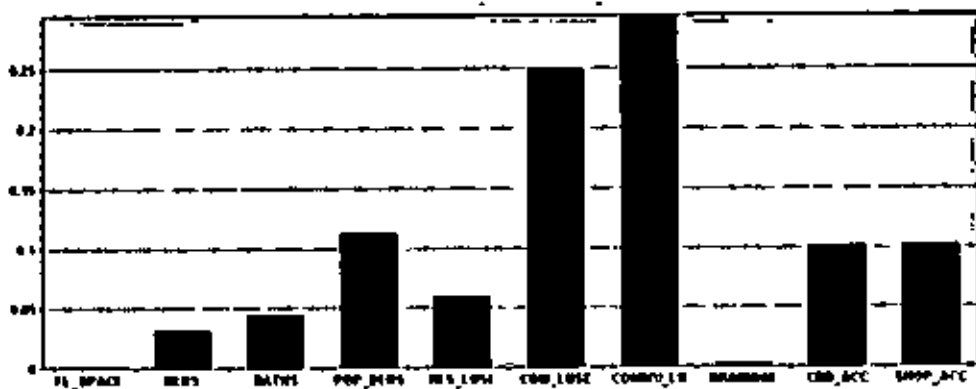


Figure 5.7: Relative importance of inputs in best ANN model

5.3 Elasticity Estimation

Elasticity is the percentage change of house rent with the changes of independent variables. Elasticity of house rent with respect to different independent variables has been discussed below.

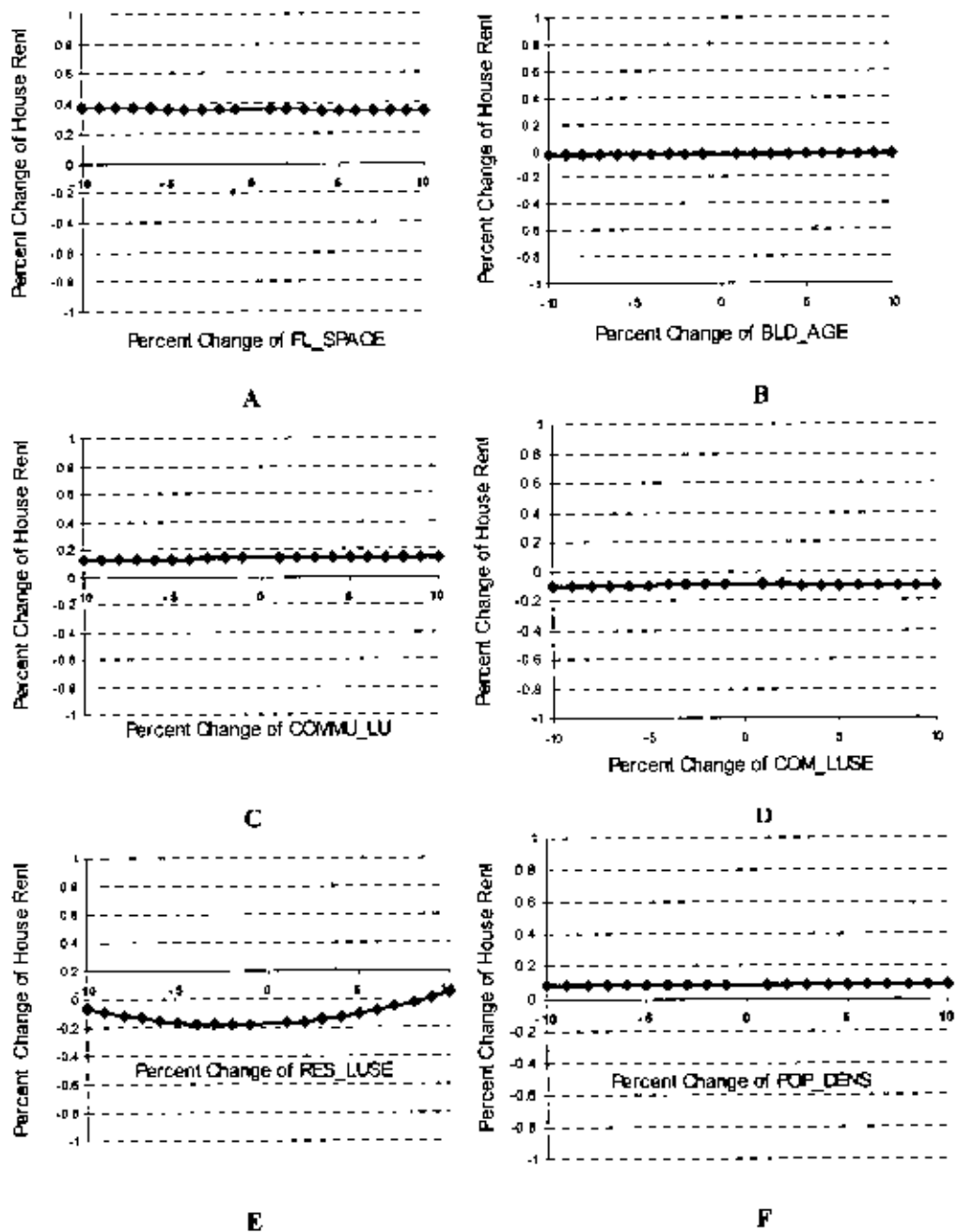


Figure 5.8: House rent elasticity with respect to different independent variables

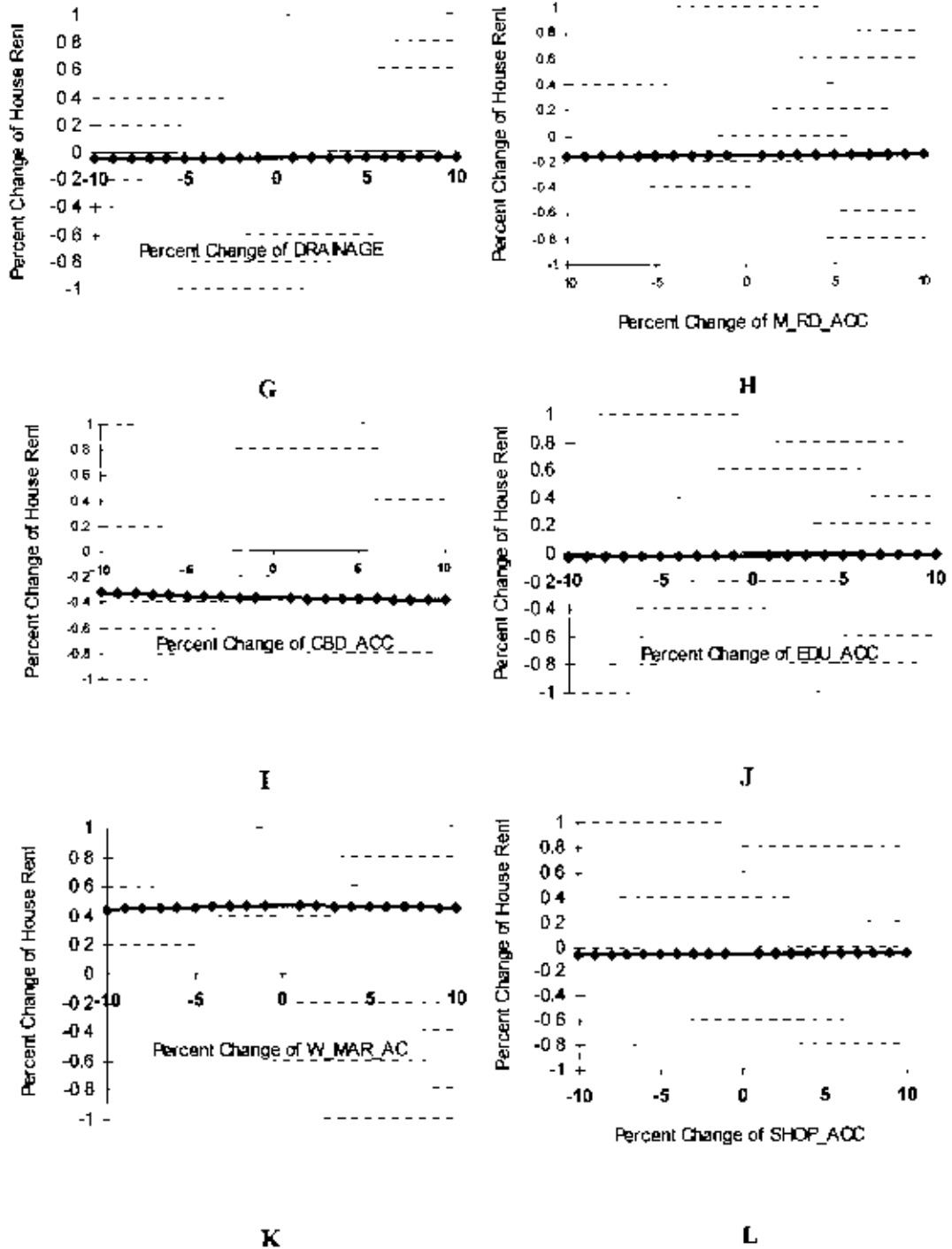


Figure 5.8: House rent elasticity with respect to different independent variables

Fourteen independent variables had been used in this study to determine house rent. But for these analysis two independent variables namely number of bedrooms and number of bathrooms were not considered because they are discrete type variables. Elasticity of house rent was estimated with respect to the rest of the twelve independent variables using ANN model. The ANN model was first trained with 369 residential properties and then tested with a hypothetical cases consisting of average values of thirteen out of fourteen independent variables with the value of the remaining independent variable varying from 10% below average to 10% above average in 1% increment. Figure 5.8 shows the percent change of house rent at different points with respect to different independent variables.

Table 5.6: Summary of house rent elasticity estimation

| Independent Variables | Percent Increase of Independent Variables from Average Value | Percent Change of House Rent |
|-----------------------|--|------------------------------|
| FL SPACE | 1% | 0.35 % |
| BEDS | 1% | 0.29 % |
| BATHS | 1% | 0.24 % |
| BLD AGE | 1% | -0.03 % |
| POP DENS | 1% | 0.09 % |
| RES LUSE | 1% | -0.17 % |
| COM LUSE | 1% | -0.10 % |
| COMMU LU | 1% | 0.13 % |
| DRAINAGE | 1% | -0.05 % |
| M RD ACC | 1% | -0.16 % |
| CBD ACC | 1% | -0.37 % |
| W MAR AC | 1% | 0.46 % |
| EDU ACC | 1% | -0.03 % |
| SHOP ACC | 1% | -0.06 % |

Table 5.6 shows the summary of house rent elasticity estimation. Table 5.6 illustrates that with 1% change of the value of different independent variables the house rent changes by -0.03% to 0.46%. The maximum 0.46% change of house rent occurred due to 1% change of the value of network access distance from property to wholesale markets. It is also found that an increase of network access distance from property to CBD by 1% will result in a decrease of house rent by 0.37%. On the other hand, house rent was changed by only 0.03% due to 1% value increase of BLD_AGE,

EDU_ACC. Since the changes of house rent due to the changes of independent variables are not very significant, it can be said that the developed ANN model is a robust model.

5.4 Summary

The developed ANN model was trained with 360 residential properties (training set) and their predictability in estimating value was tested with the remaining 119 residential properties (production set). The neural network model built for this data set utilized fourteen independent variables. The initial ANN model created with 17 hidden neurons exhibited superiority with a R^2 value of 0.5967. The initial model had a mean absolute error of 24.6% and it predicted 13.45% residential property with average absolute error below 5%. On the other hand the best neural network model was developed utilizing ten independent variables with 80 hidden neurons. The R^2 value of the best model was 0.6210 with a mean absolute error of 22.52%. The relative contribution factor of the initial ANN model shows that network access distance from property to central business district (CBD_ACC), percentage of area dedicated to commercial use (COM_LUSE), percentage of area dedicated to residential use (RES_LUSE) are important factors that determine the residential property rent of Rajshahi City. In both models it is seen that land use plays a very important role in determining house rent in Rajshahi City. After elasticity estimation it is seen that with 1% change of the value of different independent variables the house rent changes by -0.03% to 0.46%. On the basis of the result of this developed model, the comparative analysis of the predictive power of ANN model and hedonic price model are presented in the following chapter.

Chapter 6

NEURAL NETWORK MODEL VS HEDONIC PRICE MODEL

Chapter 6: Neural Network Model Vs Hedonic Price Model

6.1 Introduction

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One of the main objectives of this study is to compare the predictive performance of a neural network model and a hedonic price model in the context of house rent. This chapter presents the comparative analysis of both models. Three criteria were used for comparing the performance of the two models: (1) the mean absolute error between the predicted and actual house rent, (2) the percentage of houses in the sample whose absolute error was less than 5% of the actual rent and (3) the coefficient of determination R^2 . The best model for predicting actual house rent was determined to be the one that resulted in the lowest mean absolute percentage error, higher R^2 and/or the highest percentage of predicted rent with absolute errors below 5% of the actual house rent. The comparison was conducted in six stages or cases. The first case conducted the predictive power comparisons utilizing the whole data set for training and testing. In the second case the models were trained with 360 houses and their predictability in estimating value were tested with remaining 119 houses. In the third case, the ANN model is compared with the best reduced hedonic price model and the fourth case classified the data set into three house rent range. The fifth case restricted the data set to include a more homogeneous set of houses from a single strategic planning zone area. Finally in the sixth case the tests were conducted both for a normal sample of properties as well as an outlier sample of properties. The best neural network models developed for all the cases were determined utilizing a sequential trial and error method. The best model was selected based upon the minimum mean absolute error prediction error and the maximum percentage of houses within a 5 per cent absolute prediction error of the actual house rent.

6.2 Case 1

The both models in this analysis were trained with 479 houses and their predictability in estimating value was tested with the same number of houses. All of the models built for this case utilized all fourteen variables which were used to develop the

initial neural network model. The hedonic price model was generated using the linear functional form specification. The coefficients and model summary are presented in Table 6.1. The coefficient of determination R^2 is 0.552.

Table 6.1: Coefficients and model summary of linear OLS hedonic model

| Variables | Unstandardized Coefficients | | Standardized Coefficients | t Distribution | Sig. |
|------------|-----------------------------|------------|---------------------------|----------------|------|
| | B | Std. Error | Beta | | |
| (Constant) | -908.143 | 540.210 | | -1.681 | .093 |
| FL_SPACE | .298 | .038 | .284 | 7.802 | .000 |
| BEDS | 383.842 | 43.993 | .367 | 8.725 | .000 |
| BATHS | 163.865 | 60.967 | .111 | 2.688 | .007 |
| BLD_AGE | -1.578 | 2.166 | -.025 | -.728 | .467 |
| POP_DENS | 1.355 | 1.158 | .057 | 1.171 | .242 |
| RES_LUSE | 16.621 | 13.420 | .105 | 1.238 | .216 |
| COM_LUSE | 24.192 | 28.069 | .076 | .862 | .389 |
| COMMU_LU | 87.126 | 54.703 | .141 | 1.593 | .112 |
| DRAINAGE | -.257 | .390 | -.034 | -.660 | .509 |
| M_RD_ACC | -.392 | .079 | -.227 | -4.986 | .000 |
| CBD_ACC | .044 | .129 | .067 | .344 | .731 |
| W_MAR_AC | .154 | .133 | .226 | 1.160 | .247 |
| EDU_ACC | -.026 | .031 | -.027 | -.831 | .406 |
| SHOP_ACC | .000 | .079 | -.001 | -.005 | .996 |

Model Summary

| R | R Square | Adjusted R Square | Std. Error of the Estimate |
|------|----------|-------------------|----------------------------|
| .743 | .552 | .539 | 612.448 |

a. Predictors: (Constant), SHOP_ACC, EDU_ACC, BATHS, BLD_AGE, FL_SPACE, POP_DENS, BEDS, M_RD_ACC, COM_LUSE, DRAINAGE, RES_LUSE, COMMU_LUSE, CBD_ACC, W_MAR_AC

b. Dependent Variable: RENT

The generated neural network model for 479 houses is shown in Figure 6.1. The coefficient of determination R^2 of this ANN model is 0.7295.

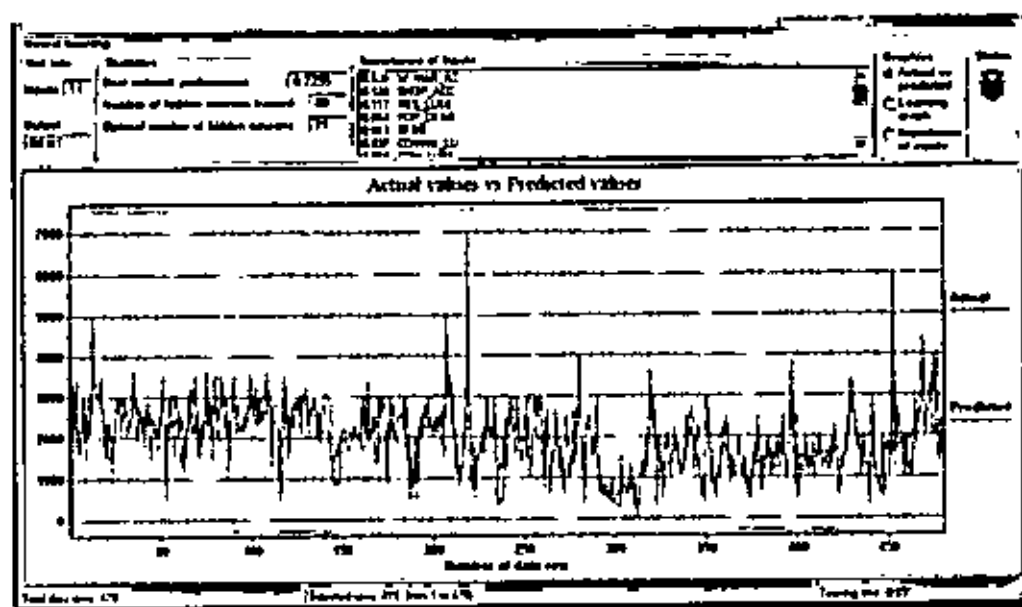


Figure 6.1: Neural Network model

Table 6.2 illustrates the prediction results of both models for case 1. From Table 5.7 it can be observed that the neural network model outperforms the hedonic price model in terms of all of the three criteria. The neural network model had a lower mean absolute error of 25.71% while hedonic price model had a mean absolute error of 29.97%. These findings indicate that in this case, the neural network models did outperform the hedonic price model.

Table 6.2: Prediction results of two models

| Absolute Error Range (%) | Neural Network Model | | Hedonic Price Model | |
|--------------------------|----------------------|--------------|---------------------|--------------|
| | % | No of Houses | % | No of Houses |
| 0-5 | 17.33 | 83 | 14.61 | 70 |
| 0-10 | 33.40 | 160 | 27.56 | 132 |
| 0-20 | 59.29 | 284 | 45.09 | 216 |
| >20 | 40.71 | 195 | 54.91 | 263 |
| Mean Absolute Error | 25.71 | 123 | 29.97 | 143 |
| R^2 | 0.7295 | | 0.552 | |

In terms of the percentage of predicted house rent within 5% of the actual rent, the neural network model also gave better result than hedonic price model. As detailed in Table 6.2, the neural network model predicted a higher number of houses with an absolute error below 5 % (17.33%) while hedonic price model predicted 14.61% of the houses within the 5% absolute error range. As the absolute error range is increased, neural network model outperforms the hedonic price model for the 0-10% range and the 0-20% range and the greater than 20% range of error. These results had the similarity with the Do and Grudnitski 1992) results which found that their neural network model had higher number of properties with less than 5% error than their hedonic price model.

The coefficient of determination R^2 value of neural network model (0.7295) is significantly higher than the R^2 value of hedonic price model (0.552). The results imply that the neural network model can estimate the house rent more accurately than the hedonic price model.

6.2.1 Relative contribution of inputs for both models

In the case of neural network model the relative contribution factor in Table 5.8 shows that network access distance from property to wholesale markets (W_MAR_AC) is the most important factor in determining the house rent where as in hedonic price model the number of bedrooms of the residential properties (BEDS) is the most influential predictor with a coefficient of 0.367(Table 6.1). In neural network model, network access distance from property to shopping centers (SHOP_ACC), another transportation attribute, is ranked second in terms of contribution (0.122) followed by a neighborhood attribute, RES_LUSE (0.117). On the other hand, usable living area is ranked second in terms of contribution (0.284) in hedonic price model which is followed by a transportation attribute W_MAR_AC. So W_MAR_AC was found important in both the models.

Table 6.3: Relative contribution of inputs in ANN model

| Variable | Relative Importance value |
|----------|---------------------------|
| W_MAR_AC | 0.53 |
| SHOP_ACC | 0.122 |
| RES_LUSE | 0.117 |
| POP_DENS | 0.064 |
| BEDS | 0.043 |
| COMMU_LU | 0.037 |
| COM_LUSE | 0.018 |
| CBD_ACC | 0.015 |
| DRAINAGE | 0.015 |
| EDU_ACC | 0.013 |
| BATHS | 0.01 |
| M_RD_ACC | 0.009 |
| FL_SPACE | 0.004 |
| BLD_AGE | 0.003 |

6.3 Case 2

The models in this analysis were trained with 360 houses and their predictability in estimating value was tested with the remaining 119 houses. The predictive model built for this case utilized the same fourteen independent variables. The results for case 2 are close between the neural network model and the hedonic price model. Figure 6.2 shows the actual and predicted rent of 119 houses of both models. From the figure it is seen that the neural network model can predict more accurately than the hedonic price model. Table 6.4 illustrates that the neural network model had a higher R^2 value of 59.67% than the hedonic price model (52.91%). This indicates that in this case neural network can predict the house rent more accurately than the hedonic price model. The neural network model had a mean absolute error of 24.61% while hedonic price model had a mean absolute error of 26.70%. So in terms of mean absolute error neural network model did outperform the hedonic price model but

only marginally. This result is contrary to the findings of the Do and Grudnitski (1992) study that reported the neural network mean absolute error (6.9%) to be significantly smaller than that of regression (11.3%), but supports the results of Worzala *et al.* (1995) study that reported the neural network mean absolute error (14.4%) to be marginally higher than their regression results (15.2%).

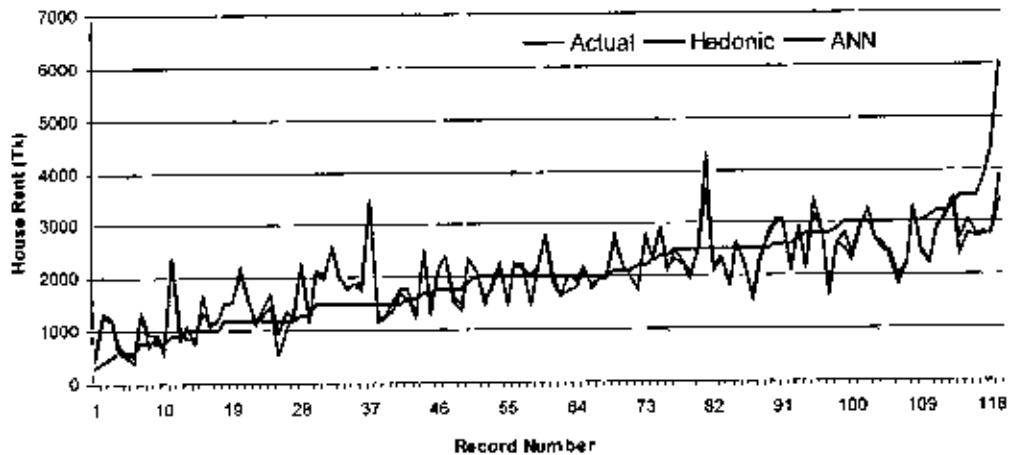


Figure 6.2: Actual and predicted house rent of 119 test sample

As detailed in Table 6.4, both the neural network model and the regression model predicted the same number of houses with an absolute error below 5 % (13.45%). Worzala *et al.* (1995) reported the same result where both the models predicted the same number of houses with an absolute error below 5 % (32.4%). However, as the absolute error range is increased, the neural network model becomes the better overall predictor for the 0-10% range, the 0-20% range and the greater-than-20% range of error.

Table 6.4: Prediction Results of Two Models Using Case 2 Data

| Absolute Error Range (%) | Neural Network Model | | Hedonic Price Model | |
|--------------------------|----------------------|--------------|---------------------|--------------|
| | % | No of Houses | % | No of Houses |
| 0-5 | 13.45 | 16 | 13.45 | 16 |
| 0-10 | 26.05 | 31 | 24.37 | 29 |
| 0-20 | 57.14 | 68 | 52.10 | 62 |
| >20 | 42.86 | 51 | 47.90 | 57 |
| Mean Absolute Error | 24.61 | 29 | 26.70 | 32 |
| R^2 | 0.5967 | | 0.5291 | |

Table 6.5 presents the results segmented by rent ranges of the test sample. At the lowest rent range, ANN was the better performer in terms of the mean absolute error test (38.5%). ANN model had twice the percentage of properties (14.6%) with less than 5% error than the hedonic model (7.3%). In rent range of Tk. 1501- 2500, the neural network model does the best job. The neural network model slightly outperformed the hedonic price model in the mean absolute error test (16% compared to 16.1%) and it also did a better job of predicting rent within 5% of the actual rent (22.9%) than the hedonic model (8.7%) in this rent range. In the highest rent range (Tk. 2500+), ANN again does a better job in predicting the actual rent than hedonic model in terms of mean absolute error test and the 5% error test.

Table 6.5: Comparison of the predictive power of each model per price range using Case 2 data

| Rent Range | No of Houses | ANN | | Hedonic Price Model | |
|-----------------|--------------|-------------------------|--------------------|-------------------------|--------------------|
| | | Mean Absolute Error (%) | Error Below 5% (%) | Mean Absolute Error (%) | Error Below 5% (%) |
| Tk. 0 - 1500 | 41 | 38.5 | 14.6 | 43.3 | 7.3 |
| Tk. 1501 - 2500 | 48 | 16.0 | 22.9 | 16.1 | 18.7 |
| Tk. 2501+ | 30 | 17.8 | 16.7 | 19.3 | 13.3 |

6.4 Case 3

In this case the best reduced hedonic price model for residential property rent asking price developed by Habib (2004) was compared with the neural network model. The neural network model was developed utilizing those independent variables which were finally selected for best reduced hedonic price model. There are several methods of regression for best reduced model depending on the method of entry and removal of independent variables to and from the regression model. This study used the stepwise method to find out the best-reduced model which was used by Habib (2004) in order to enhance the comparability of results between the two studies.

In total, six models had been constructed in the stepwise regression procedure. To insure replication of the methodology utilized by Habib (2004), two criteria had been used in removing independent variables in the stepwise regression method. They were based on an F statistic that is the square of the t statistic. The first criterion for removing variables was the minimum F value that a variable must have to remain in the model. This minimum value is sometimes known as the F -to-enter. The second criterion is the maximum probability of F -to-remove. In this study, the second criterion was used with a value of 0.10 for the maximum probability of F -to-remove and 0.05 was selected for the minimum probability of F -to-enter in the regression models. The model summary found after running stepwise regression is presented in Table 6.6.

Table 6.6: Model Summary

| Model | R ² | R Square | Adjusted R Square | Std. Error of the Estimate |
|-------|----------------|----------|-------------------|----------------------------|
| 1 | 0.620 | .385 | .384 | 708.054 |
| 2 | 0.679 | .461 | .459 | 663.436 |
| 3 | 0.711 | .506 | .503 | 635.762 |
| 4 | 0.723 | .523 | .519 | 625.731 |
| 5 | 0.731 | .534 | .529 | 618.942 |
| 6 | 0.737 | .543 | .538 | 613.201 |

1. Predictors: (Constant), BEDS

2. Predictors: (Constant), BEDS, FL_SPACE

3. Predictors: (Constant), BEDS, FL_SPACE, COMMU_LU

4. Predictors: (Constant), BEDS, FL_SPACE, COMMU_LU, M_RD_ACC

5. Predictors: (Constant), BEDS, FL_SPACE, COMMU_LU, M_RD_ACC, W_MAR_AC

6. Predictors: (Constant), BEDS, FL_SPACE, COMMU_LU, M_RD_ACC, W_MAR_AC, BATHS

* Dependent Variable: Rcnt

Among the six models, the best reduced model is comprised of three structural attributes (BEDS, FL_SPAC and BATHS), one neighborhood attribute name (COMMU_LU) and finally two transportation attributes (M_RD_ACC, W_MAR_AC) with a coefficient of determination R^2 of 0.543.

For this case the neural network model was developed utilizing the above six independent variables which were finally selected for the best reduced hedonic price model. The final model result found utilizing these six variables is shown in Figure 6.3. From figure it can be seen that the coefficient of determination R^2 value of the model was 0.6153.

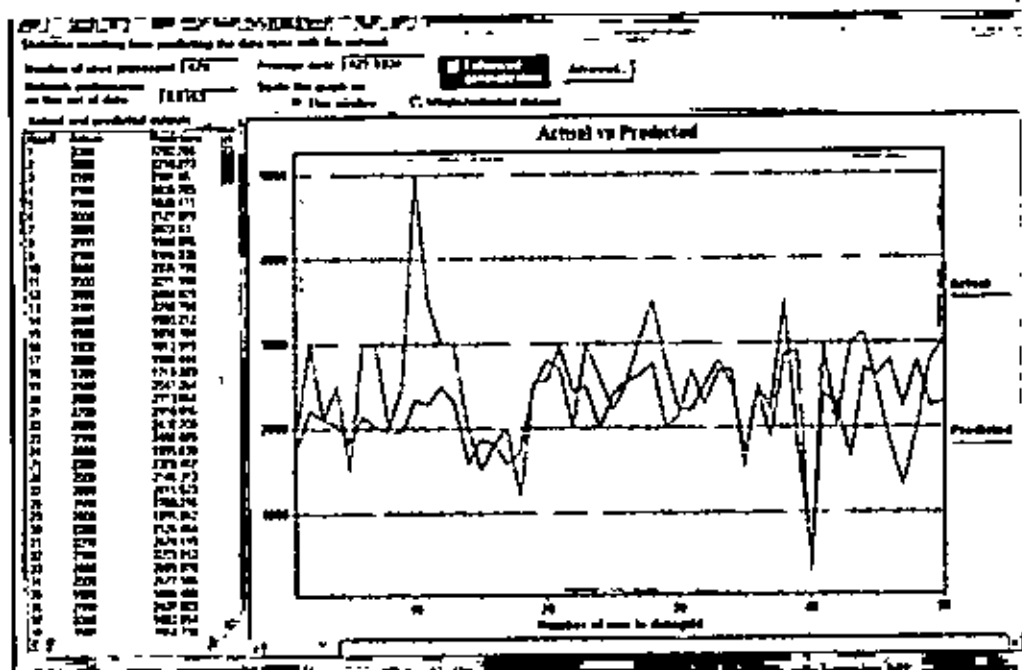


Figure 6.3: ANN model using case 3 data

Table 6.7: Predicting Results of Two Models Using Case 3 Data

| Absolute Error Range (%) | Neural Network Model | | Hedonic Price Model | |
|--------------------------|----------------------|--------------|---------------------|--------------|
| | % | No of Houses | % | No of Houses |
| 0-5 | 15.87 | 76 | 14.61 | 70 |
| 0-10 | 29.44 | 141 | 28.18 | 135 |
| 0-20 | 55.95 | 268 | 52.19 | 250 |
| >20 | 44.05 | 211 | 47.81 | 229 |
| Mean Absolute Error | 28.22 | 135 | 30.14 | 144 |
| R^2 | 0.6153 | | 0.543 | |

Table 6.7 presents the results of best reduced hedonic price model and neural network model. These results further evidence that consistency exists in the neural network models' better ability to accurately predict the actual house rent over the hedonic price model. The neural network model performed better in terms of the mean absolute error test (28.22% compared to 30.14%). The neural network model did a better job of predicting house rent within 5% of the actual rent (15.87%) than the hedonic price model (14.61%). The neural network model outperforms the hedonic price model as the absolute error range is increased. Since the R^2 value from

neural network model (61.53%) is higher than the hedonic price model (54.3%), it can be said that the neural network model can estimate the house rent more accurately than the hedonic price model.

6.5 Case 4

The data used in this case were classified into three house rent ranges. The ranges are Tk. 0 to 1500, Tk. 1501 to 2500 and more than Tk. 2500. In this analysis the models of each rent range were trained with one data set and tested with other data set. All of the predictive models built for this case utilized the same fourteen independent variables. The sample number of houses representing each data set is given in Table 6.8. The two samples of each price range were created by first sorting the houses by location, then by rent, and then by picking every fourth house for the production set. Table 6.9, 6.10 and 6.11 detail the descriptive statistics of the entire sample of each rent range and two subsets for training and testing. As can be seen from the tables, there were no significant differences between the training and testing data subsets of each rent range and each is a fair representation of the entire data set.

Table 6.8: Training and test sample size of each rent range

| Rent Range | Training Sample (No of houses) | Test Sample (No of houses) | Total (No of houses) |
|-----------------------|---|---------------------------------------|---------------------------------|
| Tk. 0 - 1500 | 135 | 45 | 180 |
| Tk. 1501- 2500 | 138 | 46 | 184 |
| Tk. 2500+ | 87 | 28 | 115 |

Table 6.9: Descriptive Statistics of Sample house for rent range 0-Tk.1500

| Variables | Mean | | | Maximum | | | Minimum | | |
|-----------|---------------|--------------|-------------|---------------|--------------|-------------|---------------|--------------|-------------|
| | Entire Sample | Training Set | Testing Set | Entire Sample | Training Set | Testing Set | Entire Sample | Training Set | Testing Set |
| RENT | 1043.6 | 1043.6 | 1043.6 | 1043.6 | 1043.6 | 1043.6 | 1043.6 | 1043.6 | 1043.6 |
| FL_SPACE | 1079.5 | 1053.1 | 1158.9 | 6000.0 | 4000.0 | 6000.0 | 200.0 | 200.0 | 300.0 |
| BEDS | 2.0 | 1.9 | 2.2 | 4.0 | 4.0 | 4.0 | 1.0 | 1.0 | 1.0 |
| BATHS | 1.1 | 1.1 | 1.2 | 2.0 | 2.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| BLD_AGE | 16.2 | 15.9 | 16.9 | 69.0 | 59.0 | 69.0 | 2.0 | 2.0 | 2.0 |
| POP_DENS | 54.2 | 54.0 | 55.0 | 161.7 | 161.7 | 161.7 | 7.4 | 7.4 | 7.4 |
| RES_LUSE | 38.6 | 38.7 | 38.6 | 45.4 | 45.4 | 45.4 | 27.0 | 27.0 | 27.0 |
| COM_LUSE | 4.5 | 4.5 | 4.4 | 8.6 | 8.6 | 8.6 | 1.4 | 1.4 | 1.4 |
| COMMU_LU | 2.4 | 2.4 | 2.4 | 5.3 | 5.3 | 5.3 | 0.2 | 0.2 | 0.2 |
| DRAINAGE | 114.0 | 112.5 | 118.4 | 760.1 | 611.0 | 760.1 | 2.5 | 2.5 | 3.1 |
| M_RD_ACC | 1135.6 | 1138.5 | 1126.6 | 2871.5 | 2871.5 | 2627.1 | 175.0 | 175.0 | 305.0 |
| CBD_ACC | 2939.3 | 2950.1 | 2907.1 | 5603.6 | 5603.6 | 5499.9 | 320.3 | 381.6 | 320.3 |
| W_MAR_AC | 2497.2 | 2503.6 | 2477.9 | 5603.4 | 5603.4 | 5359.1 | 183.4 | 183.4 | 320.5 |
| EDU_ACC | 892.2 | 904.6 | 855.0 | 2703.8 | 2703.8 | 2369.3 | 3.1 | 3.1 | 35.3 |
| SHOP_ACC | 2340.3 | 2341.1 | 2337.8 | 5691.1 | 5691.1 | 5446.7 | 149.6 | 219.9 | 149.6 |

Table 6.10: Descriptive Statistics of Sample house for rent range of Tk. 1501-2500

| Variables | Mean | | | Maximum | | | Minimum | | |
|-----------|---------------|--------------|-------------|---------------|--------------|-------------|---------------|--------------|-------------|
| | Entire Sample | Training Set | Testing Set | Entire Sample | Training Set | Testing Set | Entire Sample | Training Set | Testing Set |
| RENT | 2143.1 | 2142.2 | 2145.7 | 2500.0 | 2500.0 | 2500.0 | 1580.0 | 1580.0 | 1600.0 |
| FL_SPACE | 1614.7 | 1630.6 | 1567.2 | 8000.0 | 8000.0 | 2600.0 | 500.0 | 500.0 | 600.0 |
| BEDS | 2.9 | 3.0 | 2.7 | 4.0 | 4.0 | 4.0 | 2.0 | 2.0 | 2.0 |
| BATHS | 1.6 | 1.6 | 1.6 | 3.0 | 3.0 | 3.0 | 1.0 | 1.0 | 1.0 |
| BLD_AGE | 20.1 | 21.3 | 16.5 | 129.0 | 129.0 | 51.0 | 2.0 | 2.0 | 2.0 |
| POP_DENS | 68.9 | 69.2 | 67.9 | 161.7 | 161.7 | 161.7 | 7.4 | 7.4 | 7.4 |
| RES_LUSE | 42.2 | 42.3 | 42.0 | 45.4 | 45.4 | 45.4 | 27.0 | 27.0 | 27.0 |
| COM_LUSE | 6.5 | 6.5 | 6.5 | 8.6 | 8.6 | 8.6 | 1.4 | 1.4 | 1.4 |
| COMMU_LU | 3.3 | 3.3 | 3.3 | 5.3 | 5.3 | 5.3 | 0.2 | 0.2 | 0.2 |
| DRAINAGE | 33.9 | 32.1 | 39.3 | 733.9 | 403.5 | 733.9 | 1.3 | 1.3 | 3.4 |
| M_RD_ACC | 855.5 | 854.1 | 859.4 | 2246.0 | 2054.7 | 2246.0 | 188.2 | 207.3 | 188.2 |
| CBD_ACC | 2021.0 | 2018.9 | 2027.2 | 5404.6 | 5404.6 | 4946.1 | 207.5 | 207.5 | 349.2 |
| W_MAR_AC | 1656.9 | 1648.3 | 1682.6 | 4945.9 | 4842.3 | 4945.9 | 207.3 | 207.3 | 239.9 |
| EDU_ACC | 936.3 | 997.2 | 753.6 | 17775.6 | 17775.6 | 2305.8 | 7.9 | 7.9 | 65.9 |
| SHOP_ACC | 1554.7 | 1545.6 | 1582.1 | 5084.5 | 5084.5 | 5033.5 | 114.6 | 114.6 | 223.3 |

Table 6.11: Descriptive Statistics of Sample house for rent range of more than Tk. 2500

| Variables | Mean | | | Maximum | | | Minimum | | |
|-----------|---------------|--------------|-------------|---------------|--------------|-------------|---------------|--------------|-------------|
| | Entire Sample | Training Set | Testing Set | Entire Sample | Training Set | Testing Set | Entire Sample | Training Set | Testing Set |
| RENT | 3109.1 | 3109.1 | 3100.0 | 7000.0 | 7000.0 | 6000.0 | 2600.0 | 2600.0 | 2600.0 |
| FL_SPACE | 2107.7 | 2107.7 | 2024.6 | 7000.0 | 7000.0 | 4320.0 | 800.0 | 800.0 | 1000.0 |
| BEDS | 3.2 | 3.2 | 3.2 | 4.0 | 4.0 | 4.0 | 1.0 | 1.0 | 2.0 |
| BATHS | 1.9 | 1.9 | 2.0 | 3.0 | 3.0 | 3.0 | 1.0 | 1.0 | 1.0 |
| BLD_AGE | 20.0 | 20.0 | 20.6 | 69.0 | 69.0 | 52.0 | 1.0 | 1.0 | 2.0 |
| POP_DENS | 74.1 | 74.1 | 72.5 | 161.7 | 161.7 | 111.5 | 9.5 | 9.5 | 9.5 |
| RES_LUSE | 43.5 | 43.5 | 43.5 | 45.4 | 45.4 | 45.4 | 28.4 | 28.4 | 28.4 |
| COM_LIUSE | 7.4 | 7.4 | 7.3 | 8.6 | 8.6 | 8.6 | 1.8 | 1.8 | 1.8 |
| COMMU_LU | 3.9 | 3.9 | 3.8 | 5.3 | 5.3 | 5.3 | 1.0 | 1.0 | 1.0 |
| DRAINAGE | 28.5 | 28.5 | 20.4 | 702.2 | 702.2 | 171.2 | 2.5 | 2.5 | 4.7 |
| M_RD_ACC | 685.8 | 685.8 | 620.1 | 2341.1 | 2341.1 | 1429.0 | 48.8 | 48.8 | 48.8 |
| CBD_ACC | 1755.3 | 1755.3 | 1691.9 | 5041.2 | 5041.2 | 3652.7 | 225.2 | 225.2 | 225.2 |
| W_MAR_AC | 1466.7 | 1466.7 | 1381.9 | 5041.0 | 5041.0 | 3521.6 | 82.1 | 82.1 | 121.9 |
| EDU_ACC | 934.6 | 934.6 | 897.3 | 2475.0 | 2475.0 | 2475.0 | 21.7 | 21.7 | 21.7 |
| SHOP_ACC | 1226.3 | 1226.3 | 1142.3 | 5128.6 | 5128.6 | 3740.1 | 88.3 | 88.3 | 88.3 |

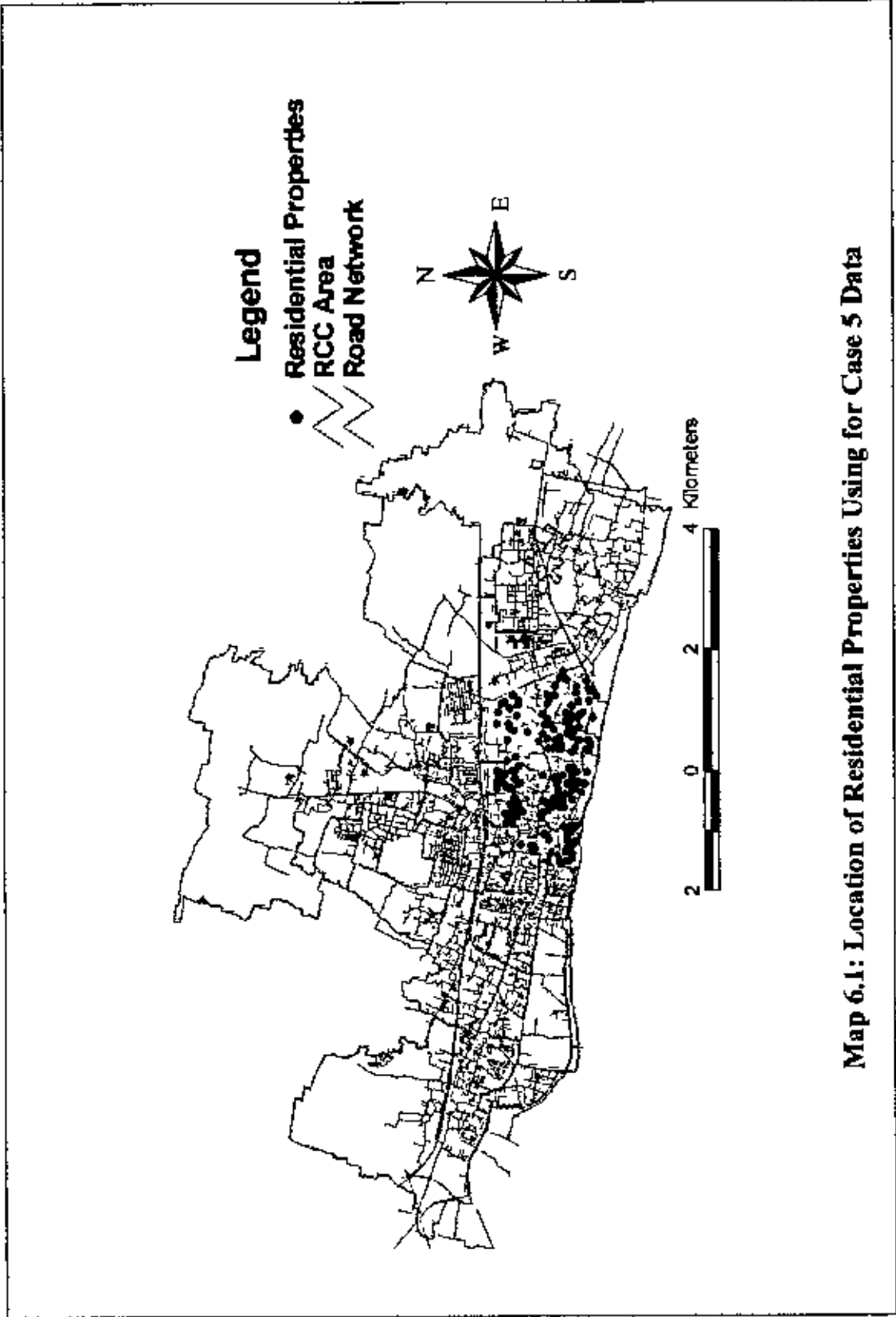
Table 6.12 shows the prediction results of each model for different house rent range. It can be seen from table that when the data set was constrained to different house rent ranges, the results for mean absolute error of ANN models for each rent range was less than that of hedonic price models. The neural network models predicted the higher percentage of houses than the hedonic model with an absolute error below 5% for all the rent range. So in terms of the percentage of predicted rent with 5% of the actual rent, the neural network models outperformed the hedonic models. The maximum absolute error showed that the neural network model became better model than the hedonic price model since the neural network model had lower maximum absolute errors for all three rent ranges. Therefore, the results provide a clear evidence of neural network model's superiority over the hedonic price model in predicting house rent.

Table 6.12: Prediction result of each model using Case 4 data

| Rent Range | ANN | | | Hedonic | | |
|----------------|-------------------------------|----------------------------------|--------------------------|-------------------------------|----------------------------------|--------------------------|
| | Mean Absolute Error (%) | Maximum Absolute Error (%) | Error Below 5% (%) | Mean Absolute Error (%) | Maximum Absolute Error (%) | Error Below 5% (%) |
| Tk. 0 - 1500 | 27.93 | 156.51 | 20 | 28.13 | 157.48 | 20 |
| Tk. 1501- 2500 | 8.37 | 20.81 | 39.13 | 9.39 | 44.47 | 36.96 |
| Tk. 2500+ | 8.33 | 39.009 | 42.86 | 8.94 | 44.89 | 39.29 |

6.6 Case 5

The data in case 5 was constrained to a more homogeneous set of houses. This was accomplished by including houses from only one Strategic Planning Zone (SPZ) area defined by the Rajshahi Master Plan Project. The models were trained with 145 houses and tested with 48 houses, representing a homogeneous set of houses from SPZ no. 18 area. The location of these houses is shown in Map 6.1. The two samples were created by first sorting the houses by rent and then by picking every fourth house. The models built for this case utilized the following eleven independent variables: usable living area, number of bedrooms, number of bathrooms, age of residential property structure, population density, Euclidian distance from the property to nearest point of drainage network, network access distance from property to central business district (CBD), network access distance from property to wholesale markets, network access distance from property to primary school, network access distance from property to shopping centers. Three variables namely percentage of area dedicated to residential use, percentage of area dedicated to commercial use, percentage of area dedicated to community facilities have been removed from models because there are same values of these three variables in all of the data set. Table 6.13 contains the descriptive statistics for this case.



Map 6.1: Location of Residential Properties Using for Case 5 Data

6.13: Descriptive Statistics of Sample houses for Case 5: SPZ no 18

| Variables | Mean | | | Maximum | | | Minimum | | |
|-----------|---------------------|--------------------|------------------|---------------|--------------|-------------|---------------|--------------|-------------|
| | Entire Sample (193) | Training Set (145) | Testing Set (48) | Entire Sample | Training Set | Testing Set | Entire Sample | Training Set | Testing Set |
| RENT | 2145.8 | 2134.8 | 2178.8 | 5000.0 | 5000.0 | 5000.0 | 350.0 | 350.0 | 500.0 |
| FL_SPACE | 1581.6 | 1594.4 | 1543.0 | 8000.0 | 8000.0 | 2800.0 | 200.0 | 200.0 | 200.0 |
| BEDS | 2.9 | 2.9 | 2.9 | 4.0 | 4.0 | 4.0 | 1.0 | 1.0 | 2.0 |
| BATHS | 1.6 | 1.6 | 1.7 | 3.0 | 3.0 | 3.0 | 1.0 | 1.0 | 1.0 |
| BLD_AGE | 22.3 | 22.2 | 22.6 | 129.0 | 102.0 | 129.0 | 1.0 | 2.0 | 1.0 |
| POP_DENS | 90.2 | 89.2 | 93.2 | 161.7 | 161.7 | 161.7 | 35.8 | 35.8 | 35.8 |
| DRAINAGE | 20.3 | 20.7 | 19.4 | 281.1 | 281.1 | 133.0 | 1.3 | 1.3 | 3.3 |
| M_RD_ACC | 805.6 | 811.4 | 788.2 | 2200.4 | 2200.4 | 1519.6 | 206.9 | 206.9 | 278.7 |
| CBD_ACC | 1497.4 | 1494.4 | 1506.4 | 5142.8 | 5142.8 | 3012.9 | 207.5 | 207.5 | 320.3 |
| W_MAR_AC | 1212.6 | 1215.8 | 1202.8 | 4988.0 | 4988.0 | 2613.9 | 176.5 | 183.4 | 176.5 |
| EDU_ACC | 709.5 | 693.5 | 757.9 | 2583.8 | 2583.8 | 1627.6 | 21.7 | 21.7 | 43.6 |
| SHOP_ACC | 1377.2 | 1365.5 | 1412.6 | 5230.2 | 5230.2 | 3025.7 | 114.6 | 149.6 | 114.6 |

The results of the neural network model, in terms of the mean absolute error, were better than the results with Case 2 data but worse for the hedonic price model. In terms of mean absolute error, neural network model (24.3%) outperformed the hedonic model (27.3) in this case.

6.14: Prediction results for both models using Case 5 data.

| Absolute Error Range (%) | Neural Network Model | | Hedonic Price Model | |
|--------------------------|----------------------|--------------|---------------------|--------------|
| | % | No of Houses | % | No of Houses |
| 0-5 | 18.8 | 9 | 16.7 | 8 |
| 0-10 | 25.0 | 12 | 25.0 | 12 |
| 0-20 | 54.2 | 26 | 47.9 | 23 |
| >20 | 45.8 | 22 | 52.1 | 25 |
| Mean Absolute Error | 24.3 | 11 | 27.3 | 13 |
| R^2 | 0.512 | | 0.501 | |

Table 6.14 shows the percentage of houses that had predicted values within 5% of the actual rent increased for both models in the current case. The neural network model had a higher percentage (18.8% compared to 16.7%). Both models gave the same result at the 0-10% range whereas the ANN model had fewer houses in the 0-20% error range and greater than 20% error range. Figure 6.4 shows the actual and predicted rent of both models for case 5 data. From the figure it is seen that the neural network model can predict more accurately than the hedonic price model. In this case, the R^2 from the neural network model (0.512) is slightly higher than the R^2 of the hedonic price model (0.501). These results indicate that with a homogenous set of data neural network model had better prediction capability of house rent than the hedonic price model.

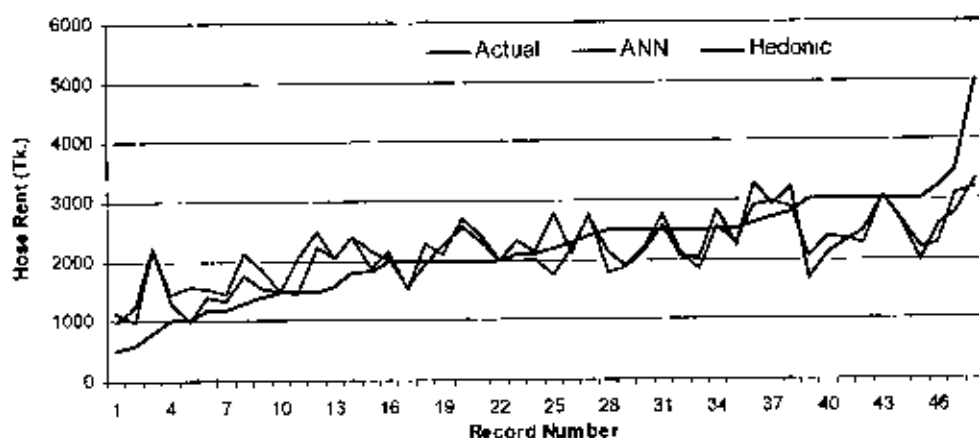


Figure 6.4: Actual and predicted house rent of two models using Case 5 data

6.7 Case 6

The case compares the predictive performance of ANN model and hedonic price model with respect to their ability to estimate the value of a random sample of "normal" residential properties and a sample of outlier properties. Outlier properties were determined as properties that possessed a z-score greater than 1.7. A z-score was measured by subtracting the property rent from the average rent of the houses in the sample and dividing by the sample standard deviation. Thirty outlier properties

were identified and separated into an “outlier” holdout sample, leaving 449 properties in the “normal properties” data set. The remaining 449 properties were sorted by rent and every fourth property was separated out into a “normal” holdout sample, leaving 337 properties to be the training sample for creating both the ANN model and hedonic price model. Table 6.15 details the descriptive statistics for each of these data subsets. There were no significant differences between the training and the normal holdout data sets. The average house rent in both the training set and normal holdout sample was approximately Tk. 1900, and standard deviation of Tk. 752 was observed. House rents in these two subsets ranged from Tk. 500 to Tk. 3,300.

The properties in the outlier holdout sample exhibit significant differences from the training and normal samples. These properties were generally more expensive with an average rent of Tk. 2,500, a range of Tk. 300 to Tk. 7,000, and a standard deviation of Tk. 2,081. Fourteen variables, which have been used in the previous cases, were chosen as the independent variables for both models.

Table 6.15 Descriptive Statistics of Sample houses for Case 6

| Variables | Mean | | | Maximum | | | Minimum | | |
|-----------|--------------------|------------------|------------------|--------------|------------|-------------|--------------|------------|-------------|
| | Training Set (337) | Normal Set (112) | Outlier Set (30) | Training Set | Normal Set | Outlier Set | Training Set | Normal Set | Outlier Set |
| RENT | 1922.7 | 1929.7 | 2521.7 | 3300.0 | 3200.0 | 7000.0 | 500.0 | 500.0 | 300.0 |
| FL_SPACE | 1551.5 | 1448.8 | 1622.7 | 8000.0 | 4400.0 | 4800.0 | 200.0 | 300.0 | 200.0 |
| BEDS | 2.6 | 2.7 | 2.6 | 4.0 | 4.0 | 4.0 | 1.0 | 1.0 | 1.0 |
| BATHS | 1.5 | 1.4 | 1.6 | 3.0 | 3.0 | 3.0 | 1.0 | 1.0 | 0.0 |
| BLD_AGE | 19.2 | 17.6 | 15.7 | 129.0 | 102.0 | 69.0 | 2.0 | 2.0 | 1.0 |
| POP_DENS | 65.1 | 65.3 | 56.7 | 161.7 | 161.7 | 161.7 | 7.4 | 7.4 | 9.5 |
| RES_USE | 41.3 | 41.5 | 38.9 | 45.4 | 45.4 | 45.4 | 27.0 | 27.0 | 28.4 |
| COM_USE | 5.9 | 6.1 | 5.5 | 8.6 | 8.6 | 8.6 | 1.4 | 1.4 | 1.8 |
| COMMU_LU | 3.1 | 3.1 | 2.8 | 5.3 | 5.3 | 5.3 | 0.2 | 0.2 | 1.0 |
| DRAINAGE | 62.6 | 52.7 | 101.1 | 760.1 | 611.0 | 391.4 | 1.3 | 2.3 | 2.6 |
| M_RD_ACC | 911.1 | 914.4 | 1040.5 | 2717.9 | 2627.1 | 2871.5 | 146.5 | 48.8 | 278.7 |
| CBD_ACC | 2276.1 | 2207.9 | 2949.8 | 5535.5 | 5376.2 | 5603.6 | 225.2 | 207.5 | 278.8 |
| W_MAR_AC | 1896.7 | 1834.3 | 2613.4 | 5449.9 | 5359.1 | 5603.4 | 82.1 | 173.6 | 278.9 |
| EDU_ACC | 938.4 | 896.4 | 790.5 | 17775.6 | 2475.0 | 2703.8 | 7.9 | 3.1 | 21.9 |
| SHOP_ACC | 1727.3 | 1717.1 | 2464.5 | 5537.5 | 5446.7 | 5691.1 | 149.6 | 88.3 | 366.6 |

Table 6.16 details the mean absolute error and maximum absolute error test results and the R² value. ANN model performed better in normal hold out sample results. When measured by the mean absolute error test, the ANN model outperformed the hedonic price model. The maximum absolute error test showed that ANN model did outperform the hedonic price model (317.9 per cent vs. 320.7 per cent). The higher R² value of ANN model (0.612 compared to 0.564) indicates that the ANN model can predict the house rent more accurately than the hedonic price model. Thus, the results indicate the out performance of ANN model for the normal holdout sample.

The results from the outlier sample clearly demonstrate the lower performance of hedonic price model in comparison to ANN model. ANN model had the mean absolute error of 78.1% which is far better than that of hedonic price model (104.3%). The maximum absolute error test showed the better performance of ANN

model (300.3 per cent compared to 338.8 per cent). ANN model can predict the outlier properties more precisely than the hedonic price model since its R^2 value is significantly higher than the hedonic price model (0.579 vs. 0.478). So the results show that ANN model outperformed the hedonic price model for the outlier holdout sample.

Table 6.16: Prediction results for both models using Case 6 data

| | Results of the "Normal" Holdout Sample | | Results of the "Outlier" Holdout Sample | |
|----------------------------|---|-----------------|--|-----------------|
| | ANN | Hedonic Pricing | ANN | Hedonic Pricing |
| R^2 | 0.612 | 0.564 | 0.579 | 0.478 |
| Mean Absolute Error (%) | 24.3 | 26.7 | 78.1 | 104.3 |
| Maximum absolute Error (%) | 317.9 | 320.7 | 300.3 | 338.8 |

Table 6.17 shows the percentage of predicted value within 0-5 per cent, 0-10 percent, 0-20 percent and over 20 percent absolute error from the actual house rent. The results for the normal holdout sample show that ANN model had twice the percentage of houses with less than 5% error than their hedonic price model which coincides with the Do and Grudnitski (1992) results and with the increase of error range ANN model did outperform the hedonic price model.

Table 6.17: Predictive power of the models

| Absolute Error Range (%) | Results of the "Normal" Holdout Sample | | Results of the "Outlier" Holdout Sample | |
|-----------------------------|---|---------------------|--|---------------------|
| | ANN (%) | Hedonic Pricing (%) | ANN (%) | Hedonic Pricing (%) |
| 0-5 | 20.5 | 10.7 | 6.7 | 0.0 |
| 0-10 | 33.9 | 26.8 | 6.7 | 0.0 |
| 0-20 | 59.8 | 56.3 | 13.3 | 3.3 |
| >20 | 40.2 | 43.8 | 86.7 | 96.7 |

The results from the outlier properties sample tests support the contention that hedonic price model are ineffective estimators of outlier values. Hedonic price model could not estimate any property within 5 per cent and 10 per cent of their actual rent where as ANN model predicated 6.7 per cent of houses for both the range. ANN model also outperformed the hedonic price model at the 0-20% arrange and the greater than 20% range of error. Therefore, the results provide clear evidence of superiority of ANN model for the outlier holdout sample.

6.8 Summary

The results discussed in this chapter indicate that the neural network model outperformed the hedonic price model in all of the cases in predicting house rent of Rajshahi City, although the difference between the two models was not large in all cases. Major concerns regarding the consistency of neural networks have been aired in the literature. The study found no problem of consistency. The analysis done with the neural network model gave better results consistently in all of the cases discussed. ANN model as well as hedonic price model performed better when they were trained and tested with same data set and they performed poorly when they were used for out-of-sample forecast, although in both cases ANN models outperformed the hedonic price models. ANN model also showed its supremacy in predicting outlier data set. As a result, the ANN model yields better prediction results compared to the hedonic price model. Based on the analysis of this chapter some recommendations have been formulated in the following chapter including concluding remarks.

Chapter 7

CONCLUSION AND RECOMMENDATION

Chapter 7: Conclusion and Recommendation

7.1 Conclusion

The study has developed an artificial neural network model for house rent prediction using 479 house information of Rajshahi City. The R^2 of the developed ANN model is 0.621 for sample forecast. The study has demonstrated that neighborhood attributes are the most significant factors in determining the house rent of Rajshahi City. The percentage of area dedicated to community facilities and percentage of area dedicated to commercial use have contributed more to the predictive power of model than the other attributes. So it is seen that land use has a great impact on house rent in Rajshahi City.

The study also empirically compares the predictive power of the artificial neural network model with the hedonic price model on house rent prediction. The comparison was conducted in six stages or cases. The first case conducted the predictive power comparisons utilizing the whole data set for training and testing. In the second case the models were trained with 360 houses and their predictability in estimating value were tested with remaining 119 houses. In the third case, the ANN model is compared with the best reduced hedonic price model and the fourth case classified the data set into three house rent range. The fifth case restricted the data set to include a more homogeneous set of houses from a single strategic planning zone area. Finally in the sixth case the tests were conducted both for a normal sample of properties as well as an outlier sample of properties. The results indicate that the neural network model outperformed the hedonic price model in all of the cases. In this study, the ANN model consistently gave better result than the hedonic price model, although the difference between the two models was not too large. ANN model and hedonic price model both do better when they are trained and tested with the same data set but they performed poorer on out-of-sample forecast. But in both cases ANN model showed better results in comparison to hedonic price model. The study also supports the superiority of ANN model in prediction of outlier holdout

sample. The artificial neural network model can overcome some of the problems related to the data patterns and the underlining assumption of the hedonic price model. As a result the model can give a better prediction result when compares with the hedonic price model. Nevertheless, it should be noted that the optimal artificial neural network model is created by a trial and error strategy. Without this strategy the results may not indicate superiority of the neural network model.

The study indicates that some problems are encountered during the development and implementation of the ANN model. The problems are that the proper settings for the models are not obvious and it takes several iterations to find the set of parameters that best fit an application. Like some other studies (Worzala et al. 1995; Allen and Zumwalt, 1994), this study found that small changes can result in very different findings and the stopping point of learning is critical. In some cases it is very difficult to prevent overtraining.

In light of the short comings of the hedonic price model and the comparative goodness of the results of the neural network, the study supports the conclusion of Do and Grudnitski (1992) who indicated that a neural network model performs better than a multiple regression model for estimating the value of residential property.

7.2 Recommendations

While the results of this study indicate that neural networks are very reliable, it is also necessary to do further research on larger and different data set to establish the superiority of ANN model over the hedonic price model. More research could determine if other software package and/or other data sets experience similar results. For example the current results might not be representative of all possible data sets and further research would determine the sensitivity of the valuation technique to data differences. It may be possible that neural networks will do much better job than hedonic price model if the nonlinear relationships between the variables are greater. This study considered only one year rent information of the houses. The time effect of the house rent, which could potentially impact the estimated results was

ignored in this study (the same house should have different rent in different years, assuming the age factor is constant). So this time effect of the house rent should be considered in future research.

The results of this study do provide a practical recommendations regarding application of this model that if an artificial neural network model is to be used, the process and results of this study support a trial-and-error strategy to find the optimal artificial neural network model. It was only through this strategy that the neural network models created in this study could compete with the hedonic price models.

Finally cautions must be undertaken before any decision to utilize these methods in valuation practice of other urban areas. Because the results found in this study could be a function of the specific data characteristics of the sample used. However, despite the comparative advantage of ANN model in house rent prediction over traditional hedonic price model, the ultimate benefits of a neural network model can be fully realized when it performs better on larger and different data set.

Based on the findings of the study certain recommendations can be made for practical applications of this model in Bangladesh. Some recommendations may be also useful for plan formulation and implementations in Rajshahi City.

The Rajshahi Development Authority (RDA) should take low income housing projects apart from the central business district as the study showed that housing rents decrease with the increase of distance from the CBD at Rajshahi City. This study showed that the percentage of area dedicated to community facilities and percentage of area dedicated to commercial use had a great contribution in determination of house rent of Rajshahi City. So the Rajshahi Development Authority should develop housing projects in the areas where percentage of community facilities and commercial use is lower. The findings and developed model of this study is expected to be very helpful to the Rajshahi Development Authority (RDA) as they have already taken an extensive effort for transportation infrastructure investment to increment transportation network through the Rajshahi

Mater Plan Project. They can use this model to predict the house rent changes due to the implementation of this transportation project. By predicting house rent they can collect additional taxes/revenues for the implementation of the project in Rajshahi City.

An accurate prediction of house rent/price is important to real estate developers. Real estate business is now booming in urban areas of Bangladesh. The ANN model can be an effective tool for these developers and investors for estimating house rent/price more accurately over traditional methods. By using this model and results of this study the real estate developers can easily select location of different housing projects in Rajshahi City.

Public authorities can assess holding tax, regulate rent more easily using this model. Most of the house owners in Bangladesh built their houses by taking loan from Bank. This loan approval process is very time consuming due to the unavailability of any authentic property valuation techniques. The loan providers can use this model to estimate the house price which will help them to take decision whether they provide loan or not as well as regarding the amount of loan.

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APPENDIX A

Appendix A

Table: Structural Attributes and Coordinate locations of the residential properties

| BUET ID | FL SPACE | BEDS | BATHS | BLD AGE | X COORD | Y COORD |
|---------|----------|------|-------|---------|--------------|--------------|
| 1 | 1400 | 2 | 1 | 8 | 360562.67420 | 695150.96325 |
| 2 | 1600 | 3 | 2 | 24 | 360445.78300 | 695183.70890 |
| 3 | 1700 | 3 | 1 | 24 | 360279.90030 | 695241.39260 |
| 4 | 1600 | 3 | 2 | 14 | 359869.68300 | 695307.41200 |
| 5 | 1400 | 3 | 1 | 25 | 359358.50600 | 695248.77990 |
| 6 | 1600 | 3 | 1 | 14 | 359510.66500 | 695604.10450 |
| 7 | 1600 | 3 | 1 | 14 | 359426.55350 | 695702.93000 |
| 8 | 1200 | 3 | 1 | 24 | 359596.96600 | 695777.31439 |
| 9 | 1400 | 3 | 1 | 9 | 359901.48400 | 695785.59350 |
| 10 | 1200 | 3 | 1 | 14 | 360075.61350 | 695744.52250 |
| 11 | 1400 | 3 | 1 | 19 | 360148.05100 | 695941.33850 |
| 12 | 2000 | 3 | 1 | 16 | 360273.94200 | 695633.77245 |
| 13 | 1600 | 3 | 1 | 9 | 360422.06950 | 695622.11300 |
| 14 | 1600 | 3 | 1 | 10 | 360466.35500 | 695808.73150 |
| 15 | 1800 | 3 | 1 | 14 | 360450.43635 | 695864.03950 |
| 16 | 1600 | 3 | 1 | 21 | 360575.66300 | 695696.56645 |
| 17 | 1600 | 3 | 1 | 28 | 360484.58935 | 695594.00200 |
| 18 | 1200 | 3 | 2 | 24 | 360714.73705 | 695050.53180 |
| 19 | 1200 | 2 | 1 | 15 | 360024.34700 | 695477.78500 |
| 20 | 1000 | 3 | 1 | 14 | 360036.19530 | 695680.08435 |
| 21 | 1200 | 2 | 1 | 31 | 360364.67100 | 695749.16150 |
| 22 | 1000 | 2 | 1 | 18 | 360148.63475 | 695764.51470 |
| 23 | 1000 | 2 | 1 | 4 | 360314.75650 | 695928.94215 |
| 25 | 1200 | 2 | 1 | 24 | 359649.89545 | 695651.30850 |
| 26 | 1400 | 3 | 2 | 33 | 358028.38331 | 695431.37823 |
| 27 | 1400 | 3 | 2 | 3 | 358024.50181 | 695390.01112 |
| 28 | 1800 | 4 | 2 | 21 | 357958.52000 | 695473.07800 |
| 29 | 1600 | 3 | 1 | 39 | 358033.84773 | 695589.29600 |
| 30 | 1400 | 3 | 2 | 17 | 358085.85800 | 695598.70200 |
| 31 | 1400 | 3 | 2 | 52 | 358199.54500 | 695573.33750 |
| 32 | 1400 | 2 | 1 | 12 | 358121.78639 | 695443.10158 |
| 33 | 1200 | 3 | 2 | 16 | 357946.45350 | 695678.89500 |
| 34 | 1600 | 3 | 2 | 9 | 358081.18600 | 695654.51146 |
| 35 | 1800 | 3 | 2 | 12 | 358041.29250 | 695718.12644 |
| 36 | 1800 | 3 | 3 | 24 | 357905.99450 | 695509.16350 |
| 37 | 1200 | 3 | 2 | 21 | 357813.15000 | 695549.97450 |
| 38 | 1400 | 2 | 1 | 17 | 357913.68700 | 695576.09850 |
| 39 | 1400 | 3 | 2 | 21 | 357753.31700 | 695610.40609 |
| 40 | 1600 | 2 | 1 | 6 | 357668.30400 | 695606.05950 |
| 41 | 1800 | 3 | 2 | 23 | 357652.85483 | 695739.76955 |
| 42 | 1800 | 2 | 1 | 39 | 357626.28076 | 695803.97350 |
| 43 | 1800 | 3 | 2 | 49 | 357604.55024 | 695581.05650 |
| 44 | 2000 | 3 | 2 | 19 | 357590.00150 | 695471.18000 |
| 45 | 1000 | 2 | 1 | 22 | 357681.32750 | 695405.85900 |
| 46 | 1200 | 2 | 1 | 9 | 357635.32650 | 695436.29500 |
| 47 | 1200 | 3 | 2 | 29 | 357786.99751 | 695464.09165 |
| 48 | 1200 | 2 | 1 | 3 | 357667.88250 | 695565.98500 |
| 49 | 1000 | 2 | 1 | 29 | 357691.10995 | 695746.94953 |
| 50 | 1600 | 2 | 1 | 9 | 357794.59921 | 695701.16003 |
| 51 | 2500 | 4 | 2 | 54 | 358260.68800 | 694877.28050 |

| | | | | | | |
|-----|------|---|---|-----|--------------|--------------|
| 52 | 2400 | 4 | 2 | 24 | 358291.06090 | 694837.60410 |
| 53 | 2500 | 4 | 2 | 36 | 358304.15650 | 694805.00970 |
| 54 | 250 | 1 | 1 | 22 | 358360.57325 | 694751.60220 |
| 55 | 2000 | 3 | 1 | 17 | 358367.19900 | 694868.23350 |
| 56 | 2200 | 4 | 3 | 24 | 358230.09600 | 694885.04150 |
| 57 | 1870 | 3 | 1 | 44 | 358466.01925 | 694872.52850 |
| 58 | 1240 | 2 | 1 | 39 | 358454.62700 | 694869.50450 |
| 59 | 2050 | 4 | 2 | 26 | 358508.27100 | 694826.83900 |
| 60 | 1700 | 4 | 2 | 39 | 358051.58300 | 694967.74400 |
| 61 | 2260 | 4 | 2 | 24 | 358067.80185 | 694992.05380 |
| 62 | 1700 | 3 | 1 | 69 | 358178.01407 | 694805.18185 |
| 63 | 2296 | 4 | 2 | 2 | 358096.23050 | 694822.61000 |
| 64 | 1200 | 2 | 1 | 38 | 358064.16700 | 694880.45700 |
| 65 | 1796 | 3 | 1 | 37 | 358074.65200 | 694911.30800 |
| 66 | 1750 | 3 | 1 | 39 | 358292.23200 | 695380.91500 |
| 67 | 2500 | 4 | 2 | 44 | 358291.48900 | 695421.80300 |
| 68 | 1500 | 3 | 2 | 24 | 358221.19303 | 695407.61649 |
| 69 | 1450 | 3 | 2 | 32 | 358254.89500 | 695403.13700 |
| 70 | 2120 | 4 | 2 | 29 | 358266.79050 | 695377.06200 |
| 72 | 1700 | 3 | 1 | 25 | 358315.88000 | 695582.94400 |
| 73 | 1600 | 3 | 1 | 102 | 358464.33500 | 695198.62300 |
| 74 | 1434 | 3 | 2 | 44 | 358480.33000 | 695228.56050 |
| 75 | 1816 | 3 | 2 | 94 | 358385.28300 | 695166.67660 |
| 81 | 2600 | 3 | 2 | 26 | 358467.28650 | 696004.26500 |
| 82 | 3500 | 4 | 3 | 56 | 358586.06209 | 696045.89788 |
| 83 | 1600 | 2 | 1 | 6 | 358555.75450 | 696070.18955 |
| 84 | 3800 | 3 | 3 | 12 | 358356.11050 | 695902.26343 |
| 85 | 2000 | 2 | 1 | 29 | 358415.57050 | 695876.82200 |
| 86 | 3600 | 4 | 2 | 12 | 358413.20600 | 695828.46200 |
| 87 | 3400 | 4 | 3 | 27 | 358451.89085 | 695780.31300 |
| 88 | 2500 | 3 | 2 | 28 | 358392.39030 | 695794.92600 |
| 89 | 2200 | 3 | 2 | 36 | 358469.65550 | 695731.05650 |
| 90 | 3800 | 4 | 2 | 42 | 358212.56150 | 695915.88000 |
| 91 | 3500 | 4 | 3 | 22 | 358161.47404 | 695956.85100 |
| 92 | 2500 | 3 | 2 | 17 | 358141.83250 | 696014.47100 |
| 93 | 3000 | 4 | 2 | 12 | 358088.04131 | 695968.90850 |
| 94 | 1800 | 3 | 2 | 7 | 358079.81100 | 696006.37850 |
| 95 | 2000 | 3 | 2 | 36 | 358031.38250 | 695963.20550 |
| 96 | 3200 | 4 | 2 | 17 | 357997.42865 | 696065.56900 |
| 97 | 3000 | 4 | 2 | 14 | 357911.13841 | 696044.47300 |
| 98 | 2100 | 3 | 2 | 14 | 357806.94899 | 696123.00057 |
| 100 | 2600 | 4 | 2 | 3 | 357711.90600 | 696194.89050 |
| 101 | 2100 | 3 | 2 | 21 | 358993.50650 | 694971.21250 |
| 102 | 2200 | 3 | 2 | 51 | 359020.64600 | 694961.06000 |
| 103 | 2150 | 3 | 2 | 15 | 358984.49300 | 694946.76450 |
| 104 | 2500 | 4 | 2 | 25 | 359010.62353 | 694803.79530 |
| 105 | 2100 | 3 | 2 | 31 | 359079.27300 | 694917.75545 |
| 106 | 4400 | 3 | 2 | 54 | 359048.85050 | 694941.33250 |
| 107 | 2800 | 4 | 3 | 7 | 358950.11075 | 694994.72000 |
| 108 | 2600 | 4 | 2 | 29 | 358892.57250 | 694977.73950 |
| 109 | 2400 | 3 | 2 | 14 | 358887.19700 | 694933.91188 |
| 110 | 2200 | 3 | 2 | 16 | 358916.09300 | 695062.44750 |
| 111 | 2100 | 2 | 1 | 129 | 358924.99600 | 695130.25350 |
| 112 | 2400 | 4 | 2 | 3 | 358945.34900 | 695188.70800 |
| 113 | 2200 | 3 | 2 | 2 | 359018.28700 | 695084.79400 |
| 114 | 2100 | 4 | 2 | 24 | 358993.08150 | 695246.52720 |
| 116 | 7000 | 3 | 2 | 24 | 358883.21650 | 695117.52150 |

| | | | | | | |
|-----|------|---|---|-----|--------------|--------------|
| 117 | 2600 | 4 | 3 | 3 | 358847.85100 | 695159.63050 |
| 118 | 2000 | 4 | 3 | 19 | 358815.63150 | 695241.84768 |
| 119 | 2400 | 4 | 2 | 28 | 358750.13100 | 695279.26700 |
| 120 | 1700 | 3 | 2 | 24 | 358719.70879 | 695272.69798 |
| 121 | 2600 | 3 | 2 | 24 | 358579.37550 | 694920.55950 |
| 122 | 2400 | 4 | 2 | 9 | 358594.58400 | 694819.01500 |
| 123 | 2400 | 4 | 2 | 39 | 358577.76550 | 694778.14100 |
| 124 | 200 | 1 | 1 | 24 | 358576.64150 | 694745.59400 |
| 125 | 1000 | 2 | 1 | 14 | 358599.61000 | 694734.75550 |
| 126 | 1600 | 2 | 2 | 6 | 356640.55550 | 695435.72450 |
| 127 | 5000 | 3 | 2 | 9 | 356793.16050 | 695406.23150 |
| 128 | 1800 | 3 | 2 | 18 | 356928.89445 | 695445.17288 |
| 129 | 1600 | 2 | 1 | 19 | 356993.29300 | 695396.80000 |
| 130 | 1000 | 4 | 1 | 16 | 356971.01200 | 695477.33400 |
| 131 | 1900 | 3 | 2 | 49 | 357023.00909 | 695466.73600 |
| 132 | 2000 | 1 | 2 | 14 | 357087.58700 | 695442.90300 |
| 133 | 2100 | 4 | 2 | 26 | 357061.42450 | 695507.21150 |
| 134 | 2000 | 4 | 1 | 9 | 357051.68750 | 695540.89350 |
| 135 | 2100 | 3 | 2 | 17 | 357013.57483 | 695570.48600 |
| 136 | 1600 | 2 | 1 | 14 | 357199.70150 | 695551.48850 |
| 137 | 1800 | 3 | 2 | 40 | 357138.96900 | 695551.74500 |
| 138 | 1900 | 3 | 2 | 7 | 356335.22700 | 695502.42900 |
| 139 | 2000 | 3 | 1 | 54 | 356266.12040 | 695489.49400 |
| 140 | 1800 | 2 | 1 | 102 | 356221.78100 | 695543.23790 |
| 141 | 1700 | 3 | 1 | 4 | 356246.35000 | 695710.15700 |
| 142 | 1600 | 2 | 1 | 44 | 356210.28125 | 695734.31900 |
| 143 | 1900 | 3 | 1 | 2 | 356144.12550 | 695608.14150 |
| 144 | 1800 | 3 | 1 | 29 | 356029.48490 | 695539.01650 |
| 144 | 1600 | 2 | 1 | 14 | 356039.87350 | 695595.89600 |
| 145 | 1800 | 4 | 2 | 24 | 356094.16300 | 695715.10850 |
| 145 | 1800 | 4 | 2 | 2 | 356011.64115 | 695821.77500 |
| 146 | 1750 | 3 | 1 | 29 | 355919.75100 | 695760.72250 |
| 147 | 2000 | 3 | 1 | 22 | 355886.61840 | 695689.70450 |
| 148 | 2000 | 2 | 1 | 14 | 355793.93455 | 695632.46160 |
| 149 | 2100 | 2 | 1 | 5 | 359295.82550 | 694591.49150 |
| 150 | 1900 | 2 | 1 | 9 | 359327.69050 | 694573.32550 |
| 151 | 1200 | 3 | 2 | 9 | 359230.71950 | 694608.15625 |
| 152 | 1300 | 3 | 2 | 6 | 359423.67150 | 694567.93800 |
| 153 | 1600 | 3 | 1 | 13 | 359106.54000 | 694658.75850 |
| 154 | 1400 | 4 | 2 | 19 | 359261.75700 | 694695.24945 |
| 155 | 1350 | 4 | 2 | 29 | 359270.36625 | 694774.80250 |
| 156 | 1900 | 4 | 2 | 24 | 359202.09600 | 694797.14205 |
| 157 | 2100 | 3 | 2 | 24 | 359246.21600 | 694791.76550 |
| 158 | 2250 | 3 | 1 | 5 | 359187.98100 | 694783.80240 |
| 159 | 1896 | 3 | 2 | 15 | 359159.90425 | 694758.45200 |
| 160 | 1750 | 4 | 2 | 29 | 359147.17600 | 694803.73150 |
| 161 | 1500 | 3 | 3 | 24 | 359258.61700 | 694860.55750 |
| 162 | 2000 | 3 | 2 | 14 | 359237.69300 | 694869.46065 |
| 163 | 1950 | 4 | 2 | 10 | 359368.65900 | 694808.36750 |
| 164 | 1700 | 4 | 2 | 19 | 359421.44650 | 694790.29700 |
| 165 | 2500 | 3 | 2 | 14 | 359417.39350 | 694728.77800 |
| 166 | 2208 | 3 | 1 | 24 | 359483.13150 | 694794.18835 |
| 167 | 1950 | 3 | 2 | 24 | 359461.25875 | 694849.32915 |
| 168 | 1400 | 3 | 1 | 10 | 359334.36200 | 695064.66750 |
| 169 | 1520 | 3 | 2 | 24 | 359348.39110 | 695005.98610 |
| 170 | 1600 | 3 | 2 | 14 | 359361.70770 | 694949.40950 |
| 171 | 4500 | 4 | 3 | 14 | 359282.13350 | 695024.47275 |

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|-----|------|---|---|----|--------------|--------------|
| 172 | 1490 | 4 | 2 | 34 | 359230.61510 | 695033.33130 |
| 173 | 2150 | 3 | 1 | 24 | 359149.42965 | 695009.03850 |
| 174 | 2500 | 3 | 2 | 44 | 359887.58700 | 694693.39950 |
| 175 | 1820 | 3 | 2 | 19 | 360039.63915 | 694766.91050 |
| 176 | 1600 | 4 | 2 | 19 | 359939.32890 | 694801.24820 |
| 177 | 1200 | 3 | 2 | 14 | 360005.69160 | 694869.69790 |
| 178 | 1200 | 3 | 2 | 24 | 360082.24450 | 694833.10155 |
| 179 | 1300 | 3 | 2 | 32 | 360125.39145 | 695119.60865 |
| 180 | 1200 | 3 | 2 | 19 | 360131.23000 | 695203.37235 |
| 181 | 1600 | 2 | 2 | 8 | 359983.78270 | 695240.16000 |
| 183 | 1600 | 3 | 2 | 14 | 360061.22650 | 695075.04495 |
| 184 | 1600 | 4 | 2 | 16 | 359771.03600 | 695161.35760 |
| 185 | 8000 | 3 | 2 | 14 | 359775.72015 | 695089.37215 |
| 186 | 1400 | 4 | 2 | 6 | 359898.38720 | 695060.24790 |
| 187 | 1200 | 3 | 2 | 24 | 359930.63730 | 694981.77975 |
| 188 | 1100 | 3 | 2 | 14 | 359786.89540 | 694745.37250 |
| 190 | 1200 | 3 | 2 | 10 | 359719.71850 | 694795.90200 |
| 191 | 900 | 3 | 2 | 6 | 359764.58880 | 694962.40425 |
| 192 | 1600 | 3 | 2 | 9 | 359765.56400 | 695019.77950 |
| 193 | 1800 | 4 | 2 | 15 | 359822.59150 | 694961.68280 |
| 194 | 1600 | 2 | 2 | 22 | 359911.98365 | 695169.13765 |
| 195 | 1000 | 2 | 1 | 15 | 359750.42530 | 694588.79720 |
| 196 | 800 | 2 | 2 | 6 | 359731.34850 | 694539.31435 |
| 197 | 800 | 2 | 1 | 8 | 359828.34785 | 694523.25300 |
| 198 | 400 | 2 | 1 | 24 | 359895.50100 | 694555.83500 |
| 199 | 800 | 2 | 1 | 11 | 360097.67650 | 694700.25019 |
| 199 | 800 | 3 | 2 | 14 | 360287.01100 | 694677.17550 |
| 201 | 1600 | 2 | 2 | 24 | 360239.84850 | 694708.55000 |
| 202 | 1400 | 3 | 2 | 4 | 360202.47750 | 694819.82100 |
| 203 | 1600 | 3 | 1 | 4 | 360201.95150 | 694896.74200 |
| 204 | 1800 | 3 | 1 | 18 | 360302.89200 | 694888.23155 |
| 205 | 1200 | 4 | 3 | 14 | 360276.15250 | 694813.33610 |
| 206 | 1400 | 3 | 2 | 8 | 360405.76550 | 694804.10800 |
| 207 | 2000 | 3 | 3 | 8 | 360481.42055 | 694700.61465 |
| 208 | 1200 | 3 | 3 | 9 | 360601.31250 | 694731.34100 |
| 209 | 1800 | 2 | 1 | 11 | 360560.08850 | 695050.17630 |
| 210 | 1800 | 2 | 2 | 11 | 360489.77200 | 695145.33350 |
| 211 | 1400 | 3 | 2 | 27 | 360215.81850 | 695165.43950 |
| 212 | 1400 | 3 | 3 | 15 | 360300.20550 | 694641.47505 |
| 213 | 1600 | 2 | 1 | 18 | 360683.54150 | 694560.68785 |
| 214 | 1800 | 4 | 3 | 13 | 360777.90325 | 694577.76345 |
| 215 | 1600 | 2 | 2 | 22 | 360700.82255 | 694735.36250 |
| 216 | 2800 | 3 | 2 | 1 | 360797.82600 | 694880.81400 |
| 217 | 1600 | 3 | 2 | 12 | 360832.03000 | 694983.38700 |
| 218 | 1800 | 3 | 3 | 8 | 360920.18230 | 694920.14400 |
| 219 | 1600 | 2 | 1 | 16 | 360558.56050 | 694432.29550 |
| 220 | 1800 | 2 | 1 | 10 | 360615.06450 | 694517.15600 |
| 221 | 1200 | 2 | 1 | 16 | 360479.80910 | 694539.48460 |
| 222 | 800 | 2 | 1 | 9 | 360230.77300 | 694485.28135 |
| 223 | 1000 | 2 | 1 | 19 | 362715.52250 | 694587.01940 |
| 224 | 1000 | 4 | 2 | 14 | 362696.81300 | 694502.54160 |
| 226 | 1200 | 4 | 1 | 4 | 362685.91940 | 694630.61195 |
| 227 | 1400 | 4 | 3 | 8 | 362516.05105 | 694799.07650 |
| 228 | 1400 | 3 | 2 | 15 | 362379.53460 | 694520.90010 |
| 229 | 4800 | 4 | 2 | 14 | 362372.06850 | 694731.15850 |
| 230 | 1200 | 3 | 2 | 24 | 362303.81550 | 694756.05650 |
| 231 | 1200 | 3 | 1 | 4 | 362259.85350 | 694599.45100 |

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| 232 | 1400 | 3 | 2 | 9 | 362198.78200 | 694515.10800 |
| 233 | 800 | 2 | 2 | 24 | 362681.40925 | 694725.86750 |
| 234 | 1400 | 2 | 2 | 7 | 361941.06395 | 694573.88760 |
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| 237 | 1600 | 4 | 2 | 14 | 361781.67255 | 694772.83345 |
| 238 | 1400 | 3 | 2 | 3 | 361716.17050 | 694584.26300 |
| 239 | 1600 | 2 | 2 | 19 | 361548.77950 | 694663.11900 |
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| 242 | 1600 | 3 | 2 | 39 | 361099.77215 | 694541.73550 |
| 243 | 1600 | 4 | 3 | 17 | 361634.02150 | 694262.72050 |
| 246 | 1400 | 3 | 2 | 24 | 361692.99850 | 694966.89250 |
| 247 | 800 | 2 | 1 | 9 | 362180.44880 | 694581.59160 |
| 248 | 800 | 2 | 1 | 14 | 362003.97350 | 694566.37250 |
| 249 | 1000 | 2 | 1 | 9 | 361886.56650 | 694472.02350 |
| 250 | 1000 | 2 | 1 | 8 | 361865.30045 | 694389.05685 |
| 251 | 1200 | 2 | 1 | 36 | 359293.76640 | 695971.65180 |
| 253 | 2000 | 2 | 2 | 31 | 359257.53325 | 695982.79670 |
| 254 | 1100 | 2 | 1 | 11 | 359265.23100 | 695937.05350 |
| 255 | 1600 | 4 | 3 | 45 | 359248.99750 | 695930.52100 |
| 256 | 1000 | 4 | 2 | 31 | 359191.09250 | 695941.39600 |
| 257 | 1200 | 2 | 1 | 24 | 359276.51465 | 695872.52690 |
| 258 | 1200 | 4 | 2 | 26 | 359257.35650 | 695848.56275 |
| 259 | 1200 | 4 | 3 | 37 | 359324.42200 | 695866.40750 |
| 260 | 1500 | 4 | 2 | 36 | 359370.13526 | 695900.23425 |
| 261 | 1200 | 2 | 1 | 34 | 359382.37370 | 695909.35010 |
| 262 | 1200 | 2 | 1 | 23 | 359370.83020 | 695869.63165 |
| 263 | 1000 | 3 | 1 | 28 | 359399.45400 | 695894.09405 |
| 264 | 1000 | 3 | 1 | 40 | 359426.06550 | 695932.70400 |
| 265 | 1100 | 3 | 1 | 30 | 359404.99115 | 695816.40870 |
| 266 | 1000 | 2 | 1 | 28 | 359372.27600 | 695817.35000 |
| 267 | 1200 | 2 | 1 | 10 | 359227.72250 | 695820.36950 |
| 268 | 1200 | 2 | 2 | 14 | 359212.07400 | 695822.83345 |
| 269 | 1200 | 3 | 2 | 4 | 359185.41450 | 695780.61450 |
| 270 | 1000 | 3 | 2 | 24 | 359185.70700 | 695745.50445 |
| 271 | 936 | 2 | 2 | 2 | 359164.51695 | 695708.48030 |
| 272 | 1000 | 3 | 2 | 14 | 359243.19855 | 695615.44850 |
| 273 | 1000 | 2 | 2 | 24 | 359262.61700 | 695578.61500 |
| 274 | 600 | 1 | 1 | 41 | 359328.92900 | 695673.57085 |
| 275 | 1600 | 4 | 1 | 32 | 359412.57500 | 695677.53280 |
| 276 | 800 | 3 | 1 | 29 | 358953.45950 | 695621.94900 |
| 277 | 600 | 1 | 1 | 24 | 358937.53350 | 695655.12050 |
| 278 | 1296 | 2 | 1 | 20 | 358930.80760 | 695675.69600 |
| 279 | 900 | 2 | 1 | 17 | 358896.81095 | 695685.32000 |
| 280 | 1000 | 4 | 1 | 36 | 358842.30350 | 695654.32850 |
| 281 | 1000 | 3 | 1 | 34 | 358839.65230 | 695674.22500 |
| 282 | 500 | 2 | 1 | 14 | 358822.68000 | 695705.46500 |
| 283 | 1200 | 3 | 1 | 12 | 358785.88205 | 695821.60685 |
| 284 | 800 | 2 | 1 | 6 | 358776.92500 | 695781.63000 |
| 285 | 200 | 2 | 1 | 24 | 358775.58550 | 695691.56250 |
| 286 | 1200 | 3 | 2 | 31 | 358655.81130 | 695804.71900 |
| 287 | 1000 | 3 | 2 | 42 | 358668.44615 | 695775.35590 |
| 288 | 900 | 2 | 1 | 9 | 358672.71050 | 695762.94100 |
| 289 | 300 | 2 | 1 | 28 | 358737.99786 | 695706.61650 |
| 290 | 1000 | 3 | 2 | 5 | 358711.30560 | 695709.87400 |
| 291 | 300 | 2 | 1 | 14 | 358638.21720 | 695715.78050 |

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|-----|------|---|---|----|--------------|--------------|
| 292 | 1000 | 4 | 2 | 18 | 358757.30800 | 695646.92300 |
| 293 | 1500 | 4 | 1 | 69 | 358918.91480 | 695623.83350 |
| 294 | 500 | 2 | 1 | 19 | 358927.46450 | 695660.33600 |
| 295 | 700 | 2 | 1 | 7 | 358965.57150 | 695699.64235 |
| 296 | 200 | 1 | 1 | 29 | 359046.72380 | 695671.06070 |
| 297 | 1200 | 3 | 2 | 7 | 358841.73350 | 695635.95000 |
| 298 | 1100 | 3 | 2 | 14 | 358830.81225 | 695548.52160 |
| 299 | 1200 | 3 | 2 | 26 | 358929.07000 | 695744.40480 |
| 300 | 700 | 3 | 1 | 26 | 358988.33800 | 695680.02000 |
| 301 | 1000 | 3 | 1 | 22 | 362834.98900 | 693793.11450 |
| 302 | 1000 | 4 | 1 | 24 | 362933.15715 | 693799.84720 |
| 303 | 1600 | 4 | 1 | 24 | 362889.51975 | 693875.98695 |
| 304 | 800 | 2 | 1 | 4 | 362910.64220 | 693965.07030 |
| 305 | 500 | 2 | 1 | 2 | 362813.39475 | 694020.91645 |
| 306 | 1200 | 1 | 1 | 14 | 362734.80365 | 693959.74240 |
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| 308 | 800 | 2 | 1 | 17 | 363037.51825 | 694230.68935 |
| 309 | 500 | 1 | 1 | 24 | 363130.66480 | 694228.59105 |
| 310 | 1000 | 1 | 1 | 33 | 363036.89510 | 694200.22495 |
| 311 | 1000 | 2 | 1 | 10 | 363074.22410 | 694140.52190 |
| 312 | 300 | 1 | 1 | 14 | 363176.70400 | 694193.29315 |
| 313 | 500 | 1 | 1 | 8 | 363232.56505 | 694138.96500 |
| 314 | 400 | 1 | 1 | 4 | 362929.19795 | 694135.75465 |
| 315 | 700 | 1 | 1 | 24 | 362796.71180 | 694179.98865 |
| 316 | 1200 | 2 | 1 | 34 | 362834.05695 | 694182.00155 |
| 317 | 900 | 1 | 1 | 2 | 362570.61750 | 694217.43100 |
| 318 | 500 | 2 | 1 | 8 | 362550.19100 | 694190.97500 |
| 319 | 600 | 1 | 1 | 14 | 362557.81700 | 694142.74740 |
| 320 | 700 | 1 | 1 | 14 | 362509.15950 | 694110.16425 |
| 321 | 1200 | 2 | 1 | 19 | 362427.75500 | 694150.86605 |
| 322 | 1000 | 1 | 1 | 14 | 362438.98600 | 694094.99100 |
| 323 | 600 | 1 | 1 | 9 | 362434.22155 | 694013.71000 |
| 324 | 700 | 1 | 1 | 12 | 362361.77640 | 693998.30040 |
| 325 | 300 | 1 | 0 | 9 | 362390.31400 | 694026.80220 |
| 326 | 300 | 1 | 0 | 11 | 358913.48705 | 697352.05545 |
| 327 | 1000 | 1 | 1 | 23 | 358923.81500 | 697315.02880 |
| 328 | 600 | 1 | 1 | 17 | 358950.04200 | 697306.45100 |
| 329 | 600 | 2 | 1 | 6 | 359042.61550 | 697299.92350 |
| 330 | 900 | 2 | 1 | 48 | 359018.96200 | 697326.69000 |
| 331 | 1200 | 3 | 2 | 19 | 359027.29595 | 697249.16505 |
| 332 | 2000 | 4 | 3 | 7 | 358997.51100 | 697257.72150 |
| 333 | 1000 | 3 | 2 | 24 | 359020.03500 | 697537.26550 |
| 334 | 1400 | 4 | 2 | 6 | 359032.02495 | 697568.91050 |
| 336 | 800 | 2 | 1 | 14 | 359037.45800 | 697600.02200 |
| 337 | 200 | 1 | 1 | 9 | 359022.93050 | 697618.64850 |
| 338 | 800 | 3 | 1 | 34 | 359074.26700 | 697622.65450 |
| 339 | 500 | 2 | 1 | 5 | 359065.10550 | 697946.33600 |
| 340 | 300 | 2 | 1 | 26 | 359055.28250 | 697962.14850 |
| 341 | 6000 | 3 | 1 | 18 | 359046.83750 | 697954.79000 |
| 342 | 1200 | 3 | 2 | 26 | 359051.58815 | 698011.76150 |
| 343 | 800 | 3 | 2 | 24 | 359062.80450 | 698046.69500 |
| 344 | 600 | 2 | 1 | 19 | 359032.15250 | 698000.04450 |
| 345 | 1000 | 2 | 2 | 22 | 359043.59300 | 698254.91950 |
| 346 | 1250 | 3 | 2 | 8 | 359009.50650 | 698264.64400 |
| 347 | 1200 | 2 | 2 | 10 | 359031.36295 | 698312.43800 |
| 348 | 1800 | 2 | 1 | 16 | 358979.08006 | 698309.42740 |
| 349 | 500 | 2 | 1 | 3 | 358940.21200 | 698374.11450 |

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|-----|------|---|---|----|--------------|--------------|
| 350 | 4000 | 2 | 1 | 14 | 358961.72820 | 698398.98655 |
| 351 | 400 | 2 | 1 | 12 | 357469.82450 | 696196.02343 |
| 352 | 700 | 2 | 1 | 18 | 357519.18050 | 696135.67450 |
| 353 | 900 | 3 | 1 | 3 | 357446.84250 | 696133.11550 |
| 354 | 1200 | 3 | 1 | 13 | 357455.65626 | 696110.33197 |
| 356 | 1000 | 3 | 1 | 39 | 357488.45073 | 696014.71500 |
| 357 | 1080 | 4 | 3 | 18 | 357522.21150 | 695870.11200 |
| 358 | 600 | 2 | 1 | 13 | 357472.95555 | 695904.17275 |
| 359 | 800 | 2 | 1 | 14 | 357464.03653 | 695766.46100 |
| 360 | 800 | 3 | 2 | 15 | 357448.81200 | 695749.51950 |
| 361 | 800 | 3 | 1 | 5 | 357400.38819 | 695742.58650 |
| 362 | 400 | 2 | 1 | 12 | 357329.31950 | 695746.37950 |
| 363 | 800 | 2 | 1 | 32 | 357407.38694 | 695716.08795 |
| 364 | 1500 | 1 | 1 | 16 | 357300.48450 | 695482.17250 |
| 365 | 800 | 3 | 2 | 11 | 357322.53522 | 695449.94900 |
| 366 | 800 | 2 | 2 | 22 | 357283.26450 | 695446.73800 |
| 367 | 700 | 3 | 1 | 59 | 357335.15179 | 695443.90000 |
| 368 | 600 | 2 | 1 | 7 | 357355.05905 | 695189.03600 |
| 369 | 600 | 1 | 1 | 4 | 357322.76190 | 695189.57620 |
| 370 | 300 | 1 | 1 | 44 | 357301.47645 | 695140.60260 |
| 371 | 400 | 2 | 1 | 12 | 357339.44390 | 695097.79305 |
| 372 | 400 | 1 | 1 | 14 | 357590.67505 | 695061.42300 |
| 373 | 600 | 3 | 1 | 14 | 357653.67000 | 695000.33350 |
| 374 | 500 | 3 | 1 | 9 | 357602.16900 | 695022.86200 |
| 375 | 800 | 3 | 1 | 14 | 357651.23300 | 694975.01500 |
| 376 | 1440 | 3 | 1 | 14 | 358553.27760 | 698194.38060 |
| 377 | 1000 | 2 | 1 | 6 | 358529.10545 | 698212.10360 |
| 378 | 720 | 1 | 1 | 19 | 358134.31005 | 697776.45430 |
| 379 | 1080 | 2 | 1 | 14 | 358318.32300 | 697930.94160 |
| 380 | 1440 | 2 | 1 | 14 | 358325.61400 | 697925.56850 |
| 381 | 540 | 2 | 1 | 6 | 358520.92240 | 698216.25470 |
| 382 | 1800 | 3 | 1 | 10 | 358606.68970 | 698355.63965 |
| 383 | 1800 | 3 | 1 | 13 | 358638.50680 | 698344.55195 |
| 384 | 900 | 2 | 1 | 9 | 358632.54000 | 698358.33545 |
| 385 | 1260 | 2 | 1 | 8 | 358533.38150 | 698364.21200 |
| 386 | 1260 | 2 | 2 | 19 | 358532.37000 | 698350.65700 |
| 387 | 1000 | 1 | 1 | 6 | 358545.94750 | 698360.39300 |
| 388 | 540 | 1 | 1 | 9 | 358555.24150 | 698366.27700 |
| 389 | 540 | 1 | 1 | 9 | 358563.55250 | 698351.22650 |
| 390 | 1260 | 2 | 1 | 24 | 358557.14800 | 698340.24450 |
| 391 | 1980 | 2 | 1 | 6 | 358489.03600 | 698369.17050 |
| 392 | 1440 | 2 | 1 | 6 | 358462.03850 | 698351.40550 |
| 393 | 2160 | 4 | 1 | 9 | 358390.09140 | 698411.31700 |
| 394 | 1440 | 3 | 1 | 13 | 358385.92565 | 698422.17895 |
| 395 | 1080 | 2 | 1 | 17 | 358375.81180 | 698423.83680 |
| 396 | 1260 | 2 | 1 | 6 | 357177.87850 | 697126.57600 |
| 397 | 1440 | 2 | 1 | 14 | 357245.79540 | 697007.78040 |
| 398 | 1400 | 2 | 1 | 9 | 357216.83615 | 696978.31740 |
| 399 | 1440 | 3 | 1 | 11 | 357156.63365 | 696987.15500 |
| 400 | 1400 | 2 | 1 | 21 | 357216.76750 | 697204.87950 |
| 401 | 1400 | 2 | 1 | 4 | 357236.61720 | 697256.96420 |
| 402 | 1440 | 2 | 1 | 10 | 357231.21920 | 697278.81865 |
| 403 | 1440 | 2 | 1 | 19 | 357220.78220 | 697322.49875 |
| 404 | 1260 | 3 | 1 | 8 | 357189.93940 | 697148.76950 |
| 405 | 1350 | 2 | 1 | 24 | 357205.07525 | 696980.30875 |
| 406 | 1440 | 2 | 1 | 16 | 357191.09335 | 696966.38620 |
| 407 | 1500 | 3 | 1 | 10 | 357206.52995 | 697154.02870 |

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| 408 | 1440 | 2 | 1 | 22 | 357191.10500 | 696995.50755 |
| 409 | 720 | 1 | 1 | 3 | 357283.05620 | 697301.98820 |
| 410 | 1260 | 2 | 1 | 12 | 357229.25150 | 696971.39980 |
| 411 | 2400 | 4 | 2 | 19 | 357773.52500 | 696962.48520 |
| 412 | 3000 | 4 | 3 | 19 | 357813.19850 | 696935.03900 |
| 413 | 720 | 1 | 1 | 13 | 357808.17500 | 696861.58600 |
| 414 | 2400 | 3 | 1 | 16 | 357808.36550 | 696849.64840 |
| 416 | 600 | 1 | 1 | 11 | 359573.22465 | 699428.28285 |
| 417 | 720 | 2 | 1 | 2 | 359573.65540 | 699439.77190 |
| 418 | 1500 | 2 | 1 | 14 | 359591.73625 | 699420.27235 |
| 419 | 1800 | 2 | 1 | 14 | 359598.03485 | 699429.65305 |
| 420 | 1440 | 3 | 1 | 9 | 359556.83490 | 699384.05520 |
| 421 | 1080 | 2 | 1 | 9 | 359549.58070 | 699352.48665 |
| 422 | 1440 | 2 | 1 | 13 | 359602.32630 | 699331.20405 |
| 423 | 1440 | 2 | 1 | 19 | 359609.45990 | 699335.72280 |
| 424 | 1080 | 2 | 2 | 4 | 359152.59250 | 699144.38000 |
| 425 | 1080 | 2 | 1 | 4 | 359536.84810 | 699031.29835 |
| 426 | 1440 | 2 | 2 | 14 | 359119.16290 | 699120.49050 |
| 427 | 1440 | 2 | 2 | 14 | 359129.35915 | 699113.11425 |
| 428 | 1440 | 3 | 2 | 10 | 359140.51175 | 699083.84825 |
| 429 | 1800 | 2 | 1 | 14 | 359141.25910 | 699060.37220 |
| 430 | 1850 | 2 | 1 | 18 | 359172.16710 | 699102.13900 |
| 431 | 2000 | 2 | 1 | 14 | 359194.18350 | 699045.52300 |
| 432 | 1800 | 2 | 2 | 19 | 359651.44475 | 699605.49875 |
| 433 | 1620 | 2 | 1 | 3 | 359623.74580 | 699575.78235 |
| 434 | 1620 | 2 | 1 | 18 | 359608.87968 | 699607.57723 |
| 435 | 1440 | 3 | 2 | 14 | 359549.70825 | 699477.80490 |
| 436 | 3600 | 3 | 1 | 14 | 359487.58050 | 696637.10550 |
| 437 | 1200 | 2 | 1 | 14 | 359485.09975 | 696646.68475 |
| 438 | 720 | 1 | 1 | 7 | 359359.22950 | 696609.06800 |
| 439 | 1440 | 1 | 1 | 6 | 359706.72750 | 697507.33700 |
| 440 | 1440 | 2 | 1 | 9 | 360099.49500 | 697203.29950 |
| 441 | 1440 | 2 | 1 | 5 | 360073.66000 | 697192.73750 |
| 442 | 1440 | 3 | 1 | 14 | 359820.08490 | 697217.67100 |
| 443 | 2340 | 2 | 1 | 12 | 359712.52650 | 697226.52050 |
| 444 | 3960 | 3 | 2 | 8 | 359716.07400 | 697240.87000 |
| 445 | 3960 | 4 | 2 | 6 | 359574.25820 | 697246.04510 |
| 446 | 3600 | 3 | 3 | 14 | 359696.77150 | 697270.95220 |
| 447 | 1800 | 3 | 2 | 24 | 359580.99000 | 697121.34300 |
| 448 | 2520 | 3 | 1 | 9 | 359594.94650 | 697074.65350 |
| 449 | 1440 | 3 | 1 | 3 | 359612.57550 | 697069.45000 |
| 450 | 1800 | 3 | 1 | 4 | 359647.93600 | 697060.54950 |
| 451 | 1800 | 2 | 1 | 6 | 359677.51995 | 697073.76150 |
| 452 | 2160 | 3 | 1 | 6 | 359666.36630 | 697074.48800 |
| 453 | 1440 | 2 | 1 | 12 | 359617.26800 | 697513.65700 |
| 454 | 1440 | 2 | 1 | 14 | 359629.71900 | 697512.10900 |
| 455 | 1440 | 1 | 1 | 14 | 359726.86600 | 697481.53650 |
| 456 | 1080 | 3 | 1 | 19 | 358702.02335 | 696721.05920 |
| 457 | 1440 | 4 | 2 | 8 | 358938.39600 | 696886.40700 |
| 458 | 720 | 2 | 1 | 19 | 358802.69620 | 696752.06700 |
| 459 | 700 | 1 | 1 | 19 | 358814.40500 | 696749.07350 |
| 460 | 700 | 1 | 1 | 9 | 358803.73220 | 696734.87335 |
| 461 | 500 | 1 | 1 | 24 | 358805.73495 | 696782.95900 |
| 462 | 1800 | 3 | 1 | 18 | 358956.49600 | 696923.72200 |
| 463 | 500 | 1 | 1 | 6 | 358848.16619 | 697014.31500 |
| 464 | 1440 | 3 | 1 | 18 | 358764.49480 | 697029.49790 |
| 465 | 1440 | 3 | 1 | 13 | 358912.99650 | 697028.65570 |

| | | | | | | |
|-----|------|---|---|----|--------------|--------------|
| 466 | 1080 | 2 | 1 | 24 | 358910.96600 | 696956.95700 |
| 467 | 1440 | 2 | 1 | 16 | 358909.99175 | 696911.92300 |
| 468 | 4320 | 4 | 3 | 23 | 358894.55450 | 696892.59650 |
| 469 | 720 | 2 | 1 | 6 | 358898.65550 | 696906.77300 |
| 470 | 1300 | 4 | 2 | 12 | 358911.30750 | 696947.42585 |
| 471 | 1080 | 4 | 1 | 12 | 358818.29750 | 697079.59950 |
| 472 | 1440 | 3 | 1 | 35 | 358914.34600 | 696889.44815 |
| 473 | 2160 | 2 | 1 | 8 | 358742.51870 | 696992.45760 |
| 474 | 2880 | 1 | 1 | 42 | 358754.00810 | 696972.50025 |
| 475 | 1800 | 3 | 1 | 15 | 358733.10285 | 696944.79970 |
| 476 | 720 | 2 | 1 | 9 | 356079.17700 | 696238.83035 |
| 477 | 1080 | 2 | 1 | 10 | 356081.51200 | 696247.93620 |
| 478 | 720 | 2 | 1 | 9 | 356058.85600 | 696245.64350 |
| 479 | 1800 | 3 | 1 | 14 | 356077.25545 | 696165.47200 |
| 480 | 1440 | 4 | 2 | 5 | 356095.29800 | 696139.93535 |
| 481 | 1440 | 2 | 1 | 19 | 355902.60700 | 696271.73900 |
| 482 | 2160 | 3 | 1 | 9 | 355908.17750 | 696339.80450 |
| 483 | 2880 | 3 | 1 | 19 | 355825.34150 | 696249.58850 |
| 485 | 2160 | 3 | 2 | 9 | 355599.24573 | 696228.97000 |
| 486 | 1440 | 3 | 1 | 29 | 355492.62090 | 696277.02855 |
| 487 | 2160 | 3 | 1 | 24 | 355504.17740 | 696286.90900 |
| 488 | 1800 | 2 | 2 | 7 | 355630.52850 | 696520.20250 |
| 489 | 3000 | 3 | 2 | 24 | 355624.08150 | 696480.82800 |
| 489 | 1440 | 2 | 1 | 18 | 355587.95225 | 696397.46120 |
| 490 | 1440 | 4 | 2 | 10 | 355553.87070 | 696383.60750 |
| 491 | 2700 | 2 | 1 | 15 | 356400.65850 | 696640.78600 |
| 492 | 1400 | 4 | 3 | 6 | 356755.08700 | 696835.68050 |
| 493 | 800 | 2 | 1 | 29 | 356739.65575 | 696559.89630 |
| 494 | 1500 | 2 | 1 | 9 | 356750.66150 | 696726.60150 |
| 495 | 1860 | 3 | 2 | 9 | 356423.02955 | 696763.46250 |

Table: Neighborhood Attributes

| HOUSE ID | RES LUSE | COM LUSE | COMMU LU | DRAINAGE |
|----------|----------|----------|----------|----------|
| 1 | 43.83 | 7.69 | 3.15 | 10.315 |
| 2 | 43.83 | 7.69 | 3.15 | 9.13 |
| 3 | 43.83 | 7.69 | 3.15 | 12.016 |
| 4 | 43.83 | 7.69 | 3.15 | 25.048 |
| 5 | 43.83 | 7.69 | 3.15 | 4.379 |
| 6 | 43.83 | 7.69 | 3.15 | 78.413 |
| 7 | 43.83 | 7.69 | 3.15 | 14.293 |
| 8 | 43.83 | 7.69 | 3.15 | 6.176 |
| 9 | 43.83 | 7.69 | 3.15 | 10.834 |
| 10 | 43.83 | 7.69 | 3.15 | 10.946 |
| 11 | 43.83 | 7.69 | 3.15 | 12.021 |
| 12 | 43.83 | 7.69 | 3.15 | 7.734 |
| 13 | 43.83 | 7.69 | 3.15 | 14.922 |
| 14 | 43.83 | 7.69 | 3.15 | 15.672 |
| 15 | 43.83 | 7.69 | 3.15 | 11.294 |
| 16 | 43.83 | 7.69 | 3.15 | 133.006 |
| 17 | 43.83 | 7.69 | 3.15 | 5.056 |
| 18 | 43.83 | 7.69 | 3.15 | 7.655 |
| 19 | 43.83 | 7.69 | 3.15 | 8.869 |
| 20 | 43.83 | 7.69 | 3.15 | 64.005 |
| 21 | 43.83 | 7.69 | 3.15 | 26.247 |
| 22 | 43.83 | 7.69 | 3.15 | 6.869 |
| 23 | 43.83 | 7.69 | 3.15 | 53.163 |
| 25 | 43.83 | 7.69 | 3.15 | 19.717 |
| 26 | 45.35 | 8.63 | 5.31 | 4.473 |
| 27 | 45.35 | 8.63 | 5.31 | 7.627 |
| 28 | 45.35 | 8.63 | 5.31 | 41.133 |
| 29 | 45.35 | 8.63 | 5.31 | 17.918 |
| 30 | 45.35 | 8.63 | 5.31 | 21.429 |
| 31 | 45.35 | 8.63 | 5.31 | 11.249 |
| 32 | 45.35 | 8.63 | 5.31 | 4.714 |
| 33 | 45.35 | 8.63 | 5.31 | 11.435 |
| 34 | 45.35 | 8.63 | 5.31 | 8.503 |
| 35 | 45.35 | 8.63 | 5.31 | 5.448 |
| 36 | 45.35 | 8.63 | 5.31 | 17.171 |
| 37 | 45.35 | 8.63 | 5.31 | 10.823 |
| 38 | 45.35 | 8.63 | 5.31 | 35.588 |
| 39 | 45.35 | 8.63 | 5.31 | 4.735 |
| 40 | 45.35 | 8.63 | 5.31 | 7.94 |
| 41 | 45.35 | 8.63 | 5.31 | 4.989 |
| 42 | 45.35 | 8.63 | 5.31 | 15.82 |
| 43 | 45.35 | 8.63 | 5.31 | 12.634 |
| 44 | 45.35 | 8.63 | 5.31 | 10.326 |
| 45 | 45.35 | 8.63 | 5.31 | 14.863 |
| 46 | 45.35 | 8.63 | 5.31 | 6.542 |
| 47 | 45.35 | 8.63 | 5.31 | 6.362 |
| 48 | 45.35 | 8.63 | 5.31 | 19.895 |
| 49 | 45.35 | 8.63 | 5.31 | 12.744 |
| 50 | 45.35 | 8.63 | 5.31 | 5.771 |
| 51 | 43.83 | 7.69 | 3.15 | 9.05 |
| 52 | 43.83 | 7.69 | 3.15 | 35.263 |

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|-----|-------|------|------|--------|
| 53 | 43.83 | 7.69 | 3.15 | 16.063 |
| 54 | 43.83 | 7.69 | 3.15 | 7.885 |
| 55 | 43.83 | 7.69 | 3.15 | 8.404 |
| 56 | 43.83 | 7.69 | 3.15 | 5.617 |
| 57 | 43.83 | 7.69 | 3.15 | 17.525 |
| 58 | 43.83 | 7.69 | 3.15 | 9.8 |
| 59 | 43.83 | 7.69 | 3.15 | 17.561 |
| 60 | 43.83 | 7.69 | 3.15 | 52.453 |
| 61 | 43.83 | 7.69 | 3.15 | 62.387 |
| 62 | 43.83 | 7.69 | 3.15 | 13.553 |
| 63 | 43.83 | 7.69 | 3.15 | 3.345 |
| 64 | 43.83 | 7.69 | 3.15 | 26.844 |
| 65 | 43.83 | 7.69 | 3.15 | 11.619 |
| 66 | 43.83 | 7.69 | 3.15 | 7.151 |
| 67 | 43.83 | 7.69 | 3.15 | 11.775 |
| 68 | 43.83 | 7.69 | 3.15 | 30.512 |
| 69 | 43.83 | 7.69 | 3.15 | 8.926 |
| 70 | 43.83 | 7.69 | 3.15 | 5.028 |
| 72 | 43.83 | 7.69 | 3.15 | 6.612 |
| 73 | 43.83 | 7.69 | 3.15 | 4.332 |
| 74 | 43.83 | 7.69 | 3.15 | 9.721 |
| 75 | 43.83 | 7.69 | 3.15 | 6.054 |
| 81 | 45.35 | 8.63 | 5.31 | 4.265 |
| 82 | 45.35 | 8.63 | 5.31 | 21.144 |
| 83 | 45.35 | 8.63 | 5.31 | 12.091 |
| 84 | 45.35 | 8.63 | 5.31 | 10.91 |
| 85 | 45.35 | 8.63 | 5.31 | 3.268 |
| 86 | 45.35 | 8.63 | 5.31 | 4.661 |
| 87 | 45.35 | 8.63 | 5.31 | 11.16 |
| 88 | 45.35 | 8.63 | 5.31 | 8.506 |
| 89 | 45.35 | 8.63 | 5.31 | 4.204 |
| 90 | 45.35 | 8.63 | 5.31 | 16.333 |
| 91 | 45.35 | 8.63 | 5.31 | 17.047 |
| 92 | 45.35 | 8.63 | 5.31 | 7.113 |
| 93 | 45.35 | 8.63 | 5.31 | 6.048 |
| 94 | 45.35 | 8.63 | 5.31 | 7.673 |
| 95 | 45.35 | 8.63 | 5.31 | 7.056 |
| 96 | 45.35 | 8.63 | 5.31 | 8.168 |
| 97 | 45.35 | 8.63 | 5.31 | 26.668 |
| 98 | 45.35 | 8.63 | 5.31 | 14.309 |
| 100 | 45.35 | 8.63 | 5.31 | 29.159 |
| 101 | 43.83 | 7.69 | 3.15 | 36.131 |
| 102 | 43.83 | 7.69 | 3.15 | 64.846 |
| 103 | 43.83 | 7.69 | 3.15 | 40.666 |
| 104 | 43.83 | 7.69 | 3.15 | 19.814 |
| 105 | 43.83 | 7.69 | 3.15 | 13.463 |
| 106 | 43.83 | 7.69 | 3.15 | 47.364 |
| 107 | 43.83 | 7.69 | 3.15 | 12.641 |
| 108 | 43.83 | 7.69 | 3.15 | 14.44 |
| 109 | 43.83 | 7.69 | 3.15 | 7.428 |
| 110 | 43.83 | 7.69 | 3.15 | 6.511 |
| 111 | 43.83 | 7.69 | 3.15 | 7.357 |
| 112 | 43.83 | 7.69 | 3.15 | 6.978 |
| 113 | 43.83 | 7.69 | 3.15 | 8.107 |

| | | | | |
|-----|-------|------|------|--------|
| 114 | 43.83 | 7.69 | 3.15 | 12.41 |
| 116 | 43.83 | 7.69 | 3.15 | 4.081 |
| 117 | 43.83 | 7.69 | 3.15 | 7.758 |
| 118 | 43.83 | 7.69 | 3.15 | 7.617 |
| 119 | 43.83 | 7.69 | 3.15 | 7.977 |
| 120 | 43.83 | 7.69 | 3.15 | 16.121 |
| 121 | 43.83 | 7.69 | 3.15 | 4.319 |
| 122 | 43.83 | 7.69 | 3.15 | 11.317 |
| 123 | 43.83 | 7.69 | 3.15 | 9.784 |
| 124 | 43.83 | 7.69 | 3.15 | 16.77 |
| 125 | 43.83 | 7.69 | 3.15 | 16.111 |
| 126 | 45.35 | 8.63 | 5.31 | 13.417 |
| 127 | 45.35 | 8.63 | 5.31 | 14.449 |
| 128 | 45.35 | 8.63 | 5.31 | 18.287 |
| 129 | 45.35 | 8.63 | 5.31 | 46.802 |
| 130 | 45.35 | 8.63 | 5.31 | 6.826 |
| 131 | 45.35 | 8.63 | 5.31 | 11.839 |
| 132 | 45.35 | 8.63 | 5.31 | 9.838 |
| 133 | 45.35 | 8.63 | 5.31 | 8.182 |
| 134 | 45.35 | 8.63 | 5.31 | 7.22 |
| 135 | 45.35 | 8.63 | 5.31 | 10.876 |
| 136 | 45.35 | 8.63 | 5.31 | 8.921 |
| 137 | 45.35 | 8.63 | 5.31 | 21.027 |
| 138 | 45.35 | 8.63 | 5.31 | 28.264 |
| 139 | 45.35 | 8.63 | 5.31 | 10.673 |
| 140 | 45.35 | 8.63 | 5.31 | 10.91 |
| 141 | 45.35 | 8.63 | 5.31 | 10.081 |
| 142 | 45.35 | 8.63 | 5.31 | 8.624 |
| 143 | 45.35 | 8.63 | 5.31 | 12.359 |
| 144 | 45.35 | 8.63 | 5.31 | 15.593 |
| 144 | 28.41 | 3.54 | 1.03 | 8.782 |
| 145 | 45.35 | 8.63 | 5.31 | 9.151 |
| 145 | 28.41 | 3.54 | 1.03 | 11.121 |
| 146 | 45.35 | 8.63 | 5.31 | 14.032 |
| 147 | 45.35 | 8.63 | 5.31 | 10.517 |
| 148 | 45.35 | 8.63 | 5.31 | 5.732 |
| 149 | 45.35 | 8.63 | 5.31 | 57.903 |
| 150 | 45.35 | 8.63 | 5.31 | 60.969 |
| 151 | 43.83 | 7.69 | 3.15 | 51.027 |
| 152 | 43.83 | 7.69 | 3.15 | 75.049 |
| 153 | 43.83 | 7.69 | 3.15 | 33.122 |
| 154 | 43.83 | 7.69 | 3.15 | 12.8 |
| 155 | 43.83 | 7.69 | 3.15 | 6.651 |
| 156 | 43.83 | 7.69 | 3.15 | 22.137 |
| 157 | 43.83 | 7.69 | 3.15 | 34.432 |
| 158 | 43.83 | 7.69 | 3.15 | 7.571 |
| 159 | 43.83 | 7.69 | 3.15 | 9.211 |
| 160 | 43.83 | 7.69 | 3.15 | 10.269 |
| 161 | 43.83 | 7.69 | 3.15 | 9.057 |
| 162 | 43.83 | 7.69 | 3.15 | 10.862 |
| 163 | 43.83 | 7.69 | 3.15 | 9.261 |
| 164 | 43.83 | 7.69 | 3.15 | 5.502 |
| 165 | 43.83 | 7.69 | 3.15 | 4.494 |
| 166 | 43.83 | 7.69 | 3.15 | 10.719 |

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|-----|-------|------|------|--------|
| 167 | 43.83 | 7.69 | 3.15 | 8.552 |
| 168 | 43.83 | 7.69 | 3.15 | 5.076 |
| 169 | 43.83 | 7.69 | 3.15 | 8.326 |
| 170 | 43.83 | 7.69 | 3.15 | 9.721 |
| 171 | 43.83 | 7.69 | 3.15 | 5.555 |
| 172 | 43.83 | 7.69 | 3.15 | 9.068 |
| 173 | 43.83 | 7.69 | 3.15 | 32.312 |
| 174 | 43.83 | 7.69 | 3.15 | 4.907 |
| 175 | 43.83 | 7.69 | 3.15 | 13.81 |
| 176 | 43.83 | 7.69 | 3.15 | 13.291 |
| 177 | 43.83 | 7.69 | 3.15 | 7.873 |
| 178 | 43.83 | 7.69 | 3.15 | 6.629 |
| 179 | 43.83 | 7.69 | 3.15 | 17.35 |
| 180 | 43.83 | 7.69 | 3.15 | 10.41 |
| 181 | 43.83 | 7.69 | 3.15 | 24.312 |
| 183 | 43.83 | 7.69 | 3.15 | 12.572 |
| 184 | 43.83 | 7.69 | 3.15 | 10.223 |
| 185 | 43.83 | 7.69 | 3.15 | 11.217 |
| 186 | 43.83 | 7.69 | 3.15 | 61.032 |
| 187 | 43.83 | 7.69 | 3.15 | 6.88 |
| 188 | 43.83 | 7.69 | 3.15 | 11.943 |
| 190 | 43.83 | 7.69 | 3.15 | 1.267 |
| 191 | 43.83 | 7.69 | 3.15 | 14.652 |
| 192 | 43.83 | 7.69 | 3.15 | 8.324 |
| 193 | 43.83 | 7.69 | 3.15 | 72.223 |
| 194 | 43.83 | 7.69 | 3.15 | 43.803 |
| 195 | 43.83 | 7.69 | 3.15 | 46.763 |
| 196 | 43.83 | 7.69 | 3.15 | 75.565 |
| 197 | 43.83 | 7.69 | 3.15 | 7.069 |
| 198 | 43.83 | 7.69 | 3.15 | 17.872 |
| 199 | 43.83 | 7.69 | 3.15 | 11.62 |
| 199 | 43.83 | 7.69 | 3.15 | 9.428 |
| 201 | 43.83 | 7.69 | 3.15 | 19.156 |
| 202 | 43.83 | 7.69 | 3.15 | 4.107 |
| 203 | 43.83 | 7.69 | 3.15 | 9.115 |
| 204 | 43.83 | 7.69 | 3.15 | 6.948 |
| 205 | 43.83 | 7.69 | 3.15 | 11.671 |
| 206 | 43.83 | 7.69 | 3.15 | 7.688 |
| 207 | 43.83 | 7.69 | 3.15 | 7.836 |
| 208 | 43.83 | 7.69 | 3.15 | 75.004 |
| 209 | 43.83 | 7.69 | 3.15 | 14.57 |
| 210 | 43.83 | 7.69 | 3.15 | 17.025 |
| 211 | 43.83 | 7.69 | 3.15 | 32.226 |
| 212 | 43.83 | 7.69 | 3.15 | 9.708 |
| 213 | 43.83 | 7.69 | 3.15 | 2.513 |
| 214 | 43.83 | 7.69 | 3.15 | 15.673 |
| 215 | 43.83 | 7.69 | 3.15 | 5.545 |
| 216 | 43.83 | 7.69 | 3.15 | 19.9 |
| 217 | 43.83 | 7.69 | 3.15 | 9.691 |
| 218 | 43.83 | 7.69 | 3.15 | 22.45 |
| 219 | 43.83 | 7.69 | 3.15 | 33.907 |
| 220 | 43.83 | 7.69 | 3.15 | 42.024 |
| 221 | 43.83 | 7.69 | 3.15 | 7.825 |
| 222 | 43.83 | 7.69 | 3.15 | 57.721 |

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|-----|-------|------|------|---------|
| 223 | 43.83 | 7.69 | 3.15 | 236.491 |
| 224 | 43.83 | 7.69 | 3.15 | 281.111 |
| 226 | 28.41 | 3.54 | 1.03 | 262.564 |
| 227 | 28.41 | 3.54 | 1.03 | 356.037 |
| 228 | 28.41 | 3.54 | 1.03 | 255.564 |
| 229 | 28.41 | 3.54 | 1.03 | 362.385 |
| 230 | 28.41 | 3.54 | 1.03 | 296.129 |
| 231 | 28.41 | 3.54 | 1.03 | 256.474 |
| 232 | 28.41 | 3.54 | 1.03 | 165.3 |
| 233 | 28.41 | 3.54 | 1.03 | 284.318 |
| 234 | 28.41 | 3.54 | 1.03 | 5.178 |
| 235 | 28.41 | 3.54 | 1.03 | 235.681 |
| 236 | 28.41 | 3.54 | 1.03 | 284.327 |
| 237 | 28.41 | 3.54 | 1.03 | 14.412 |
| 238 | 28.41 | 3.54 | 1.03 | 12.135 |
| 239 | 28.41 | 3.54 | 1.03 | 8.048 |
| 240 | 28.41 | 3.54 | 1.03 | 6.763 |
| 241 | 28.41 | 3.54 | 1.03 | 19.305 |
| 242 | 28.41 | 3.54 | 1.03 | 36.67 |
| 243 | 28.41 | 3.54 | 1.03 | 46.323 |
| 246 | 28.41 | 3.54 | 1.03 | 11.481 |
| 247 | 28.41 | 3.54 | 1.03 | 181.218 |
| 248 | 28.41 | 3.54 | 1.03 | 34.281 |
| 249 | 28.41 | 3.54 | 1.03 | 101.691 |
| 250 | 28.41 | 3.54 | 1.03 | 142.582 |
| 251 | 43.83 | 7.69 | 3.15 | 16.252 |
| 253 | 43.83 | 7.69 | 3.15 | 18.772 |
| 254 | 43.83 | 7.69 | 3.15 | 8.658 |
| 255 | 43.83 | 7.69 | 3.15 | 8.35 |
| 256 | 43.83 | 7.69 | 3.15 | 11.814 |
| 257 | 43.83 | 7.69 | 3.15 | 12.559 |
| 258 | 43.83 | 7.69 | 3.15 | 26.321 |
| 259 | 43.83 | 7.69 | 3.15 | 21.468 |
| 260 | 43.83 | 7.69 | 3.15 | 16.125 |
| 261 | 43.83 | 7.69 | 3.15 | 27.69 |
| 262 | 43.83 | 7.69 | 3.15 | 12.111 |
| 263 | 43.83 | 7.69 | 3.15 | 25.21 |
| 264 | 43.83 | 7.69 | 3.15 | 61.699 |
| 265 | 43.83 | 7.69 | 3.15 | 6.333 |
| 266 | 43.83 | 7.69 | 3.15 | 28.256 |
| 267 | 43.83 | 7.69 | 3.15 | 38.122 |
| 268 | 43.83 | 7.69 | 3.15 | 46.122 |
| 269 | 43.83 | 7.69 | 3.15 | 25.039 |
| 270 | 43.83 | 7.69 | 3.15 | 5.822 |
| 271 | 43.83 | 7.69 | 3.15 | 8.297 |
| 272 | 43.83 | 7.69 | 3.15 | 14.232 |
| 273 | 43.83 | 7.69 | 3.15 | 9.363 |
| 274 | 43.83 | 7.69 | 3.15 | 22.517 |
| 275 | 43.83 | 7.69 | 3.15 | 9.53 |
| 276 | 43.83 | 7.69 | 3.15 | 9.714 |
| 277 | 43.83 | 7.69 | 3.15 | 5.675 |
| 278 | 43.83 | 7.69 | 3.15 | 9.362 |
| 279 | 43.83 | 7.69 | 3.15 | 5.59 |
| 280 | 43.83 | 7.69 | 3.15 | 9.185 |

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|-----|-------|------|------|---------|
| 281 | 43.83 | 7.69 | 3.15 | 10.475 |
| 282 | 43.83 | 7.69 | 3.15 | 10.347 |
| 283 | 43.83 | 7.69 | 3.15 | 8.819 |
| 284 | 43.83 | 7.69 | 3.15 | 11.129 |
| 285 | 43.83 | 7.69 | 3.15 | 31.729 |
| 286 | 43.83 | 7.69 | 3.15 | 3.339 |
| 287 | 43.83 | 7.69 | 3.15 | 12.161 |
| 288 | 43.83 | 7.69 | 3.15 | 5.568 |
| 289 | 43.83 | 7.69 | 3.15 | 11.654 |
| 290 | 43.83 | 7.69 | 3.15 | 2.455 |
| 291 | 43.83 | 7.69 | 3.15 | 8.723 |
| 292 | 43.83 | 7.69 | 3.15 | 2.3 |
| 293 | 43.83 | 7.69 | 3.15 | 6.187 |
| 294 | 43.83 | 7.69 | 3.15 | 4.871 |
| 295 | 43.83 | 7.69 | 3.15 | 12.407 |
| 296 | 43.83 | 7.69 | 3.15 | 2.554 |
| 297 | 43.83 | 7.69 | 3.15 | 8.591 |
| 298 | 43.83 | 7.69 | 3.15 | 14.808 |
| 299 | 43.83 | 7.69 | 3.15 | 15.137 |
| 300 | 43.83 | 7.69 | 3.15 | 3.498 |
| 301 | 28.41 | 3.54 | 1.03 | 733.912 |
| 302 | 28.41 | 3.54 | 1.03 | 760.067 |
| 303 | 28.41 | 3.54 | 1.03 | 702.235 |
| 304 | 28.41 | 3.54 | 1.03 | 610.965 |
| 305 | 28.41 | 3.54 | 1.03 | 587.109 |
| 306 | 28.41 | 3.54 | 1.03 | 551.251 |
| 307 | 28.41 | 3.54 | 1.03 | 377.107 |
| 308 | 28.41 | 3.54 | 1.03 | 320.673 |
| 309 | 28.41 | 3.54 | 1.03 | 289.437 |
| 310 | 28.41 | 3.54 | 1.03 | 349.663 |
| 311 | 28.41 | 3.54 | 1.03 | 391.414 |
| 312 | 28.41 | 3.54 | 1.03 | 307.374 |
| 313 | 28.41 | 3.54 | 1.03 | 344.188 |
| 314 | 28.41 | 3.54 | 1.03 | 444.424 |
| 315 | 28.41 | 3.54 | 1.03 | 463.4 |
| 316 | 28.41 | 3.54 | 1.03 | 442.848 |
| 317 | 28.41 | 3.54 | 1.03 | 290.39 |
| 318 | 28.41 | 3.54 | 1.03 | 278.003 |
| 319 | 28.41 | 3.54 | 1.03 | 304.047 |
| 320 | 28.41 | 3.54 | 1.03 | 280.408 |
| 321 | 28.41 | 3.54 | 1.03 | 191.913 |
| 322 | 28.41 | 3.54 | 1.03 | 240.513 |
| 323 | 28.41 | 3.54 | 1.03 | 305.565 |
| 324 | 28.41 | 3.54 | 1.03 | 283.729 |
| 325 | 28.41 | 3.54 | 1.03 | 274.864 |
| 326 | 40.56 | 1.83 | 2.21 | 60.968 |
| 327 | 40.56 | 1.83 | 2.21 | 70.425 |
| 328 | 40.56 | 1.83 | 2.21 | 50.42 |
| 329 | 40.56 | 1.83 | 2.21 | 7.107 |
| 330 | 40.56 | 1.83 | 2.21 | 13.184 |
| 331 | 40.56 | 1.83 | 2.21 | 8.961 |
| 332 | 40.56 | 1.83 | 2.21 | 14.007 |
| 333 | 40.56 | 1.83 | 2.21 | 7.847 |
| 334 | 40.56 | 1.83 | 2.21 | 10.378 |

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|-----|-------|------|------|---------|
| 336 | 40.56 | 1.83 | 2.21 | 7.734 |
| 337 | 40.56 | 1.83 | 2.21 | 10.201 |
| 338 | 40.56 | 1.83 | 2.21 | 38.172 |
| 339 | 40.56 | 1.83 | 2.21 | 7.616 |
| 340 | 40.56 | 1.83 | 2.21 | 16.242 |
| 341 | 40.56 | 1.83 | 2.21 | 6.16 |
| 342 | 40.56 | 1.83 | 2.21 | 7.199 |
| 343 | 40.56 | 1.83 | 2.21 | 22.989 |
| 344 | 40.56 | 1.83 | 2.21 | 11.978 |
| 345 | 40.56 | 1.83 | 2.21 | 68.692 |
| 346 | 40.56 | 1.83 | 2.21 | 33.74 |
| 347 | 40.56 | 1.83 | 2.21 | 41.814 |
| 348 | 40.56 | 1.83 | 2.21 | 4.385 |
| 349 | 40.56 | 1.83 | 2.21 | 73.786 |
| 350 | 40.56 | 1.83 | 2.21 | 66.978 |
| 351 | 45.35 | 8.63 | 5.31 | 2.544 |
| 352 | 45.35 | 8.63 | 5.31 | 9.009 |
| 353 | 45.35 | 8.63 | 5.31 | 7.455 |
| 354 | 45.35 | 8.63 | 5.31 | 7.942 |
| 356 | 45.35 | 8.63 | 5.31 | 15.349 |
| 357 | 45.35 | 8.63 | 5.31 | 10.432 |
| 358 | 45.35 | 8.63 | 5.31 | 16.821 |
| 359 | 45.35 | 8.63 | 5.31 | 4.913 |
| 360 | 45.35 | 8.63 | 5.31 | 5.251 |
| 361 | 45.35 | 8.63 | 5.31 | 4.231 |
| 362 | 45.35 | 8.63 | 5.31 | 6.231 |
| 363 | 45.35 | 8.63 | 5.31 | 5.29 |
| 364 | 45.35 | 8.63 | 5.31 | 4.751 |
| 365 | 45.35 | 8.63 | 5.31 | 8.247 |
| 366 | 45.35 | 8.63 | 5.31 | 9.601 |
| 367 | 45.35 | 8.63 | 5.31 | 8.831 |
| 368 | 45.35 | 8.63 | 5.31 | 11.345 |
| 369 | 45.35 | 8.63 | 5.31 | 3.351 |
| 370 | 45.35 | 8.63 | 5.31 | 16.069 |
| 371 | 45.35 | 8.63 | 5.31 | 21.694 |
| 372 | 45.35 | 8.63 | 5.31 | 3.063 |
| 373 | 45.35 | 8.63 | 5.31 | 6.881 |
| 374 | 45.35 | 8.63 | 5.31 | 4.482 |
| 375 | 45.35 | 8.63 | 5.31 | 3.268 |
| 376 | 40.56 | 1.83 | 2.21 | 19.347 |
| 377 | 40.56 | 1.83 | 2.21 | 3.423 |
| 378 | 40.56 | 1.83 | 2.21 | 135.887 |
| 379 | 40.56 | 1.83 | 2.21 | 73.428 |
| 380 | 40.56 | 1.83 | 2.21 | 70.348 |
| 381 | 40.56 | 1.83 | 2.21 | 6.155 |
| 382 | 40.56 | 1.83 | 2.21 | 34.198 |
| 383 | 40.56 | 1.83 | 2.21 | 20.396 |
| 384 | 40.56 | 1.83 | 2.21 | 30.15 |
| 385 | 40.56 | 1.83 | 2.21 | 45.353 |
| 386 | 40.56 | 1.83 | 2.21 | 36.26 |
| 387 | 40.56 | 1.83 | 2.21 | 34.983 |
| 388 | 40.56 | 1.83 | 2.21 | 37.264 |
| 389 | 40.56 | 1.83 | 2.21 | 20.816 |
| 390 | 40.56 | 1.83 | 2.21 | 11.931 |

| | | | | |
|-----|-------|------|------|---------|
| 391 | 40.56 | 1.83 | 2.21 | 75.062 |
| 392 | 40.56 | 1.83 | 2.21 | 49.846 |
| 393 | 40.56 | 1.83 | 2.21 | 94.475 |
| 394 | 40.56 | 1.83 | 2.21 | 105.916 |
| 395 | 40.56 | 1.83 | 2.21 | 109.913 |
| 396 | 40.56 | 1.83 | 2.21 | 12.634 |
| 397 | 40.56 | 1.83 | 2.21 | 25.726 |
| 398 | 40.56 | 1.83 | 2.21 | 6.243 |
| 399 | 40.56 | 1.83 | 2.21 | 7.471 |
| 400 | 40.56 | 1.83 | 2.21 | 7.08 |
| 401 | 40.56 | 1.83 | 2.21 | 52.316 |
| 402 | 40.56 | 1.83 | 2.21 | 70.394 |
| 403 | 40.56 | 1.83 | 2.21 | 111.474 |
| 404 | 40.56 | 1.83 | 2.21 | 6.92 |
| 405 | 40.56 | 1.83 | 2.21 | 5.449 |
| 406 | 40.56 | 1.83 | 2.21 | 20.783 |
| 407 | 40.56 | 1.83 | 2.21 | 8.304 |
| 408 | 40.56 | 1.83 | 2.21 | 6.083 |
| 409 | 40.56 | 1.83 | 2.21 | 115.819 |
| 410 | 40.56 | 1.83 | 2.21 | 11.872 |
| 411 | 40.56 | 1.83 | 2.21 | 13.124 |
| 412 | 40.56 | 1.83 | 2.21 | 9.693 |
| 413 | 40.56 | 1.83 | 2.21 | 10.569 |
| 414 | 40.56 | 1.83 | 2.21 | 13.18 |
| 416 | 27.04 | 1.36 | 0.19 | 379.94 |
| 417 | 27.04 | 1.36 | 0.19 | 371.876 |
| 418 | 27.04 | 1.36 | 0.19 | 398.463 |
| 419 | 27.04 | 1.36 | 0.19 | 396.218 |
| 420 | 27.04 | 1.36 | 0.19 | 403.533 |
| 421 | 27.04 | 1.36 | 0.19 | 425.222 |
| 422 | 27.04 | 1.36 | 0.19 | 473.121 |
| 423 | 27.04 | 1.36 | 0.19 | 473.924 |
| 424 | 27.04 | 1.36 | 0.19 | 75.354 |
| 425 | 27.04 | 1.36 | 0.19 | 432.498 |
| 426 | 27.04 | 1.36 | 0.19 | 34.942 |
| 427 | 27.04 | 1.36 | 0.19 | 37.798 |
| 428 | 27.04 | 1.36 | 0.19 | 44.089 |
| 429 | 27.04 | 1.36 | 0.19 | 40.629 |
| 430 | 27.04 | 1.36 | 0.19 | 75.552 |
| 431 | 27.04 | 1.36 | 0.19 | 92.507 |
| 432 | 27.04 | 1.36 | 0.19 | 350.97 |
| 433 | 27.04 | 1.36 | 0.19 | 335.119 |
| 434 | 27.04 | 1.36 | 0.19 | 309.823 |
| 435 | 27.04 | 1.36 | 0.19 | 327.999 |
| 436 | 40.56 | 1.83 | 2.21 | 34.403 |
| 437 | 40.56 | 1.83 | 2.21 | 34.125 |
| 438 | 40.56 | 1.83 | 2.21 | 84.66 |
| 439 | 40.56 | 1.83 | 2.21 | 351.997 |
| 440 | 40.56 | 1.83 | 2.21 | 39.571 |
| 441 | 40.56 | 1.83 | 2.21 | 21.973 |
| 442 | 40.56 | 1.83 | 2.21 | 135.118 |
| 443 | 40.56 | 1.83 | 2.21 | 159.263 |
| 444 | 40.56 | 1.83 | 2.21 | 171.164 |
| 445 | 40.56 | 1.83 | 2.21 | 76.476 |

| | | | | |
|-----|-------|------|------|---------|
| 446 | 40.56 | 1.83 | 2.21 | 179.977 |
| 447 | 40.56 | 1.83 | 2.21 | 5.959 |
| 448 | 40.56 | 1.83 | 2.21 | 39.799 |
| 449 | 40.56 | 1.83 | 2.21 | 51.107 |
| 450 | 40.56 | 1.83 | 2.21 | 72.602 |
| 451 | 40.56 | 1.83 | 2.21 | 94.947 |
| 452 | 40.56 | 1.83 | 2.21 | 88.603 |
| 453 | 40.56 | 1.83 | 2.21 | 311.39 |
| 454 | 40.56 | 1.83 | 2.21 | 317.894 |
| 455 | 40.56 | 1.83 | 2.21 | 344.157 |
| 456 | 40.56 | 1.83 | 2.21 | 6.586 |
| 457 | 40.56 | 1.83 | 2.21 | 27.999 |
| 458 | 40.56 | 1.83 | 2.21 | 18.514 |
| 459 | 40.56 | 1.83 | 2.21 | 6.428 |
| 460 | 40.56 | 1.83 | 2.21 | 13.221 |
| 461 | 40.56 | 1.83 | 2.21 | 23.151 |
| 462 | 40.56 | 1.83 | 2.21 | 12.206 |
| 463 | 40.56 | 1.83 | 2.21 | 29.342 |
| 464 | 40.56 | 1.83 | 2.21 | 41.112 |
| 465 | 40.56 | 1.83 | 2.21 | 56.615 |
| 466 | 40.56 | 1.83 | 2.21 | 35.475 |
| 467 | 40.56 | 1.83 | 2.21 | 9 |
| 468 | 40.56 | 1.83 | 2.21 | 29.14 |
| 469 | 40.56 | 1.83 | 2.21 | 15.457 |
| 470 | 40.56 | 1.83 | 2.21 | 26.067 |
| 471 | 40.56 | 1.83 | 2.21 | 60.288 |
| 472 | 40.56 | 1.83 | 2.21 | 30.68 |
| 473 | 40.56 | 1.83 | 2.21 | 60.907 |
| 474 | 40.56 | 1.83 | 2.21 | 71.101 |
| 475 | 40.56 | 1.83 | 2.21 | 70.34 |
| 476 | 45.35 | 8.63 | 5.31 | 40.039 |
| 477 | 45.35 | 8.63 | 5.31 | 49.225 |
| 478 | 45.35 | 8.63 | 5.31 | 42.22 |
| 479 | 45.35 | 8.63 | 5.31 | 26.86 |
| 480 | 45.35 | 8.63 | 5.31 | 19.994 |
| 481 | 45.35 | 8.63 | 5.31 | 22.351 |
| 482 | 45.35 | 8.63 | 5.31 | 16.08 |
| 483 | 45.35 | 8.63 | 5.31 | 15.868 |
| 485 | 45.35 | 8.63 | 5.31 | 20.227 |
| 486 | 45.35 | 8.63 | 5.31 | 9.361 |
| 487 | 45.35 | 8.63 | 5.31 | 4.412 |
| 488 | 45.35 | 8.63 | 5.31 | 82.523 |
| 489 | 45.35 | 8.63 | 5.31 | 52.58 |
| 489 | 45.35 | 8.63 | 5.31 | 3.383 |
| 490 | 45.35 | 8.63 | 5.31 | 9.633 |
| 491 | 45.35 | 8.63 | 5.31 | 11.822 |
| 492 | 45.35 | 8.63 | 5.31 | 24.102 |
| 493 | 45.35 | 8.63 | 5.31 | 5.731 |
| 494 | 45.35 | 8.63 | 5.31 | 12.232 |
| 495 | 45.35 | 8.63 | 5.31 | 10.824 |

Table: Transportation Attributes

| BUET ID | CBD ACC | M RD ACC | EDU ACC | SHOP ACC | W MAR AC |
|---------|----------|----------|---------|----------|----------|
| 1 | 2551.767 | 735.514 | 1076.93 | 2537.897 | 2052.035 |
| 2 | 2433.072 | 854.209 | 687.52 | 2419.202 | 1933.34 |
| 3 | 2263.333 | 949.847 | 47.69 | 2249.464 | 1763.602 |
| 4 | 1838.9 | 1374.281 | 1200.01 | 1825.03 | 1339.168 |
| 5 | 1340.949 | 1305.074 | 714.36 | 1327.079 | 841.218 |
| 6 | 1701.277 | 862.384 | 1096.35 | 1366.848 | 1201.547 |
| 7 | 1578.52 | 682.779 | 507.09 | 1187.243 | 1078.789 |
| 8 | 1835.122 | 586.677 | 1059.72 | 1416.778 | 1335.392 |
| 9 | 2107.685 | 859.24 | 395.5 | 1689.341 | 1607.955 |
| 10 | 2286.905 | 902.176 | 192.49 | 1868.561 | 1787.175 |
| 11 | 2586.183 | 1082.035 | 1174.37 | 2167.839 | 2086.453 |
| 12 | 2520.816 | 697.195 | 21.91 | 2102.472 | 2021.086 |
| 13 | 2692.145 | 521.036 | 599.86 | 2278.632 | 2192.414 |
| 14 | 2886.845 | 326.336 | 1238.64 | 2465.42 | 2387.114 |
| 15 | 2887.276 | 301.805 | 1431.16 | 2440.888 | 2387.546 |
| 16 | 2910.164 | 513.318 | 1315.14 | 2496.65 | 2410.433 |
| 17 | 2731.057 | 621.003 | 727.52 | 2317.543 | 2231.326 |
| 18 | 2736.474 | 550.807 | 471.53 | 2722.604 | 2236.743 |
| 19 | 2132.799 | 1125.864 | 1318.16 | 2118.929 | 1633.068 |
| 20 | 2279.564 | 909.517 | 168.4 | 1861.22 | 1779.834 |
| 21 | 2801.964 | 411.217 | 960.16 | 2388.451 | 2302.233 |
| 22 | 2408.316 | 904.168 | 590.82 | 1989.972 | 1908.586 |
| 23 | 2772.95 | 416.131 | 1067.65 | 2354.606 | 2273.22 |
| 25 | 2094.432 | 845.987 | 1655.04 | 1676.088 | 1594.702 |
| 26 | 570.721 | 570.534 | 2087.55 | 505.228 | 570.534 |
| 27 | 530.18 | 529.994 | 1954.54 | 464.687 | 529.994 |
| 28 | 614.99 | 614.804 | 1636.54 | 549.497 | 614.804 |
| 29 | 780.072 | 779.885 | 1243.68 | 714.578 | 589.307 |
| 30 | 829.093 | 828.906 | 1404.51 | 763.599 | 638.328 |
| 31 | 567.845 | 567.658 | 192.4 | 506.315 | 376.294 |
| 32 | 688.831 | 688.644 | 2475.04 | 623.337 | 688.644 |
| 33 | 889.213 | 889.026 | 801.05 | 823.719 | 615.212 |
| 34 | 857.61 | 857.423 | 840.54 | 754.364 | 466.43 |
| 35 | 874.041 | 873.854 | 862.24 | 760.977 | 473.044 |
| 36 | 759.778 | 759.591 | 1970.47 | 671.974 | 759.591 |
| 37 | 866.758 | 866.571 | 2079.44 | 790.308 | 866.571 |
| 38 | 773.398 | 773.211 | 1914.18 | 707.904 | 773.211 |
| 39 | 945.724 | 937.276 | 1585.87 | 880.23 | 945.537 |
| 40 | 1040.277 | 861.086 | 1335.91 | 974.783 | 1040.09 |
| 41 | 1267.698 | 705.38 | 440.7 | 1197.513 | 990.892 |
| 42 | 1291.423 | 711.486 | 665.87 | 1203.618 | 1059.523 |
| 43 | 1085.105 | 757.919 | 997.43 | 997.3 | 1084.918 |
| 44 | 956.036 | 866.324 | 1302.18 | 868.232 | 955.85 |

| | | | | | |
|----|----------|---------|---------|----------|---------|
| 45 | 835.221 | 835.034 | 1390.92 | 747.416 | 835.034 |
| 46 | 891.688 | 891.501 | 1513.3 | 803.884 | 891.501 |
| 47 | 770.878 | 770.691 | 2230.47 | 683.074 | 770.691 |
| 48 | 1060.237 | 919 | 1525.91 | 994.743 | 1060.05 |
| 49 | 1242.265 | 794.707 | 357.26 | 1176.772 | 965.459 |
| 50 | 1187.488 | 844.093 | 200.36 | 1121.994 | 910.681 |
| 51 | 248.847 | 249.033 | 445.64 | 336.651 | 249.033 |
| 52 | 278.758 | 278.945 | 308.55 | 366.563 | 278.945 |
| 53 | 317.802 | 317.989 | 418.68 | 405.606 | 317.989 |
| 54 | 418.438 | 418.624 | 124.61 | 506.242 | 418.624 |
| 55 | 292.603 | 292.79 | 353.98 | 380.408 | 292.79 |
| 56 | 225.202 | 225.389 | 592.96 | 313.007 | 225.389 |
| 57 | 401.28 | 401.467 | 710.53 | 489.085 | 401.467 |
| 58 | 378.006 | 378.193 | 634.17 | 465.811 | 378.193 |
| 59 | 461.345 | 461.532 | 494.86 | 549.15 | 461.532 |
| 60 | 348.576 | 348.389 | 1389 | 333.915 | 348.389 |
| 61 | 348.576 | 348.389 | 1389 | 333.915 | 348.389 |
| 62 | 320.284 | 320.471 | 699.7 | 408.089 | 320.471 |
| 63 | 409.735 | 409.549 | 1463.98 | 395.074 | 409.549 |
| 64 | 381.593 | 381.406 | 1497.33 | 366.932 | 381.406 |
| 65 | 349.183 | 348.996 | 1391 | 334.522 | 348.996 |
| 66 | 316.624 | 316.437 | 1434.61 | 396.735 | 316.437 |
| 67 | 344.494 | 344.307 | 1526.05 | 424.605 | 344.307 |
| 68 | 375.456 | 375.269 | 1627.63 | 455.567 | 375.269 |
| 69 | 372.86 | 372.673 | 1619.12 | 452.971 | 372.673 |
| 70 | 319.752 | 319.565 | 1444.88 | 399.863 | 319.565 |
| 72 | 663.28 | 663.093 | 69.05 | 569.943 | 471.627 |
| 73 | 463.356 | 463.169 | 867.08 | 544.022 | 270.553 |
| 74 | 433.213 | 433.026 | 766.37 | 513.325 | 239.855 |
| 75 | 207.501 | 207.314 | 1167.19 | 294.932 | 207.314 |
| 81 | 1188.109 | 328.628 | 735.46 | 224.877 | 513.761 |
| 82 | 1153.163 | 165.699 | 200.92 | 189.932 | 478.815 |
| 83 | 1186.528 | 199.063 | 310.38 | 223.296 | 512.179 |
| 84 | 1011.753 | 533.049 | 1039.04 | 317.335 | 121.901 |
| 85 | 979.09 | 576.352 | 1447.95 | 278.5 | 319.399 |
| 86 | 930.931 | 528.193 | 1289.95 | 230.341 | 336.828 |
| 87 | 871.314 | 528.488 | 1156.85 | 230.636 | 379.875 |
| 88 | 919.212 | 557.07 | 1140.84 | 259.218 | 291.381 |
| 89 | 914.942 | 612.856 | 1299.99 | 315.004 | 454.312 |
| 90 | 916.28 | 668.837 | 950.76 | 453.124 | 82.102 |
| 91 | 1007.802 | 728.533 | 1102.67 | 544.645 | 173.623 |
| 92 | 1064.044 | 711.025 | 1013.52 | 600.887 | 229.865 |
| 93 | 1069.745 | 648.403 | 839.78 | 606.588 | 235.566 |
| 94 | 1102.865 | 681.523 | 948.44 | 639.708 | 268.686 |
| 95 | 1114.676 | 628.956 | 775.98 | 651.519 | 280.498 |
| 96 | 1217.347 | 524.681 | 433.87 | 754.19 | 383.169 |
| 97 | 1274.815 | 477.661 | 279.61 | 811.658 | 440.636 |

| | | | | | |
|-----|----------|---------|---------|----------|----------|
| 98 | 1378.444 | 315.414 | 338.57 | 915.287 | 544.266 |
| 100 | 1513.967 | 217.078 | 783.19 | 914.805 | 679.788 |
| 101 | 777.254 | 777.068 | 656.68 | 864.685 | 720.908 |
| 102 | 816.336 | 816.149 | 784.91 | 903.767 | 759.99 |
| 103 | 801 | 800.813 | 734.59 | 888.43 | 744.654 |
| 104 | 871.636 | 871.449 | 558.64 | 959.066 | 871.449 |
| 105 | 885.515 | 885.328 | 1011.87 | 972.946 | 829.169 |
| 106 | 849.497 | 849.31 | 893.7 | 936.928 | 793.151 |
| 107 | 728.774 | 728.587 | 497.63 | 816.204 | 672.428 |
| 108 | 719.83 | 719.643 | 319.12 | 807.26 | 663.484 |
| 109 | 765.323 | 765.136 | 169.87 | 852.754 | 708.977 |
| 110 | 753.88 | 753.693 | 607.47 | 841.311 | 605.11 |
| 111 | 866.46 | 866.273 | 943.09 | 953.89 | 492.53 |
| 112 | 883.575 | 883.389 | 940.73 | 971.006 | 495.296 |
| 113 | 940.344 | 940.157 | 1219.23 | 1027.775 | 621.464 |
| 114 | 956.795 | 956.608 | 815.3 | 942.925 | 457.064 |
| 116 | 851.332 | 851.145 | 800.72 | 938.763 | 449.137 |
| 117 | 793.756 | 793.569 | 611.82 | 881.187 | 391.561 |
| 118 | 708.823 | 708.636 | 243.58 | 796.254 | 306.628 |
| 119 | 651.932 | 651.745 | 447.43 | 737.125 | 176.514 |
| 120 | 645.053 | 644.866 | 424.86 | 732.484 | 183.393 |
| 121 | 427.693 | 427.507 | 236.55 | 515.124 | 427.507 |
| 122 | 535.561 | 535.374 | 97.27 | 622.992 | 535.374 |
| 123 | 562.667 | 562.854 | 375.85 | 650.472 | 562.854 |
| 124 | 589.05 | 589.237 | 462.41 | 676.854 | 589.237 |
| 125 | 615.196 | 615.383 | 548.19 | 703.001 | 615.383 |
| 126 | 1718.064 | 367.028 | 1821.37 | 327.495 | 1717.877 |
| 127 | 1533.552 | 429.095 | 2025 | 389.562 | 1533.365 |
| 128 | 1468.078 | 654.335 | 2305.77 | 614.803 | 1467.892 |
| 129 | 1334.485 | 628.162 | 2108.41 | 588.629 | 1334.298 |
| 130 | 1478.416 | 706.743 | 2113.68 | 677.356 | 1478.229 |
| 131 | 1425.686 | 759.473 | 1940.69 | 730.086 | 1425.499 |
| 132 | 1374.884 | 798.005 | 1854.45 | 758.472 | 1374.697 |
| 133 | 1487.756 | 738.47 | 1826.71 | 738.47 | 1487.569 |
| 134 | 1501.289 | 690.521 | 1669.39 | 690.521 | 1501.102 |
| 135 | 1518.463 | 707.695 | 1725.74 | 707.695 | 1518.276 |
| 136 | 1364.876 | 774.062 | 984.83 | 774.062 | 1364.689 |
| 137 | 1423.961 | 727.632 | 1178.68 | 727.632 | 1423.774 |
| 138 | 2011.443 | 48.796 | 777.3 | 88.328 | 2011.256 |
| 139 | 2109.104 | 146.457 | 1097.71 | 185.99 | 2108.917 |
| 140 | 2181.826 | 219.18 | 1336.3 | 258.712 | 2181.639 |
| 141 | 2350.316 | 387.669 | 882.35 | 398.689 | 2350.129 |
| 142 | 2405.995 | 443.348 | 699.67 | 453.983 | 2405.808 |
| 143 | 2350.959 | 388.312 | 1187.74 | 427.845 | 2350.772 |
| 144 | 2374.253 | 411.606 | 1464.43 | 451.139 | 2374.066 |
| 145 | 2429.688 | 467.041 | 1570.42 | 506.573 | 2429.5 |
| 146 | 2506.344 | 543.697 | 1157.45 | 566.995 | 2506.157 |

| | | | | | |
|-----|----------|----------|---------|----------|----------|
| 147 | 2687.823 | 725.176 | 890.12 | 748.474 | 2687.636 |
| 148 | 2742.917 | 780.27 | 376.8 | 810.922 | 2742.729 |
| 149 | 2664.442 | 701.795 | 225.78 | 741.328 | 2664.255 |
| 150 | 2658.756 | 696.109 | 1252.26 | 735.642 | 2658.569 |
| 151 | 1193.131 | 1192.944 | 467.62 | 1280.562 | 1192.944 |
| 152 | 1205.545 | 1205.358 | 508.34 | 1292.976 | 1205.358 |
| 153 | 1122.062 | 1121.875 | 44.74 | 1209.493 | 1121.875 |
| 154 | 1271.015 | 1270.829 | 723.14 | 1358.446 | 1270.829 |
| 155 | 953.238 | 953.051 | 507.45 | 1040.669 | 953.051 |
| 156 | 1118.393 | 1118.207 | 108.51 | 1205.824 | 1118.207 |
| 157 | 1180.481 | 1180.294 | 208.53 | 1267.912 | 1149.139 |
| 158 | 1109.31 | 1109.123 | 442.03 | 1196.741 | 1077.968 |
| 159 | 1153.895 | 1153.708 | 295.75 | 1241.326 | 1122.553 |
| 160 | 1094.753 | 1094.566 | 489.79 | 1182.184 | 1063.411 |
| 161 | 1061.172 | 1060.985 | 642.79 | 1148.603 | 1060.985 |
| 162 | 1051.296 | 1051.109 | 632.37 | 1138.726 | 1019.953 |
| 163 | 1123.452 | 1123.265 | 521.35 | 1210.883 | 1037.434 |
| 164 | 1100.592 | 1100.405 | 596.34 | 1188.023 | 1014.575 |
| 165 | 1246.439 | 1246.252 | 645.96 | 1333.87 | 1158.329 |
| 166 | 1326.044 | 1325.857 | 907.13 | 1413.474 | 1237.933 |
| 167 | 1327.977 | 1327.79 | 1022.74 | 1415.408 | 1299.825 |
| 168 | 1360.981 | 1360.794 | 1021.75 | 1448.412 | 1272.871 |
| 169 | 1385.999 | 1385.812 | 1103.83 | 1473.43 | 1297.889 |
| 170 | 1272.3 | 1272.113 | 518.2 | 1359.731 | 874.748 |
| 171 | 1268.877 | 1268.69 | 739.17 | 1356.308 | 921.453 |
| 172 | 1360.056 | 1359.869 | 828.85 | 1447.486 | 1012.631 |
| 173 | 1214.897 | 1214.71 | 758.5 | 1302.328 | 867.829 |
| 174 | 1162.893 | 1162.706 | 951.51 | 1250.323 | 815.468 |
| 175 | 1033.936 | 1033.75 | 1305.9 | 1121.367 | 829.898 |
| 176 | 1763.232 | 1260.359 | 463.66 | 1850.663 | 1714.068 |
| 177 | 1988.883 | 1167.899 | 257.23 | 2076.314 | 1904.508 |
| 178 | 1885.272 | 1274.616 | 607.36 | 1972.703 | 1797.791 |
| 179 | 2000.474 | 1197.592 | 768.92 | 2087.905 | 1800.887 |
| 180 | 2083.001 | 1115.065 | 498.17 | 2170.432 | 1883.414 |
| 181 | 2305.977 | 1220.416 | 757.06 | 2342.888 | 1857.027 |
| 183 | 2140.13 | 1146.836 | 515.65 | 2126.26 | 1640.398 |
| 184 | 1961.463 | 1321.328 | 1088.13 | 1947.593 | 1461.732 |
| 185 | 2225.446 | 1300.948 | 1021.27 | 2312.877 | 1913.206 |
| 186 | 1771.762 | 1433.359 | 454.74 | 1757.892 | 1272.031 |
| 187 | 1860.902 | 1522.5 | 246.51 | 1847.032 | 1361.171 |
| 188 | 1984.629 | 1513.581 | 349.31 | 1970.759 | 1484.898 |
| 189 | 2019.485 | 1396.644 | 732.96 | 2087.696 | 1601.835 |
| 190 | 1788.887 | 1391.855 | 895.07 | 1876.318 | 1700.777 |
| 191 | 1627.715 | 1526.2 | 911.77 | 1715.146 | 1536.382 |
| 192 | 1804.873 | 1519.622 | 368.81 | 1892.304 | 1495.186 |
| 193 | 1847.247 | 1576.009 | 165.88 | 1900.541 | 1414.68 |
| 194 | 1863.153 | 1476.442 | 177.61 | 1950.584 | 1543.322 |

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|-----|----------|----------|---------|----------|----------|
| 195 | 2083.628 | 1429.043 | 674.11 | 2069.758 | 1583.897 |
| 196 | 1850.528 | 1353.88 | 340.7 | 1937.959 | 1850.341 |
| 197 | 1866.363 | 1369.714 | 168.42 | 1953.794 | 1866.176 |
| 198 | 1853.968 | 1357.32 | 127.76 | 1941.399 | 1853.781 |
| 199 | 1879.078 | 1382.429 | 210.14 | 1966.509 | 1878.891 |
| 201 | 2032.949 | 1077.25 | 198.35 | 2120.381 | 1995.157 |
| 202 | 2251.54 | 869.013 | 447.25 | 2338.971 | 2174.249 |
| 203 | 2304.976 | 893.09 | 673.17 | 2392.407 | 2105.389 |
| 204 | 2247.796 | 1023.122 | 914.82 | 2335.227 | 2048.208 |
| 205 | 2277.893 | 1061.715 | 1013.56 | 2365.324 | 2051.516 |
| 206 | 2377.352 | 962.256 | 1078.37 | 2464.782 | 2150.974 |
| 207 | 2468.832 | 1030.274 | 1301.52 | 2556.263 | 2242.454 |
| 208 | 2482.431 | 818.272 | 517.85 | 2569.862 | 2321.821 |
| 209 | 2522.581 | 732.391 | 65.85 | 2610.012 | 2400.507 |
| 210 | 2752.946 | 574.057 | 784.28 | 2840.377 | 2514.723 |
| 211 | 2654.86 | 786.255 | 1244 | 2640.99 | 2155.128 |
| 212 | 2485.075 | 802.206 | 858.13 | 2471.205 | 1985.344 |
| 213 | 2229.56 | 1093.218 | 339.74 | 2215.69 | 1729.829 |
| 214 | 2243.357 | 866.843 | 420.41 | 2330.788 | 2205.564 |
| 215 | 2678.516 | 412.189 | 468.16 | 2765.947 | 2586.29 |
| 216 | 2743.703 | 273.524 | 682.02 | 2831.134 | 2743.517 |
| 217 | 2852.164 | 447.534 | 1019.01 | 2939.595 | 2613.941 |
| 218 | 3012.908 | 567.09 | 524.95 | 3025.708 | 2539.847 |
| 219 | 2892.856 | 420.367 | 43.58 | 2878.987 | 2393.125 |
| 220 | 3008.553 | 278.728 | 164.86 | 2994.683 | 2508.822 |
| 221 | 2464.853 | 559.641 | 741.31 | 2552.284 | 2464.666 |
| 222 | 2674.505 | 471.46 | 662.61 | 2761.936 | 2552.432 |
| 223 | 2404.682 | 639.343 | 721.55 | 2492.112 | 2404.495 |
| 224 | 2142.491 | 913.018 | 503.21 | 2229.922 | 2142.305 |
| 226 | 5057.159 | 2114.793 | 2583.79 | 5144.589 | 4902.343 |
| 227 | 5142.809 | 2200.443 | 2302.78 | 5230.24 | 4987.994 |
| 228 | 4997.103 | 2054.738 | 2428.66 | 5084.534 | 4842.288 |
| 229 | 4687.419 | 1745.054 | 1500.26 | 4774.85 | 4532.604 |
| 230 | 4753.971 | 1819.305 | 669.92 | 4841.402 | 4606.854 |
| 231 | 4510.643 | 1568.277 | 320.29 | 4598.073 | 4355.827 |
| 232 | 4422.705 | 1480.339 | 631.78 | 4510.135 | 4267.889 |
| 233 | 4397.649 | 1455.283 | 31.93 | 4485.08 | 4242.833 |
| 234 | 4262.11 | 1319.745 | 843.41 | 4349.541 | 4107.294 |
| 235 | 4906.245 | 1963.88 | 2130.57 | 4993.676 | 4751.43 |
| 236 | 4252.789 | 1310.423 | 894.05 | 4340.22 | 4097.974 |
| 237 | 3760.284 | 961.722 | 1082.97 | 3847.715 | 3749.272 |
| 238 | 4160.267 | 1460.15 | 1370.79 | 4247.697 | 4160.08 |
| 239 | 3865.649 | 923.284 | 232.17 | 3953.08 | 3710.834 |
| 240 | 3736.655 | 794.29 | 816.67 | 3824.086 | 3581.84 |
| 241 | 3550.056 | 607.69 | 1011.41 | 3637.486 | 3395.24 |
| 242 | 3345.571 | 403.205 | 814.45 | 3433.001 | 3190.755 |
| 243 | 3338.118 | 419.545 | 1159.24 | 3425.549 | 3207.095 |

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|-----|----------|----------|---------|----------|----------|
| 244 | 3008.938 | 188.231 | 1014.11 | 3096.369 | 2975.78 |
| 245 | 3652.656 | 734.083 | 592.35 | 3740.087 | 3521.633 |
| 246 | 3686.229 | 743.864 | 710.35 | 3773.66 | 3531.414 |
| 247 | 4377.146 | 1434.78 | 35.34 | 4464.576 | 4222.33 |
| 248 | 4314.408 | 1372.042 | 1096.21 | 4401.839 | 4159.592 |
| 249 | 3983.468 | 1041.103 | 1156.71 | 4070.899 | 3828.653 |
| 250 | 4018.51 | 1076.145 | 1246.96 | 4105.941 | 3863.695 |
| 251 | 1672.329 | 206.927 | 766.97 | 1083.344 | 1172.598 |
| 253 | 1711.99 | 352.132 | 897.09 | 1064.366 | 1212.259 |
| 254 | 1666.347 | 306.489 | 747.34 | 1018.722 | 1166.616 |
| 255 | 1671.397 | 311.539 | 763.91 | 978.732 | 1171.666 |
| 256 | 1616.902 | 372.55 | 703.67 | 917.721 | 1117.171 |
| 257 | 1571.079 | 308.178 | 434.79 | 1079.051 | 1071.348 |
| 258 | 1542.671 | 336.586 | 341.58 | 1107.459 | 1042.94 |
| 259 | 1623.102 | 319.084 | 605.47 | 1089.957 | 1123.371 |
| 260 | 1664.155 | 360.137 | 740.15 | 1131.01 | 1164.424 |
| 261 | 1669.748 | 365.73 | 741.67 | 1136.603 | 1170.017 |
| 262 | 1676.634 | 372.616 | 719.08 | 1143.489 | 1176.903 |
| 263 | 1735.812 | 447.132 | 733.9 | 1218.005 | 1236.081 |
| 264 | 1776.473 | 487.793 | 867.3 | 1258.666 | 1276.742 |
| 265 | 1602.863 | 501.047 | 297.72 | 1211.586 | 1103.132 |
| 266 | 1583.945 | 512.528 | 235.65 | 1192.668 | 1084.214 |
| 267 | 1443.832 | 435.424 | 335.09 | 1042.776 | 944.101 |
| 268 | 1436.296 | 454.046 | 312.92 | 1035.239 | 936.565 |
| 269 | 1408.277 | 531.715 | 21.73 | 1007.22 | 908.546 |
| 270 | 1378.554 | 500.702 | 123.48 | 977.498 | 878.823 |
| 271 | 1333.571 | 565.184 | 234.84 | 942.294 | 833.84 |
| 272 | 1434.1 | 658.368 | 286.25 | 1042.823 | 934.369 |
| 273 | 1470.496 | 694.764 | 405.66 | 1079.219 | 970.765 |
| 274 | 1455.095 | 655.78 | 277.76 | 1063.818 | 955.364 |
| 275 | 1561.201 | 665.46 | 450.28 | 1169.924 | 1061.471 |
| 276 | 1109.851 | 912.327 | 796.89 | 719.096 | 610.12 |
| 277 | 1116.652 | 847.441 | 837.98 | 654.21 | 619.479 |
| 278 | 1112.234 | 828.408 | 341.45 | 649.792 | 615.06 |
| 279 | 1071.658 | 894.124 | 1057.05 | 609.215 | 574.484 |
| 280 | 1010.02 | 845.43 | 913.11 | 547.578 | 512.846 |
| 281 | 1007.117 | 842.527 | 903.58 | 544.675 | 509.943 |
| 282 | 1010.345 | 845.755 | 914.18 | 547.903 | 513.172 |
| 283 | 1125.967 | 961.377 | 1293.51 | 663.525 | 628.793 |
| 284 | 1123.991 | 959.401 | 1287.03 | 661.549 | 626.817 |
| 285 | 982.893 | 818.303 | 824.11 | 520.451 | 485.719 |
| 286 | 964.541 | 412.462 | 954.77 | 114.61 | 485.632 |
| 287 | 929.586 | 447.417 | 910.1 | 149.565 | 520.587 |
| 288 | 926.176 | 478.77 | 898.91 | 180.918 | 548.703 |
| 289 | 948.054 | 592.933 | 970.69 | 295.081 | 570.581 |
| 290 | 921.492 | 566.371 | 883.55 | 268.519 | 544.019 |
| 291 | 859.285 | 517.718 | 679.45 | 219.866 | 481.812 |

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|-----|----------|----------|---------|----------|----------|
| 292 | 919.33 | 754.74 | 615.57 | 456.888 | 422.156 |
| 293 | 1087.891 | 881.927 | 724.84 | 688.696 | 588.161 |
| 294 | 1113.163 | 843.952 | 849.43 | 650.721 | 615.989 |
| 295 | 1151.692 | 788.95 | 711.99 | 689.25 | 654.518 |
| 296 | 1234.75 | 705.892 | 439.49 | 772.308 | 737.576 |
| 297 | 1061.908 | 982.379 | 995.13 | 717.577 | 562.177 |
| 298 | 958.108 | 911.628 | 682.71 | 613.776 | 458.377 |
| 299 | 1153.231 | 914.842 | 1125.02 | 690.789 | 656.057 |
| 300 | 1176.795 | 763.847 | 629.63 | 714.353 | 679.621 |
| 301 | 4946.092 | 2245.976 | 195.77 | 5033.522 | 4945.905 |
| 302 | 5040.109 | 2339.993 | 339.05 | 5127.54 | 5039.922 |
| 303 | 5041.188 | 2341.071 | 116.22 | 5128.618 | 5041.001 |
| 304 | 5132.379 | 2432.263 | 415.41 | 5219.81 | 5132.192 |
| 305 | 5078.012 | 2377.896 | 794.95 | 5165.443 | 5077.826 |
| 306 | 4963.961 | 2263.844 | 1169.13 | 5051.392 | 4963.774 |
| 307 | 5332.11 | 2599.938 | 642.16 | 5419.541 | 5331.923 |
| 308 | 5359.259 | 2627.088 | 553.09 | 5446.69 | 5359.073 |
| 309 | 5450.116 | 2717.944 | 255 | 5537.546 | 5449.929 |
| 310 | 5395.838 | 2663.667 | 574.17 | 5483.269 | 5395.652 |
| 311 | 5469.807 | 2737.635 | 816.85 | 5557.237 | 5469.62 |
| 312 | 5505.279 | 2773.107 | 137.26 | 5592.709 | 5505.092 |
| 313 | 5603.634 | 2871.462 | 248.67 | 5691.064 | 5603.447 |
| 314 | 5206.513 | 2474.341 | 942.62 | 5293.943 | 5206.326 |
| 315 | 5043.645 | 2311.473 | 1476.97 | 5131.075 | 5043.458 |
| 316 | 5080.713 | 2348.542 | 1355.35 | 5168.144 | 5080.526 |
| 317 | 4803.104 | 2070.932 | 860.46 | 4890.534 | 4802.917 |
| 318 | 4759.939 | 2050.334 | 718.85 | 4847.37 | 4759.752 |
| 319 | 4718.856 | 2009.252 | 584.06 | 4806.287 | 4718.67 |
| 320 | 4666.103 | 1956.498 | 410.99 | 4753.534 | 4665.917 |
| 321 | 4598.418 | 1888.814 | 3.09 | 4685.849 | 4598.232 |
| 322 | 4627.773 | 1918.168 | 285.23 | 4715.204 | 4627.586 |
| 323 | 4580.585 | 1870.98 | 246.75 | 4668.016 | 4580.399 |
| 324 | 4502.47 | 1792.865 | 9.54 | 4589.9 | 4502.283 |
| 325 | 4537.493 | 1827.888 | 105.37 | 4624.923 | 4537.306 |
| 326 | 2683.288 | 690.233 | 280.41 | 1678.37 | 1939.386 |
| 327 | 2719.221 | 726.165 | 398.29 | 1714.302 | 1975.318 |
| 328 | 2746.769 | 753.713 | 488.67 | 1741.85 | 2002.866 |
| 329 | 2671.749 | 372.743 | 1475.3 | 1708.517 | 1997.401 |
| 330 | 2693.265 | 394.259 | 1545.89 | 1730.034 | 2018.917 |
| 331 | 2589.046 | 290.04 | 1203.97 | 1625.814 | 1914.697 |
| 332 | 2619.239 | 320.233 | 1303.03 | 1656.007 | 1944.891 |
| 333 | 2898.694 | 599.688 | 735.88 | 1919.665 | 2180.681 |
| 334 | 2914.089 | 615.084 | 844.54 | 1950.858 | 2213.801 |
| 336 | 2914.158 | 615.152 | 953.21 | 1950.926 | 2239.81 |
| 337 | 2948.039 | 649.033 | 995.11 | 1984.807 | 2259.697 |
| 338 | 2907.272 | 608.267 | 1153.04 | 1944.041 | 2232.924 |
| 339 | 3226.848 | 927.843 | 825.25 | 2263.617 | 2552.5 |

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|-----|----------|----------|---------|----------|----------|
| 340 | 3341.907 | 1120.39 | 747.61 | 2336.989 | 2598.005 |
| 341 | 3245.623 | 946.617 | 763.65 | 2282.391 | 2571.274 |
| 342 | 3338.465 | 1039.459 | 56.26 | 2375.233 | 2639.844 |
| 343 | 3323.717 | 1024.711 | 7.88 | 2360.485 | 2649.369 |
| 344 | 3310.811 | 1089.294 | 645.58 | 2305.892 | 2566.908 |
| 345 | 3535.671 | 1236.666 | 445.51 | 2572.44 | 2855.49 |
| 346 | 3565.037 | 1271.021 | 332.8 | 2560.118 | 2821.135 |
| 347 | 3595.137 | 1359.298 | 431.55 | 2590.219 | 2851.235 |
| 348 | 3584.663 | 1348.825 | 397.19 | 2579.745 | 2840.761 |
| 349 | 3702.862 | 1463.7 | 784.98 | 2697.944 | 2958.96 |
| 350 | 3692.975 | 1453.814 | 752.54 | 2688.057 | 2949.073 |
| 351 | 1730.104 | 175.014 | 1492.3 | 872.741 | 895.925 |
| 352 | 1806.817 | 251.727 | 1552.15 | 949.454 | 972.639 |
| 353 | 1745.009 | 242.439 | 1320.33 | 940.165 | 963.35 |
| 354 | 1726.592 | 260.855 | 1259.91 | 958.582 | 981.767 |
| 356 | 1602.432 | 284.339 | 780.02 | 982.065 | 986.216 |
| 357 | 1427.23 | 459.54 | 510.7 | 1157.267 | 1070.036 |
| 358 | 1509.031 | 417.148 | 488.02 | 1114.874 | 1068.303 |
| 359 | 1450.241 | 654.267 | 750.98 | 1158.898 | 1249.281 |
| 360 | 1337.598 | 662.797 | 778.96 | 1125.829 | 1168.576 |
| 361 | 1392.752 | 644.529 | 719.03 | 1070.791 | 1229.883 |
| 362 | 1463.542 | 715.319 | 351.28 | 1000.001 | 1300.673 |
| 363 | 1381.958 | 657.313 | 760.97 | 1067.206 | 1242.667 |
| 364 | 1262.452 | 912.792 | 648.8 | 937.477 | 1262.265 |
| 365 | 1170.684 | 1079.59 | 1087.36 | 1040.057 | 1170.497 |
| 366 | 1219.439 | 965.218 | 820.8 | 981.093 | 1219.253 |
| 367 | 1170.684 | 1079.59 | 1087.36 | 1040.057 | 1170.497 |
| 368 | 1012.826 | 1012.639 | 1424.85 | 925.021 | 1012.639 |
| 369 | 1113.637 | 1113.45 | 1755.6 | 1025.832 | 1113.45 |
| 370 | 1287.807 | 1193.713 | 2062.83 | 1154.18 | 1287.62 |
| 371 | 1120.861 | 1120.674 | 1779.3 | 1033.056 | 1120.674 |
| 372 | 1025.131 | 1024.944 | 674.83 | 937.327 | 1024.944 |
| 373 | 1060.525 | 1060.338 | 324.37 | 999.917 | 1060.338 |
| 374 | 1038.826 | 1038.639 | 1228.08 | 951.021 | 1038.639 |
| 375 | 1035.793 | 1035.606 | 316.21 | 975.185 | 1035.606 |
| 376 | 3491.5 | 1664.73 | 124.65 | 2237.068 | 2547.361 |
| 377 | 3507.994 | 1681.224 | 178.76 | 2253.562 | 2563.855 |
| 378 | 3354.019 | 1572.893 | 842.13 | 1862.229 | 2409.88 |
| 379 | 3387.335 | 1606.209 | 405.44 | 2132.904 | 2443.196 |
| 380 | 3383.541 | 1602.415 | 393 | 2129.109 | 2439.402 |
| 381 | 3516.784 | 1690.015 | 207.6 | 2262.353 | 2572.646 |
| 382 | 3696.005 | 1760.485 | 666.55 | 2441.573 | 2751.866 |
| 383 | 3725.111 | 1789.591 | 762.04 | 2470.679 | 2780.972 |
| 384 | 3719.694 | 1784.175 | 744.27 | 2465.262 | 2775.555 |
| 385 | 3676.136 | 1849.367 | 730.41 | 2421.705 | 2731.998 |
| 386 | 3662.873 | 1836.103 | 686.89 | 2408.441 | 2718.734 |
| 387 | 3676.135 | 1849.366 | 730.41 | 2421.704 | 2731.997 |

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|-----|----------|----------|---------|----------|----------|
| 388 | 3684.468 | 1857.698 | 757.74 | 2430.036 | 2740.329 |
| 389 | 3632.501 | 1744.724 | 587.25 | 2378.069 | 2688.362 |
| 390 | 3632.501 | 1744.724 | 587.25 | 2378.069 | 2688.362 |
| 391 | 3693.839 | 1867.07 | 788.49 | 2439.408 | 2749.7 |
| 392 | 3699.434 | 1872.664 | 806.84 | 2445.002 | 2755.295 |
| 393 | 3739.774 | 1913.004 | 939.19 | 2485.342 | 2795.635 |
| 394 | 3739.774 | 1913.004 | 939.19 | 2485.342 | 2795.635 |
| 395 | 3739.774 | 1913.004 | 939.19 | 2485.342 | 2795.635 |
| 396 | 3068.257 | 1275.555 | 1301.81 | 1399.762 | 2234.079 |
| 397 | 2993.053 | 1303.25 | 2187.28 | 1324.558 | 2158.875 |
| 398 | 2967.272 | 1277.469 | 2102.7 | 1298.777 | 2133.094 |
| 399 | 2906.668 | 1216.865 | 1903.86 | 1238.173 | 2072.49 |
| 400 | 3134.387 | 1360.929 | 1457.01 | 1465.891 | 2300.209 |
| 401 | 3192.927 | 1503.123 | 374.76 | 1524.431 | 2358.748 |
| 402 | 3202.227 | 1512.423 | 1005.27 | 1533.731 | 2368.048 |
| 403 | 3243.645 | 1553.841 | 1141.16 | 1575.15 | 2409.467 |
| 404 | 3076.189 | 1286.448 | 1266.07 | 1407.693 | 2242.01 |
| 405 | 2955.369 | 1265.566 | 2063.64 | 1286.874 | 2121.191 |
| 406 | 2941.755 | 1251.951 | 2018.98 | 1273.259 | 2107.577 |
| 407 | 3082.091 | 1308.633 | 1285.44 | 1413.595 | 2247.913 |
| 408 | 2940.163 | 1250.36 | 2013.75 | 1271.668 | 2105.985 |
| 409 | 3140.84 | 1451.036 | 303.87 | 1472.344 | 2306.661 |
| 410 | 2980.333 | 1290.529 | 2145.54 | 1311.837 | 2146.155 |
| 411 | 2430.519 | 820.492 | 825.53 | 725.79 | 1596.341 |
| 412 | 2367.107 | 819.572 | 822.51 | 662.379 | 1532.929 |
| 413 | 2314.157 | 755.956 | 613.8 | 609.428 | 1479.979 |
| 414 | 2302.819 | 744.618 | 576.6 | 598.09 | 1468.641 |
| 416 | 5364.513 | 768.886 | 521.56 | 4401.281 | 4665.117 |
| 417 | 5374.654 | 758.745 | 554.83 | 4411.422 | 4675.258 |
| 418 | 5364.659 | 768.741 | 522.04 | 4401.427 | 4665.263 |
| 419 | 5376.19 | 757.21 | 559.87 | 4412.958 | 4676.794 |
| 420 | 5318.16 | 815.24 | 369.48 | 4354.928 | 4618.764 |
| 421 | 5286.787 | 846.612 | 266.55 | 4323.555 | 4587.391 |
| 422 | 5251.498 | 881.902 | 150.78 | 4288.266 | 4552.102 |
| 423 | 5251.498 | 881.902 | 150.78 | 4288.266 | 4552.102 |
| 424 | 4449.096 | 688.262 | 981.32 | 3485.864 | 3749.7 |
| 425 | 4959.193 | 1174.206 | 787.94 | 3995.961 | 4259.797 |
| 426 | 4435.455 | 674.62 | 936.56 | 3472.223 | 3736.059 |
| 427 | 4445.965 | 685.13 | 971.04 | 3482.733 | 3746.569 |
| 428 | 4470.917 | 710.083 | 1052.91 | 3507.686 | 3771.521 |
| 429 | 4480.987 | 720.152 | 1085.94 | 3517.755 | 3781.591 |
| 430 | 4489.312 | 728.478 | 1113.26 | 3526.08 | 3789.916 |
| 431 | 4537.08 | 776.246 | 1269.98 | 3573.848 | 3837.684 |
| 432 | 5535.547 | 521.849 | 1332.05 | 4572.316 | 4836.152 |
| 433 | 5503.345 | 630.054 | 977.05 | 4540.113 | 4803.949 |
| 434 | 5499.928 | 486.229 | 1448.91 | 4536.697 | 4800.532 |
| 435 | 5404.574 | 728.825 | 652.99 | 4441.342 | 4705.178 |

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|-----|----------|----------|---------|----------|----------|
| 436 | 2556.503 | 858.017 | 568.25 | 1593.271 | 1882.154 |
| 437 | 2571.604 | 873.117 | 617.79 | 1608.372 | 1897.255 |
| 438 | 2414.122 | 730.138 | 148.7 | 1450.891 | 1739.774 |
| 439 | 3172.537 | 873.531 | 2613.52 | 2209.305 | 2498.188 |
| 440 | 3361.226 | 1062.221 | 758.76 | 2397.995 | 2686.878 |
| 441 | 3345.083 | 1046.078 | 705.8 | 2381.852 | 2670.735 |
| 442 | 3062.468 | 763.463 | 209.66 | 2099.237 | 2388.12 |
| 443 | 2982.146 | 683.14 | 587.51 | 2018.914 | 2307.797 |
| 444 | 2996.887 | 697.881 | 635.88 | 2033.655 | 2322.539 |
| 445 | 2899.169 | 600.163 | 1716.64 | 1935.937 | 2224.821 |
| 446 | 3023.529 | 724.523 | 723.28 | 2060.297 | 2349.18 |
| 447 | 2872.141 | 573.136 | 78.89 | 1908.91 | 2197.793 |
| 448 | 2920.981 | 621.975 | 239.12 | 1957.749 | 2246.633 |
| 449 | 2939.042 | 640.036 | 298.38 | 1975.81 | 2264.694 |
| 450 | 2974.857 | 675.852 | 415.88 | 2011.625 | 2300.509 |
| 451 | 3001.892 | 702.887 | 504.58 | 2038.661 | 2327.544 |
| 452 | 2990.824 | 691.818 | 468.27 | 2027.592 | 2316.476 |
| 453 | 3086.007 | 787.001 | 2329.63 | 2122.775 | 2411.659 |
| 454 | 3098.094 | 799.088 | 2369.28 | 2134.862 | 2423.745 |
| 455 | 3200.054 | 901.048 | 2703.79 | 2236.823 | 2525.706 |
| 456 | 2002.756 | 340.373 | 891.24 | 962.436 | 1223.453 |
| 457 | 2232.004 | 321.046 | 1305.69 | 1268.772 | 1557.656 |
| 458 | 1967.378 | 304.995 | 1463.03 | 1004.146 | 1293.03 |
| 459 | 1967.465 | 305.081 | 1463.31 | 1004.233 | 1293.116 |
| 460 | 1951.015 | 288.632 | 1409.34 | 987.783 | 1276.667 |
| 461 | 1998.026 | 335.642 | 1563.58 | 1034.794 | 1323.677 |
| 462 | 2233.11 | 312.305 | 1277.02 | 1269.878 | 1558.761 |
| 463 | 2270.224 | 555.528 | 1206.16 | 1306.992 | 1595.876 |
| 464 | 2319.724 | 523.898 | 869.72 | 1243.888 | 1504.904 |
| 465 | 2343.563 | 628.868 | 1446.78 | 1380.331 | 1669.215 |
| 466 | 2225.35 | 405.73 | 1583.53 | 1262.118 | 1551.001 |
| 467 | 2197.481 | 355.569 | 1418.96 | 1234.249 | 1523.133 |
| 468 | 2175.288 | 377.762 | 1491.77 | 1212.056 | 1500.94 |
| 469 | 2183.7 | 369.35 | 1464.17 | 1220.468 | 1509.351 |
| 470 | 2215.037 | 395.417 | 1549.69 | 1251.805 | 1540.688 |
| 471 | 2305.428 | 467.276 | 1055.48 | 1300.509 | 1561.526 |
| 472 | 2206.513 | 346.537 | 1389.32 | 1243.281 | 1532.164 |
| 473 | 2313.026 | 659.915 | 423.47 | 1107.871 | 1368.887 |
| 474 | 2214.234 | 507.78 | 1215.81 | 1251.003 | 1539.886 |
| 475 | 2265.786 | 687.416 | 268.48 | 1060.63 | 1321.647 |
| 476 | 2933.254 | 874.543 | 1865.2 | 874.543 | 2724.387 |
| 477 | 2942.654 | 883.942 | 1834.36 | 883.942 | 2714.987 |
| 478 | 2971.381 | 912.67 | 2008.35 | 912.67 | 2768.021 |
| 479 | 2890.24 | 831.529 | 1742.15 | 831.529 | 2686.881 |
| 480 | 2863.977 | 805.266 | 1655.98 | 805.266 | 2660.617 |
| 481 | 3056.882 | 998.171 | 1966.85 | 998.171 | 2868.169 |
| 482 | 3078.037 | 1019.326 | 17775.6 | 1019.326 | 2783.781 |

| | | | | | |
|-----|----------|----------|---------|----------|----------|
| 483 | 2960.742 | 902.031 | 1864.09 | 902.031 | 2901.075 |
| 484 | 3074.023 | 1015.312 | 1174.53 | 1015.312 | 3073.836 |
| 485 | 3194.977 | 1136.266 | 836.64 | 1136.266 | 3194.79 |
| 486 | 3208.947 | 1150.236 | 882.47 | 1150.236 | 3208.76 |
| 487 | 3522.751 | 1464.04 | 1881.04 | 1464.04 | 3479.238 |
| 488 | 3395.652 | 1336.941 | 1556.88 | 1336.941 | 3352.138 |
| 489 | 3334.304 | 1275.593 | 1355.61 | 1275.593 | 3290.791 |
| 490 | 3298.665 | 1239.954 | 1238.69 | 1239.954 | 3255.152 |
| 491 | 3043.674 | 664.652 | 1037.59 | 1139.997 | 2209.495 |
| 492 | 3027.002 | 647.98 | 1596.64 | 1176.208 | 2192.823 |
| 493 | 2712.365 | 333.343 | 564.37 | 938.18 | 1878.186 |
| 494 | 2906.253 | 527.232 | 1200.49 | 1055.459 | 2072.074 |
| 495 | 3152.513 | 773.491 | 869.07 | 1248.836 | 2318.334 |

APPENDIX B

Appendix B

Table: Actual and predicted house rent

| House_ID | Actual House Rent | Predicted Rent (Initial ANN model) | Predicted Rent (Best ANN Model) | Predicted Rent (Hedonic Pricing) |
|----------|-------------------|------------------------------------|---------------------------------|----------------------------------|
| 361 | 2000 | 2095.457 | 2139.558 | 2109.099 |
| 362 | 1500 | 2129.653 | 2243.425 | 2093.291 |
| 363 | 3000 | 2799.002 | 3420.819 | 2518.2 |
| 364 | 3500 | 2663.631 | 3371.545 | 2379.904 |
| 365 | 2500 | 2487.608 | 2111.354 | 2338.29 |
| 366 | 2000 | 1448.365 | 1616.816 | 1608.179 |
| 367 | 3000 | 2378.684 | 2404.431 | 2283.267 |
| 368 | 2800 | 2127.752 | 2476.738 | 2155.447 |
| 369 | 2500 | 2233.238 | 2604.8 | 2227.172 |
| 370 | 2200 | 1729.116 | 1815.628 | 1712.838 |
| 371 | 2000 | 1839.005 | 1876.987 | 1738.1 |
| 372 | 2500 | 2044.202 | 2094.515 | 1949.444 |
| 373 | 2700 | 2901.149 | 2793.303 | 2924.925 |
| 374 | 3000 | 2957.398 | 3269.689 | 2902.987 |
| 375 | 1200 | 1512.558 | 1594.539 | 1547.288 |
| 376 | 1800 | 2150.936 | 2145.229 | 2189.659 |
| 377 | 3200 | 2832.615 | 2765.376 | 2894.234 |
| 378 | 2000 | 2259.945 | 2392.595 | 2208.282 |
| 379 | 1500 | 2038.601 | 2064.716 | 1989.052 |
| 380 | 2800 | 3178.398 | 3485.036 | 3466.939 |
| 381 | 3300 | 3440.232 | 3547.105 | 3418.044 |
| 382 | 3000 | 3022.835 | 3115.296 | 3258.241 |
| 383 | 2100 | 2778.228 | 2564.641 | 2701.711 |
| 384 | 2300 | 2283.523 | 2373.757 | 2313.13 |
| 385 | 3200 | 3121.599 | 2920.644 | 3076.461 |
| 386 | 2800 | 2763.053 | 2912.314 | 2858.466 |
| 387 | 2600 | 3029.298 | 2904.222 | 2995.829 |
| 388 | 1300 | 2274.656 | 2293.22 | 2219.265 |
| 389 | 2400 | 2886.686 | 2881.055 | 2934.879 |
| 390 | 2500 | 2489.739 | 2067.958 | 2551.704 |
| 391 | 2800 | 1780.168 | 2051.816 | 1644.128 |
| 392 | 3000 | 2668.026 | 2491.595 | 2695.994 |
| 393 | 2900 | 2605.807 | 2435.427 | 2617.184 |
| 394 | 2600 | 3084.588 | 3041.957 | 3073.84 |
| 395 | 3100 | 2269.256 | 2012.87 | 2239.62 |
| 396 | 900 | 2375.491 | 2261.575 | 2368.881 |
| 397 | 1700 | 2507.433 | 2372.828 | 2520.523 |
| 398 | 2100 | 2207.188 | 2052.13 | 2195.316 |
| 399 | 2100 | 1999.829 | 1912.966 | 2002.563 |

| | | | | |
|-----|------|----------|----------|----------|
| 400 | 1800 | 2373.27 | 2293.767 | 2394.417 |
| 401 | 2400 | 2063.809 | 2357.602 | 2180.329 |
| 402 | 1500 | 2552.052 | 2616.528 | 2597.553 |
| 403 | 2500 | 3628.202 | 3541.062 | 4318.291 |
| 404 | 2500 | 2128.727 | 2242.046 | 2081.895 |
| 405 | 3000 | 2460.094 | 2614.327 | 2590.495 |
| 406 | 2000 | 1458.702 | 1522.353 | 1470.174 |
| 407 | 500 | 1208.191 | 1115.424 | 1255.428 |
| 408 | 2000 | 2246.629 | 2565.931 | 2231.783 |
| 409 | 3000 | 2445.291 | 2044.794 | 2335.695 |
| 410 | 2000 | 2214.729 | 1834.137 | 2162.471 |
| 411 | 2500 | 2369.608 | 1615.782 | 2315.593 |
| 412 | 3500 | 3002.441 | 2681.189 | 2798.919 |
| 413 | 1200 | 1526.415 | 1136.011 | 1556.134 |
| 414 | 2000 | 1445.677 | 1646.073 | 2040.287 |
| 415 | 1000 | 860.8999 | 1130.615 | 1095.497 |
| 416 | 1500 | 1964.974 | 1869.585 | 2057.052 |
| 417 | 3000 | 1952.486 | 1936.649 | 1832.337 |
| 418 | 2000 | 2103.843 | 1952.698 | 2176.365 |
| 419 | 400 | 1256.939 | 1030.201 | 1353.469 |
| 420 | 1200 | 2203.496 | 1757.727 | 2105.866 |
| 421 | 1500 | 1808.95 | 1583.956 | 1786.49 |
| 422 | 2000 | 2806.95 | 2473.325 | 2767.461 |
| 423 | 2500 | 1795.193 | 1721.625 | 1781.435 |
| 424 | 3000 | 2228.165 | 2091.755 | 2194.886 |
| 425 | 2500 | 2600.213 | 2757.576 | 2651.33 |
| 426 | 1500 | 1887.565 | 1604.013 | 1881.173 |
| 427 | 1900 | 2315.399 | 1529.362 | 2364.676 |
| 428 | 2500 | 2230.608 | 2297.541 | 2191.734 |
| 429 | 1200 | 1658.447 | 1166.899 | 1623.72 |
| 430 | 800 | 1357.973 | 709.1577 | 1356.287 |
| 431 | 2600 | 2128.31 | 2249.957 | 2102.996 |
| 432 | 1500 | 1917.413 | 2400.191 | 1765.833 |
| 433 | 600 | 600.9938 | 892.1793 | 799.8159 |
| 434 | 600 | 516.1232 | 636.8037 | 532.0384 |
| 435 | 800 | 704.3817 | 761.4359 | 929.8795 |
| 436 | 600 | 383.49 | 522.9702 | 539.693 |
| 437 | 300 | 442.0874 | 530.0228 | 577.8313 |
| 438 | 1000 | 851.5492 | 919.4736 | 744.1374 |
| 439 | 3500 | 2773.722 | 2663.233 | 2721.083 |
| 440 | 1300 | 1205.558 | 1205.966 | 1173.009 |
| 441 | 1500 | 3413.033 | 1512.329 | 3491.488 |
| 442 | 2000 | 1982.788 | 1754.134 | 1855.096 |
| 443 | 1800 | 1624.371 | 1333.905 | 1534.142 |
| 444 | 1000 | 1338.228 | 1250.435 | 1694.689 |
| 445 | 1600 | 1569.588 | 1405.691 | 1775.168 |
| 446 | 2200 | 2800.508 | 3113.173 | 2753.328 |

| | | | | |
|-----|------|----------|----------|----------|
| 447 | 2500 | 1518.363 | 1683.198 | 1553.939 |
| 448 | 1700 | 1301.982 | 1370.51 | 1397.471 |
| 449 | 800 | 910.5846 | 827.5762 | 955.6391 |
| 450 | 1500 | 1232.491 | 1350.578 | 1148.38 |
| 451 | 800 | 631.7795 | 916.1721 | 566.9257 |
| 452 | 1000 | 1117.987 | 1285.915 | 1090.998 |
| 453 | 1600 | 1236.153 | 1383.453 | 1241.536 |
| 454 | 2500 | 2150.32 | 2697.199 | 2310.931 |
| 455 | 1000 | 1200.577 | 1394.499 | 1205.451 |
| 456 | 1500 | 1223.109 | 1362.544 | 1209.643 |
| 457 | 1200 | 1094.713 | 1287.737 | 1164.278 |
| 458 | 2000 | 1599.828 | 1656.014 | 1624.586 |
| 459 | 3800 | 2788.399 | 3296.481 | 2776.608 |
| 460 | 1500 | 1339.93 | 1211.872 | 1547.835 |
| 461 | 1200 | 1273.842 | 1299.936 | 1451.346 |
| 462 | 1800 | 1489.317 | 1416.017 | 1395.255 |
| 463 | 1200 | 1429.319 | 1247.178 | 1681.05 |
| 464 | 2000 | 1734.042 | 1828.5 | 2028.451 |
| 465 | 1200 | 521.3929 | 764.2921 | 944.1941 |
| 466 | 2000 | 1802.129 | 1609.699 | 1905.977 |
| 467 | 3000 | 3299.787 | 2909.854 | 3267.702 |
| 468 | 2000 | 2101.537 | 1925.979 | 2184.423 |
| 469 | 1200 | 1013.92 | 1227.677 | 1383.543 |
| 470 | 2000 | 1830.635 | 1345.119 | 1779.39 |
| 471 | 1200 | 1276.154 | 969.1458 | 1226.763 |
| 472 | 900 | 997.6525 | 766.1116 | 815.5585 |
| 473 | 6000 | 3853.721 | 3388.567 | 3414.564 |
| 474 | 2000 | 1933.464 | 1794.641 | 1948.439 |
| 475 | 1500 | 1686.935 | 2022.746 | 1795.176 |
| 476 | 4400 | 2759.308 | 2785.064 | 2759.848 |
| 477 | 3000 | 2438.756 | 2459.633 | 2429.429 |
| 478 | 2000 | 2006.456 | 1761.449 | 1985.23 |
| 479 | 2500 | 2792.88 | 2694.929 | 2697.776 |