## BANGLADESH UNIVERSITY OF ENGINEERING AND TECHNOLOGY, DHAKA

L-3/T-2 $\quad$ B. Sc. Engineering Examinations 2016-2017
Sub : IPE 303 (Product Design I)
Full Marks: 210
Time: 3 Hours
USE SEPARATE SCRIPTS FOR EACH SECTION
The figures in the margin indicate full marks.

## SECTION - A

There are FOUR questions in this section. Answer any THREE.

1. (a) An arm is welded to a hollow shaft at section ' 1 '. The hollow shaft is welded to a plate C at section ' 2 '. The arrangement is shown in Fig 1(a) with dimensions. A force of $\mathrm{P}=15 \mathrm{kN}$ acts at arm A perpendicular to the axis of the arm. Calculate the size of weld at section ' 1 ' and ' 2 '. The permissible shear stress in the weld is 120 MPa .

fig.1(a)
(b) A bracket in the form of a plate is fitted to a column by means of four rivets $\mathrm{A}, \mathrm{B}$, $C$ and $D$ in the same vertical line, as shown in Fig $1(b) . A B=B C=C D=60 \mathrm{~mm}$. $E$ is the mid-point of BC . A load of 100 kN is applied to the bracket at a point of F which is at horizontal distance of 150 m from E . The load acts at an angle of $30^{\circ}$ to the horizontal. Determine the diameter of the rivets which are made of steel having a yield stress in shear of 240 MPa . Take a factor of safety of 1.5 . What would be the thickness of the plate taking an allowable bending stress of 125 MPa for the plate, assuming its total width at section $A B C D$ as 240 mm .


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2. (a) A hollow shaft of 0.5 m outside diameter and 0.3 m inside diameter is used to drive a propeller of a marine vessel. The shaft is mounted on bearings 6 m apart and it transmits 5600 kW at 150 r.p.m. The maximum axial propeller thrust is 500 kN and shaft weights 70 kN . Determine
$(8+5+4+4+5)$
(i) The maximum shear stress developed in the shaft
(ii) The lateral deflection using Castigliano's theorem.
(iii) The angular twist between the bearings.
(iv) What would be its first critical speed? Assume, Young's modulus 180 GPa and density $1000 \mathrm{~kg} / \mathrm{m}^{3}$.
(v) Including all of the above considerations in constraints, formulate an optimization problem so that cost of manufacturing the shaft will be minimized.
(b) The hydraulic cylinder 400 mm bore operated at a maximum pressure of $5 \mathrm{~N} / \mathrm{mm}^{2}$ as shown in Fig. 2 (b). The piston rod is connected to the load and the cylinder to the frame through hinged joints. Design: Cylinder, Piston rod and Hinge pin.

3. (a) A pulley is keyed to a shaft midway between two bearings. The shaft is made of cold drawn steel for which the ultimate strength is 550 MPa and the yield strength is 400 MPa . The bending moment at the pulley varies from $-150 \mathrm{~N}-\mathrm{m}$ to $+400 \mathrm{~N}-\mathrm{m}$ as the torque on the shaft varies from $-50 \mathrm{~N}-\mathrm{m}$ to $+150 \mathrm{~N}-\mathrm{m}$. Determine the diameter of the shaft for a life of at least $10^{7}$ cycles using distortion energy theorem. The stress concentration factors for the keyway at the pulley in bending and in torsion are 1.6 and 1.3 respectively.

Take the following values:
Factor of safety $=1.5$
Load correction factors $=1.0$ in normal loading and 0.6 in shear loading
Size effect factor $=0.85$
Surface effect factor $=0.88$

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## Contd... Q. No. 3

(b) A toggle jack as shown in Fig.3(b), is to be designed for lifting a load of 4 kN . When the jack is in the top position, the distance between the center lines of nuts is 50 mm and, in the bottom position this distance is 210 mm . the eight links of the jack are symmetrical and 110 mm long. The link pins in the base are set 30 mm apart. The links, screw and pins are made from mild steel for which the permissible stresses are 100 MPa in tension and 50 MPa in shear. The bearing pressure of the pins is limited to $20 \mathrm{~N} / \mathrm{mm}^{2}$. Assume the pitch of the square threads as 6 mm and the coefficient of friction between threads as 0.20 .

4. (a) The constructional details of an exhaust valve of a diesel engine are shown in Fig. 4(a). The diameter of the valve is 32 mm and the suction pressure in the cylinder is $0.03 \mathrm{~N} / \mathrm{mm}^{2}$. The mass of the valve is 50 gm . The maximum valve lift is 10 mm . The stiffness of the spring for the valve is $10 \mathrm{~N} / \mathrm{mm}$. The spring index can be assumed as 8 . (4+2+12)
(i) What is the function of rocker arm and push rod?
(ii) What type of spring actually used?
(iii) Neglecting the effect of inertia forces, design the spring for static consideration and determine the factor of safety for fatigue loading after defining the actual reason for fatigue loading considerations.


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## Contd... Q. No. 4(a)

Consider, oil-hardened and tempered spring steel wire is used and relationship between wire diameter and minimum tensile strength can be perceived from following data.

| Wire diameter <br> $d(m m)$ | Minimum tensile strength $\mathrm{N} / \mathrm{mm}^{2}$ |  |
| :---: | :---: | :---: |
|  | SW | VW |
| 2.0 | 1620 | 1520 |
| 2.5 | 1570 | 1470 |
| 3.0 | 1520 | 1430 |
| 3.6 | 1480 | 1400 |
| 4 | 1480 | 1400 |

(b) A cantilever beam is supported as shown in Fig 4(b) to be used for a particular purpose. Suppose, the beam is immersed on the river and the river water is flowing at different velocity at different layer from the bottom. Suppose that, the force distribution from bottom to top of the river, follows a triangular distribution with peak value 500 N . The attacking force on the initial point of the beam, where the beam is attached to the vertical support is 50 N . Suddenly, a garbage of 80 kg falls on the outer most extreme point vertically. Design the diameter of the beam if the projection of the beam on the river is $10 \sqrt{2} \mathrm{~m}$ and inclined at 45 degrees with the river bed. Consider, the beam is made of steel 45 C 8 with a tensile yield strength of $380 \mathrm{~N} / \mathrm{mm}^{2}$. The factor safety is 2.5 .

(c) What do you mean by critical frequency of helical spring? Derive mathematical equation for it.

## SECTION-B

There are FOUR questions in this section. Answer any THREE questions.
5. (a) You are responsible for arranging a design team for the development of a new brand of food product for your company. Mention any six individuals whom you should incorporate in your team, and elaborate their roles.

## IPE 303

## Contd... Q. No. 5

(b) Discuss the 'Specification Development' phase of the product design process for a company who are planning to launch a new model of family sedan car.
(c) Explain Function, Sub-function and Constraint, using digital SLR camera as an example.
(d) Briefly describe the working mechanism and design consideration of diaphragm spring of a single plate dry clutch with necessary schematic diagrams.
6. (a) The basic QFD methodology involves four basic phases - Explain each phases with appropriate example.
(b) Justify the four purposes of prototype to a multinational company who are designing a new version of smart phone.
(c) Formulate torque transmission capacity equation of semi-centrifugal clutch with necessary schematic diagrams.
(d) Write a short note on "Design for Manufacturing".
7. (a) What are the steps to identify customer needs? Explain each step with example.
(b) Explain the 'FAST method' for functional decomposition.
(c) Compare the traditional and concurrent engineering approaches of product development.
(d) i) A $15 \mathrm{~kW}, 960 \mathrm{r} . \mathrm{p} . \mathrm{m}$. motor has a mild steel of 40 mm diameter and the extension being 75 mm . The permissible shear and crushing stresses for mild steel key are 56 MPa and 112 MPa respectively. Design the keyway in the motor shaft extension. Check the shear strength of the key against normal strength of the shaft.
(ii) Differentiate between Gib-head taper key and woodruff key with necessary diagrams. Also mention their application differences.
8. (a) Write a short note on 'Function Analysis System Technique'.
(b) For a ready-made garments factory, discuss the possible advantages of implementing ISO 14000 EMS.
(c) What are the steps for subtract and operate procedure? Draw a function tree for a blender using subtract and operate procedure and explain.
(d) Draw the following components and write down the purpose of using them.
(i) Multi-Leaf spring
(ii) Setscrews
(iii) Retaining ring

## BANGLADESH UNIVERSITY OF ENGINEERING AND TECHNOLOGY, DHAKA

## L-3/T-2 B. Sc. Engineering Examinations 2016-2017

Sub : IPE 319 (Quality Management)
Full Marks: 210
Time : 3 Hours
USE SEPARATE SCRIPTS FOR EACH SECTION
The figures in the margin indicate full marks.

## SECTION - A

There are FOUR questions in this section. Answer any THREE questions.

1. (a) In the new version of ISO9000:2015, some changes are explicit. What are the explicit changes with respect to "Product", "risk" "six compulsory procedures" and "document and Records"?
(b) What will be the defect rate in case of $3 \sigma$ limit and process control with $1.5 \sigma$ shift in process mean? Compute defect rate using appropriate and comprehensive diagram.
2. (a) Which " $S$ ", in $5 S$ philosophy, is the most difficult to implement and achieve? Explain this " S ".
(b) What are the three kinds of losses which may take place as per Taguchi Loss Function? Explain with necessary diagrams (if any).
3. (a) According to Juran, $100 \%$ good quality level may not be of interest to the company in terms of cost. If this is true, then zero defect concept is not economically beneficial. Do you agree? Justify with schematic diagrams.
(b) What are the four phases (or stages or steps) in the complete Quality Function Development (QFD) methodology? Explain with appropriate diagram.
4. (a) What is Risk Priority Number in FMEA analysis? Define and explain.
(b) For the following combinatorial matrix, fill in the ANOVA table (attached in the question paper) and find Red X and Pink X factors. Afterwards, attach the filled in ANOVA table to Section-A of your answer script.


## IPE 319

## SECTION-B

There are FOUR questions in this section. Answer any THREE questions.
5. (a) List and explain at least five advantages of control charts.
(b) Discuss the Phase I and Phase II of control chart application.
(c) What are the types of variable charts? When $\bar{x}-\mathrm{S}$ chart should be used rather than $\bar{x}-\mathrm{R}$ chart?
(d) A control chart indicates that the current process fraction nonconforming is 0.02 . If 50 items are inspected each day, what is the probability of detecting a shift in the fraction nonconforming to 0.04 on the first day after the shift and by the end of the third day following the shift?
6. (a) Discuss the operating-characteristic function of $\bar{x}$ and R chart. Define 'Average Run Length' and 'Average Time to Signal' for the $\bar{x}$ Chart.
(b) Explain the performance advantages of CUSUM and Weighted average charts relative to Shewhart control chart.
(c) A normally distributed quality characteristic is controlled by $\bar{x}$ and R charts having the following parameters ( $n=4$, both charts are in control):

| R Chart | $\bar{x}$ Chart |
| :--- | :--- |
| UCL $=18.795$ | UCL $=626$ |
| Center line $=8.236$ | Center line $=620$ |
| LCL $=0$ | LCL $=614$ |

(i) What is the estimated standard deviation of the quality characteristic $x$ ?
(ii) If specifications are $610 \pm 15$, what is your estimate of the fraction of nonconforming material produced by this process when it is in control at the given level?
(iii) Suppose you wish to establish a modified chart to substitute for the original chart. The process mean is to be controlled so that the fraction nonconforming is less than 0.005 . The probability of type I error is to be 0.01 . What control limits do you recommend?
(d) Suppose that a stable process has upper and lower specifications at USL $=62$ and $\mathrm{LSL}=38$. A sample of size $\mathrm{n}=20$ from this process reveals that the process mean is centered approximately at the midpoint of the specification interval and that the sample standard deviation $s=1.75$. Find a $95 \%$ confidence interval on Cp .

## IPE 319

## Contd... Q. No. 7

7. (a) Discuss the Markov Chain Approach to Finding the ARLs for CUSUM and EWMA Control Charts.
(b) Explain the gauge and measurement system capability studies.
(c) The tensile strength and diameter of a textile fiber are two important quality characteristics that are to be jointly controlled. The quality engineer has decided to use $\mathrm{n}=10$ fiber specimens in each sample. He has taken 20 preliminary samples, and on the basis of these data he concludes that $\overline{\overline{x_{1}}}=115.59 \mathrm{psi}, \overline{\overline{x_{2}}}=1.06\left(\times 10^{-2}\right)$ inch, $\bar{s}_{1}^{2}=1.23,{\overline{s_{2}}}^{2}=0.83$ and $\overline{s_{12}}=0.79$. Write down the statistic of a $\mathrm{T}^{2}$ control chart that can be used for process control purpose. Calculate the UCL if $\alpha=0.001$. (Use $\mathrm{F}_{0.001,2,179}=7.18$ ).
(d) Define $\mathrm{C}_{\mathrm{p}}, \mathrm{C}_{\mathrm{pk}}$ and k . Mention the relationship equation among these indices.
8. (a) Write a short note on DMAIC model for improvement.
(b) Explain the Multivariate EWMA control chart.
(c) What are the major aspects of lean manufacturing?

## Cumulative Poisson Distribution Table

Table shows cumulative probability functions of Poisson Distribution with various $\alpha$. Example: to find the probability $\mathrm{P}(\mathrm{X} \leq 3)$ where X has a Poisson Distribution with $\alpha=2$, look in row 4 and column 4 to find $P(X \leq 3)=0.8571$ where $X$ is Poisson(2).

|  |  |  |  | $\alpha$ |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| x | 0.5 | 1 | 1.5 | 2 | 2.5 | 3 | 3.5 | 4 | 4.5 | 5 |
| 0 | 0.6065 | 0.3679 | 0.2231 | 0.1353 | 0.0821 | 0.0498 | 0.0302 | 0.0183 | 0.0111 | 0.0067 |
| 1 | 0.9098 | 0.7358 | 0.5578 | 0.4060 | 0.2873 | 0.1991 | 0.1359 | 0.0916 | 0.0611 | 0.0404 |
| 2 | 0.9856 | 0.9197 | 0.8088 | 0.6767 | 0.5438 | 0.4232 | 0.3208 | 0.2381 | 0.1736 | 0.1247 |
| 3 | 0.9982 | 0.9810 | 0.9344 | 0.8571 | 0.7576 | 0.6472 | 0.5366 | 0.4335 | 0.3423 | 0.2650 |
| 4 | 0.9998 | 0.9963 | 0.9814 | 0.9473 | 0.8912 | 0.8153 | 0.7254 | 0.6288 | 0.5321 | 0.4405 |
| 5 | 1.0000 | 0.9994 | 0.9955 | 0.9834 | 0.9580 | 0.9161 | 0.8576 | 0.7851 | 0.7029 | 0.6160 |
| 6 | 1.0000 | 0.9999 | 0.9991 | 0.9955 | 0.9858 | 0.9665 | 0.9347 | 0.8893 | 0.8311 | 0.7622 |
| 7 | 1.0000 | 1.0000 | 0.9998 | 0.9989 | 0.9958 | 0.9881 | 0.9733 | 0.9489 | 0.9134 | 0.8666 |
| 8 | 1.0000 | 1.0000 | 1.0000 | 0.9998 | 0.9989 | 0.9962 | 0.9901 | 0.9786 | 0.9597 | 0.9319 |
| 9 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.9997 | 0.9989 | 0.9967 | 0.9919 | 0.9829 | 0.9682 |
| 10 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.9999 | 0.9997 | 0.9990 | 0.9972 | 0.9933 | 0.9863 |
| 11 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.9999 | 0.9997 | 0.9991 | 0.9976 | 0.9945 |
| 12 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.9999 | 0.9997 | 0.9992 | 0.9980 |
| 13 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.9999 | 0.9997 | 0.9993 |
| 14 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.9999 | 0.9998 |
| 15 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.9999 |
| 16 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |

For Question 4b: Fill in the following ANOVA table and attach: , it to Section-A of answer script

| Cell group | Factors |  |  |  | 2 factors interactions |  |  |  |  |  | 3 factors interactions |  |  |  | 4 factors | ut |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | AB | AC | BC | AD | BD | CD | ABC | ABD | ACD. | BCD | ABCD |  |
| 1 | - | - | - | - | + | $\pm$ | + | + | + | + | - | - | - | - | + |  |
| 2 | + | - | - | - | - | - | + | - | + | $+$ | + | $+$ | + | - | - |  |
| 3 | - | + | - | - | - | + | - | + | - | + | $+$ | + | - | + | - |  |
| 4 | + | + | - | - | $+$ | - | - | - | - | + | - | - | $+$ | $+$ | $+$ |  |
| 5 | - | - | + | - | + | - | - | + | + | - | + | - | + | $+$ | - |  |
| 6 | $+$ | - | + | - | - | + | - | - | + | - | - | + | - | + | + |  |
| 7 | - | $+$ | + | - | - | - | + | + | - | - | - | + | + | - | + |  |
| 8 | $+$ | + | + | - | + | + | + | - | - | - | $+$ | - | - | - | - |  |
| 9 | - | - | - | + | + | + | + | - | - | - | - | + | $+$ | + | - |  |
| 10 | + | - | - | $+$ | - | - | + | + | - | - | + | - | - | + | + |  |
| 11 | - | + | - | + | - | $+$ | - | - | + | - | + | - | + | - | + |  |
| 12 | + | + | - | $+$ | $+$ | - | - | + | + | - | - | + | - | - | - |  |
| 13 | - | - | + | + | + | - | - | - | - | + | + | + | - | - | + |  |
| 14 | + | - | + | + | - | + | - | + | - | + | - | - | + | - | - |  |
| 15 | - | + | + | + | - | - | $+$ | - | $+$ | + | - | - | - | + | - |  |
| 16 | $+$ | + | + | $+$ | + | + | + | + | $+$ | + | + | + | + | + | + |  |
| Main and interaction contribution | 49 | 67 | -65 |  | 71 | -77 | $\begin{gathered} \overline{-} \\ 159 \end{gathered}$ |  | $\stackrel{-}{103}$ | 77 | -115 |  | 61 | 79 | 183 |  |

Table B. Factors used in $3 \sigma$ Quality Control Charts.

| Sample size $n$ |  | $\bar{X}$ charts |  | $S$ charts |  |  |  |  | $R$ charts |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Factors for control limits |  |  | Factors for central line | Factors for control limits |  |  |  | Factors <br> for central line | Factors for control limits |  |  |  |  |
|  | A | $\mathrm{A}_{2}$ | $\mathrm{A}_{3}$ | $\mathrm{C}_{4}$ | $\mathrm{B}_{3}$ | $\mathrm{B}_{4}$ | $\mathrm{B}_{5}$ | $\mathrm{B}_{6}$ | $\mathrm{d}_{2}$ | $\mathrm{d}_{3}$ | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ |
| 2 | 2.121 | 1.880 | 2.659 | 0.7979 | 0 | 3.267 | 0 | 2.606 | 1.128 | 0.853 | 0 | 3.686 | 0 | 3.267 |
| 3 | 1.732 | 1.023 | 1.954 | 0.8862 | 0 | 2.568 | 0 | 2.276 | 1.693 | 0.888 | 0 | 4.358 | 0 | 2.574 |
| 4 | 1.500 | 0.729 | 1.628 | 0.9213 | 0 | 2.266 | 0 | 2.088 | 2.059 | 0.880 | 0 | 4.698 | 0 | 2.282 |
| 5 | 1.342 | 0.577 | 1.427 | 0.9400 | 0 | 2.089 | 0 | 1.964 | 2.326 | 0.864 | 0 | 4.918 | 0 | 2.114 |
| 6 | 1.225 | 0.483 | 1.287 | 0.9515 | 0.030 | 1.970 | 0.029 | 1.874 | 2.534 | 0.848 | 0. | 5.078 | 0 | 2.004 |
| 7 | 1.134 | 0.419 | 1.182 | 0.9594 | 0.118 | 1.882 | 0.113 | 1.806 | 2.704 | 0.833 | 0.204 | 5.204 | 0.076 | 1.924 |
| 8 | 1.061 | 0.373 | 1.099 | 0.9650 | 0.185 | 1.815 | 0.179 | 1.751 | 2.847 | 0.820 | 0.388 | 5.306 | 0.136 | 1.864 |
| 9 | 1.000 | 0.337 | 1.032 | 0.9693 | 0.239 | 1.761 | 0.232 | 1.707 | 2.970 | 0.808 | 0.547 | 5.393 | 0.184 | 1.816 |
| 10 | 0.949 | 0.308 | 0.975 | 0.9727 | 0.284 | 1.716 | 0.276 | 1.669 | 3.078 | 0.797 | 0.687 | 5.469 | 0.223 | 1.777 |
| 11 | 0.905 | 0.285 | 0.927 | 0.9754 | 0.321 | 1.679 | 0.313 | 1.637 | 3.173 | 0.787 | 0.811 | 5.535 | 0.256 | 1.744 |
| 12 | 0.866 | 0.266 | 0.886 | 0.9776 | 0.354 | 1.646 | 0.346 | 1.610 | 3.258 | 0.778 | 0.922 | 5.594 | 0.283 | 1.717 |
| 13 | 0.832 | 0.249 | 0.850 | 0.9794 | 0.382 | 1.618 | 0.374 | 1.585 | 3.336 | 0.770 | 1.025 | 5.647 | 0.307 | 1.693 |
| 14 | 0.802 | 0.235 | 0.817 | 0.9810 | 0.406 | 1.594 | 0.399 | 1.563 | 3.407 | 0.763 | 1.118 | 5.696 | 0.328 | 1.672 |
| 15 | 0.775 | 0.223 | 0.789 | 0.9823 | 0.428 | 1.572 | 0.421 | 1.544 | 3.472 | 0.756 | 1.203 | 5.741 | 0.347 | 1.653 |
| 16 | 0.750 | 0.212 | 0.763 | 0.9835 | 0.448 | 1.552 | 0.440 | 1.526 | 3.532 | 0.750 | 1.282 | 5.782 | 0.363 | 1.637 |
| 17 | 0.728 | 0.203 | 0.739 | 0.9845 | 0.466 | 1.534 | 0.458 | 1.511 | 3.588 | 0.744 | 1.356 | 5.820 | 0.378 | 1.622 |
| 18 | 0.707 | 0.194 | 0.718 | 0.9854 | 0.482 | 1.518 | 0.475 | 1.496 | 3.640 | 0.739 | 1.424 | 5.856 | 0.391 | 1.608 |
| 19 | 0.688 | 0.187 | 0.698 | 0.9862 | 0.497 | 1.503 | 0.490 | 1.483 | 3.689 | 0.734 | 1.487 | 5.891 | 0.403 | 1.597 |
| 20 | 0.671 | 0.180 | 0.680 | 0.9869 | 0.510 | 1.490 | 0.504 | 1.470 | 3.735 | 0.729 | 1.549 | 5.921 | 0.415 | 1.585 |
| 21 | 0.655 | 0.173 | 0.663 | 0.9876 | 0.523 | 1.477 | 0.516 | 1.459 | 3.778 | 0.724 | 1.605 | 5.951 | 0.425 | 1.575 |
| 22 | 0.640 | 0.167 | 0.647 | 0.9882 | 0.534 | 1.466 | 0.528 | 1.448 | 3.819 | 0.720 | 1.659 | 5.979 | 0.434 | 1.566 |
| 23 | 0.626 | 0.162 | 0.633 | 0.9887 | 0.545 | 1.455 | 0.539 | 1.438 | 3.858 | 0.716 | 1.710 | 6.006 | 0.443 | 1.557 |
| 24 | 0.612 | 0.157 | 0.619 | 0.9892 | 0.555 | 1.445 | 0.549 | 1.429 | 3.895 | 0.712 | 1.759 | 6.031 | 0.451 | 1.548 |
| 25 | 0.600 | 0.153 | 0.606 | 0.9896 | 0.565 | 1.435 | 0.559 | 1.420 | 3.931 | 0.708 | 1.806 | 6.056 | 0.459 | 1.541 |



Table A. Standard Normal Distribution Values (Areas under the normal curve).


| Z | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0/09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| 0.1 | 0:0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| 0.2 | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | 0.1026 | 0.1064 | 0.1103 | 0.1141 |
| 0.3 | 0.1179 | 0.1217 | 0.1255 | 0.1293 | 0.1331 | 0.1368 | 0.1406 | 0.1443 | 0.1480 | 0.1517 |
| 0.4 | 0.1554 | 0.1591 | 0.1628 | 0.1664 | 0.1700 | 0.1736 | 0.1772 | 0.1808 | 0.1844 | 0.1879 |
| C. 5 | 0.1915 | 0.9950 | 0.1985 | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2995 | 0.3023 | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | 0.3159 | 0.3186 | 0.3212 | 0.3238 | 0.3264 | 0.3289 | 0.3315 | 0.3340 | 0.3365 | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| 1.1 | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | $0.3749^{\text { }}$ | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| . 1.2 | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 . | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 . | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| 2.1 | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| 2.2 | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 . | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| 2.3 | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| 2.6 | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4954 |
| 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 . |
| 2.9 | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 30 | 0.4987 | 04987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |

IPE $319=8=$


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Table 4-Standard Normal Distribution


| 2 | . 09 | . 08 | . 07 | . 06 | . 05 | 04 | 03 | 12 | . 01 | . 00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -3.4 | .0002 | . 0003 | 0003 | 0003 | 0003 | . 0003 | 0003 | 0003 | 3 | 3 |
| -3.3 | 0003 | 0004 | 0004 | 0004 | 0004 | 0004 | 0004 | 0005 | .0005: | 0005 |
| -3.2 | . 0005 | . 0005 | . 0005 | . 0006 | 0006 | 0006 | 0006 | 0006 | . 0007 | 0007 |
| -3.1 | \% 00007 | . 00007 | . 0000 | 0008 | 0008 | 0008 | 0009 | . 0009 | 0009 | 0010 |
| -3.0 | . 0010 | 0010 | 0011 | 0011 | 0011 | 0012 | 0012 | 0013 | 0013 | 0013 |
| -2.9 | $\because .0014$ | 0014 | 0015 | 0015 | 0016 | 0016 | 0017 | .001) | 0018 | 0019 |
| -2.8 | . 0079 | 0020 | 0021 | . 0021 | 0022 | 0023 | . 0023 | . 0024 | 0025 | 0026 |
| -2.7 | $\therefore 0026$ | 0027 | 0028 | . 0029 | 0030 | 0031 | 0032 | 0033 | 0034 | .0035: |
| $-2.6$ | . 0036 | 0037 | . 0038 | 0039 | 0040 | 0041 | . 0043 | 0044 | 0045 | 0047 |
| -2.5 | . 0048 | 0049 | 0051 | 0032 | 0054 | 0055 | 0057 | 0059 | 0060 | $0062 \%$ |
| -2.4 | . 0064 | . 0066 | . 0068 | 0069 | 0071 | 0073 | 0075 | 0078 | 0080 | 0082 |
| $\cdots-2.3$ | . 0084 | 0087 | . 0089 | 0091 | 0094 | 0096 | 0099 | 0102 | 0104 | 0107 |
| -2.2 | . 0110 | 0113 | 0116 | 0119 | 0122 | 0125 | . 0129 | 0132 | 0136 | 0139 |
| $-2.1$ | . 0143 | 0146 | 0150 | 0154 | . 01585 | 0162 | 0166 | 0170 | 0174 | .0179: |
| -2.0) | . 0183 | . 0188 | 0192 | 0197 | . 0202 | . 0207 | . 0212 | . 0217 | . 0222 | 0228 |
| . 9 | 0233 | 0239 | 0244 | 0250 | 0256 | 0262 | 0268 | 0274 | . $0281{ }^{\circ}$ | 0287. |
| -1.8 | . 0294 | . 0301 | . 0307 | 0314 | . 0322 | 0329 | . 0336 | . 0344 | . 0352 | 0359 |
| -1.7 | . 0367 | . 0375 | 0384 | 0392: | . 04011 | 0409 | . 0418 | . 0427 | .0436. | . 0446 |
| -1.6 | . 0455 | . 0465 | . 0475 | . 0485 | . 0495 | 0505 | 0516 | . 0526 | 0537 | . 0548 |
| $-1.5$ | . 0559 | 00571 | 0582 | . 0594 | 0606 | 0618 | 0630 | 0643 | . 06555 | 0668 |
| -1.4 | . 0681 | . 0694 | . 0708 | . 0722 | . 0735 | 0749 | 0764 | 0778 | 0793 | . 0808 |
| $-1.3$ | . 0823 | . 0838 | 0853 | 0869 | 0885 | 0901 | 0918. | 0934 | 0951 | 0968 \% |
| -1.2 | . 0985 | 1003 | 1020 | 1038 | 1056 | 1075 | 1093 | 1112 | 1131 | 1151 |
| $-1.1$ | . 11370 | 1190 | 1210 | 1230 | 1251 | 1271 | 1292 | 1314 | 1335 | 1357 |
| $-1.0$ | . 1379 | . 1401 | 1423 | 1446 | 1469 | 1492 | 1515 | 1539 | 1562 | 1587 |
| $0.9$ | 161 | 1635 | 1660 | 1685 | 1711 | 1736 | 1762 | 1788 | $1814 \times$ | 18419 |
| $-0.8$ | 1867 | . 1894 | 1922 | 1949 | 1977 | 2005 | 2033 | 2061 | 2090 | 2119 : |
| $0^{-0.0}$ | $\bigcirc 2148$ | 2177 | 2206 | 2236 | 2266 | 2296 | 2327 | 23.58 | 2389.' | 2420 |
| -0.6 | . 2451 | . 2483 | . 2514 | 2546 | 2578 | 2611 | 2643 | 2676 | . 2709 | 2743 |
| $\bigcirc$ | 2776 ${ }^{\circ}$ | $\therefore 2810{ }^{-1}$ | 2843 | 2877 |  | 2946 | $2981{ }^{\circ}$ | 3015 |  | . 3055 |
| $-0.4$ | 3121 | 3156 | .3192 | 3228 | 3264 | 3300 | 333 | 3372 | 3409 | 3446 |
| -0.3 | $\bigcirc 3483$ | $3520^{\circ}$ | 3557 | 3594 | 3632 | 3669 | 300 | 374 | 3783: | 3821. |
| -0.2 | 3859 | . 3897 | . 3936 | 3974 | 4013 | 4052 | 4090 | 4129 | 4165 | 02 |
| - -0.1 | $\therefore 4247$. | 4286 | 4325 | 14364: | 4404 | 4443 | 4483 | 4522 | 4562 | 4602 |
| -0.0 | . 4641 | . 4681 | 4721 | 4761 | 4801 | . 4840 | 4880 | 4920 | 4960 | . 5000 |



## IPE $319=9=$

```
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```

Table 4-Standard Normal Distribution (continued)


| $z$ | . 017 | . 01 | . 12 | . 03 | . 04 | . 05 | . 06 | . 17 | . 08 | . 09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (1.0) | 5000 | 5040 | . 5080 | 5120 | 5160 | . 5199 | 5239 | 5279 | . 5319 |  |
| 0.1 | . 5398 | . 5438 | 5478 | 5517 | 5 |  | 5636 |  |  | 3 |
| 0.2 | . 5793 | 58.32 | . 5871 | 5910 | . 5948 | 5987 | 6026 | 6064 | 6103 | 41 |
| 0.3 | - 6779 | $621 \%$ | . 6255 | 6629 | 6331 |  | 6406 | 6438 |  | 6517 |
| 0.4 | . 6554 | 6591 | . 6628 | 6664 | . 6700 | 6736 | 6772 | 6808 | 6844 | 879 |
| 0.5 | 6915 | 6950 | 66985 | 7019 | 7054 | 7088 |  |  |  | 7224. |
| 0.6 | 7257 | 7291 | 7324 | 7357 | 7389 | 7422 | 745 |  | 7 |  |
| 0.7 | 7580 | 7611 |  |  |  |  | 776 |  |  | 2- |
| 0.8 | . 7881 | 7910 | . 7939 | $7967$ | 7995 | $802$ | $805$ | $.8078$ |  | $\begin{aligned} & 8133 \\ & 4889 \end{aligned}$ |
| 0.9 | - 8.8159 | \$186 | 8461 | $8238$ | $5264$ |  | $885$ | $8340$ |  |  |
| 1.0 | .8413 | . 8438 | $8461$ | $8485$ | $8508$ | $85318$ | $855$ | $8577$ | $\begin{aligned} & 8599 \\ & .8810 \end{aligned}$ | $88621$ |
| 1.1 | 8664 8849 | . 8665 | $8686$ | $8878$ | $88729$ | $8879$ | $87707$ | $8790$ | $8810$ | $8830 \div \therefore$ |
| 1.2 | .8849 | .8869 .9049 | $8808$ | $\begin{array}{r} 89077 \\ .9082 \end{array}$ | $\begin{aligned} & 8925 \\ & 9099 \end{aligned}$ | $8944$ | $8962$ | $8980$ | $\begin{aligned} & .8997 \\ & .9162 \end{aligned}$ | $90157$ |
| 1.3 | .9032', | 9049 | $\begin{array}{r} 9066 \\ 9222 \end{array}$ | $\begin{array}{r} 9082 \\ 9236 \end{array}$ | $9099$ | $9115$ | $9131$ | $9147$ |  | $.9319$ |
| 1.4 1.5 | . 91932 | .9207 .9345 | $.9222$ | $9236$ | $\begin{aligned} & 9251 \\ & 9932 . \end{aligned}$ | $\begin{aligned} & .9265 \\ & .9394 \end{aligned}$ | $9278$ | $\begin{array}{r} 9292 \\ .941 .18 \end{array}$ | $\begin{aligned} & 9306 \\ & 9429 \end{aligned}$ | $\begin{aligned} & .9319 \\ & .9441: \end{aligned}$ |
| 1.5 1.6 | . 9332 | -9345 | $.9357$ | $9370 \%$ | $\begin{aligned} & 9382 \\ & .9495 \end{aligned}$ | $\begin{aligned} & 9394 \\ & 9505 \end{aligned}$ | $\begin{aligned} & 94067 \\ & 9515 \end{aligned}$ | $\begin{aligned} & 9418 \\ & \hline 9525 \end{aligned}$ | $\begin{aligned} & 9429 \\ & .9535 \end{aligned}$ | $\frac{.941,}{.9545}$ |
| 1.6 | . 9452 | . 9463 | $9474$ | $\begin{aligned} & 9884 \\ & 9582 \end{aligned}$ | $9495$ | $\begin{aligned} & 9505 \\ & 95997 \end{aligned}$ | $.9515$ | $9525$ |  | $9545$ |
| 1.7. | .9554: | .9564 .9649 | $9673$ | $9582$ | $\begin{aligned} & 9591 \\ & 9671 \end{aligned}$ | $9599$ | $\begin{aligned} & 96088^{\circ} \\ & \hline \end{aligned}$ | $\begin{aligned} & 9616 \\ & 9693 \end{aligned}$ | $\begin{array}{r} 9625 \\ 9699 \end{array}$ | $9633$ |
| $\bigcirc 1.9$ | -9713 | . 9719 | 9726 | 9732 | 9738 | 9744 | 9750 | 9756 | 9761 i | 9767. |
| 2.0 | . 9772 | 9778 | . 9783 | . 9788 | . 9793 | 9798 | 9803 | 9808 | 9812 |  |
| 2.1 | - 9821 | \%826 | 9830 | 0834 |  | 98 | 984 | 9850 | 98 |  |
| 2.2 | 9861 | . 9864 | 9868 | .9871 | 9875 | 9878 | 9881 | 9884 | . 9887 | .9890 |
| $\cdots 2.3$ | \%9893 | 9896 | 9898 | 9925 | 927 | 929 | $0 \cdot 1$ |  | 9913 |  |
| 2.4 | . 9918 | . 9920 | . 9922 | . 9925 | 9927 | 9929 | 9931 | 9932 | 9934 | 9936 |
| . 2.5 | . 9938 | 9940 | 9941 | "9943 | 9945 | 9946 | 9948 | 9949 | 995 |  |
| 2.6 | 9953 | . 9955 | 9956 | 9957 | 9959 | 9960 | 9961 | 9962 | . 9963 | 9964 |
| : 2.7 \%, | . 9965 | 9966 | 9967 | 9968 | 9969 | 9970 | 997 | 9979 | 9973 | $9974 \times$ |
| 2.8 | . 9974 | . 9975 | . 9976 | 9977 | 9977 | 9978 | 9979 | 997 | 80 | 9981 |
| 2.9 | :9981 | . 9982 | 9982 | :9983 | :99.84: | 9984 | 9 | 998 | 980. | 9986. |
| 3.0 | . 9987 | . 9987 | . 9987 | . 9988 | 9988 | 9989 | 9989 | 998 | 9990 | 9990 |
| 3.1 | . 9990 | $\because .9991$ | 9991 | 9991 - | 9992: | 0992 | 9992 | 9992 | 9993 | 9993 |
| 3.2 | . 9993 | . 9993 | . 9994 | 9994. | 9994 | 9994 | . 9994 | . 9995 | 9995 | 9995 |
| -3.3: | 9995;- | 9995 | 9995 | 9996 | 9996 | 9996 | 9996 | 9996 | 9996 | 9997. |
| 3.4 | 9997 | . 999 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | 9997 | 9997 | 9998 |

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| Degrees of frectom |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.995 | 0.99 | 0.975 | 0.95 | 0.90 | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 |
| 1 |  |  | 0.001 | 0.004 | 0.016 | 2.706 | 3.84. | 5.024 | 6.635 | 7.879 |
| 2 | 0.010 | 0.020 | 0.051 | 0903 | 0.214 | 4605 | 5.991 | 7.378 | 9210 | $10.597 \%$ |
| 3 | 0.072 | 0.115 | 0.216 | 0.352 | 0.584 | 6.251 | 7815 | 9348 | 11.345 | 12.838 |
|  | 0.207 | 0.297 | 0.484 | 0:7711 | 1.064 | 7.779 | 9488 | 11.143 , | 13.277 | 14.860 |
| 5 | 0.412 | 0.554 | 0.831 | 1.145 | 1610 | 9.236 | 11.071 | 12.833 | 15.086 | 16.750 |
| : 6 | $\because 6676$ | 0.872 | 1.237. | 1635 | 12204 | $10.645^{\prime}$ | 12.592 | 14.449 | 16.812. | 18.548 |
| 7 | 0.989 | 1.239 | 1.690 | 2.167 | 2.833 | 12.017 | 14.067 | 16.013 | 18.475 | 20.278 |
| 8 | 1344 | 1.646 | 2.180 | 2733 | $34490{ }^{\circ}$ | 13.362 | 15507 | 17.535 | 20.090 | 21.955 |
| 9 | 1.735 | 2.088 | 2.700 | 3325 | 4.168 | 14.684 | 16.919 | 19.023 | 21.666 | 23.589 |
| 10 | 21156 | 2.558 | \%3.247: | 3'940 | 4.865 | 15 | 18307 | 20.483 | 23.209 | $25.188 .:$ |
| 11 | 2.603 | 3.053 | 3.816 | 4.575 | 5.578 | 17.275 | 19.675 | 21.920 | 24.725 | 26.757 |
|  | 3.074 | 3.571 | 14404 | 5.226 | 630 | 18.549 | $21.026{ }^{\circ}$ | 23.337 | 26.217 | 28.299 |
| 13 | 3.565 | 4.107 | 5.009 | 5892 | 7.042 | 19.812 | 22.362 | 24.736 | 27.688 | 29.819 |
|  | 4.075 | 4:660 | 5.629 | 6.571 | 7.79 | 21.064 | 23.685 | 26.119 | 29.141 | 31.319:. |
| 15 | 4.601 | 5.229 | 6.262 | 7.261 | 8.547 | 22.307. | 24.996. | 27.488 | 30.578 | 32.801 |
| 16 | 5:142, | 5.812 | 6.908 | 7.962 | 9.312 | 23.542 | 26.296 | 28:845 | 32.000 | 34.267 |
| 17 | 5.697 | 6.408 | 7.564 | 8.672 | 10.085 | 24.769 | 27.587 | 30.191 | 33.409 | 35.718 |
| 18 | 6.265 | 7.015 | . 8.8231 | 9390 | 10865 | 25.989 | 28.869: | 31.526 | $34.805^{\circ}$ | $6^{3}$ |
| 19 | 6.844 | 7.633 | 8.907 | 10.117 | 11.651 | 27.204 | 30.144 | 32.852 | 36.191 | 38.582 |
| 20 | . 7.434 | 8.260 | 29.59] | '10.851 | 12.443 | 28.412 | 31.410 | 34.170 | 37.566 | 39.997\% |
| 21 | 8.034 | 8.897 | 10.283 | 11.591 | .13240 | 29.615 | 32.671 | 35.479 | 38.932 |  |
| 22 | 8.643 | 9.542 | 10982 | 12338 | -14.042 | 30.813 | - $33: 924$ | 366781 | 40.289 | 42998. |
| 23 | 9.262 | 10.196 | 11.689 | 13.091 | 14.848 | 32.007 | 35.172 | 38.076 | 41.638 | 44.181 |
| 24 | $9: 886$. | 10.856: | 12.401 | 13.848 | 15.659 | 33:196 | 36.415 | 39364 | 42.980 | 45559 |
| 25 | 10.520 | 11.524 | 13.120 | 14.611 | 16.473 | 34.382 | 37.652 | 40.646 | 44.314 | 46.928 |
| 25 | 11.160 | 1249 | 13884 | 15379 | 17292 | $35.563^{2}$ | \% 38885 | 41.923 | 45:642: | 48290 |
| 27 | 11.808 | 12.879 | 14.573 | 16.151 | 18.114 | 36.741 | 40.113 | 43.194 | 46.963 | 49.645 |
| 28 | P12:461 | 13.565 | 115308 | 16.928 | 18.839 | $377.916^{\circ}$ | 41337 | 44,461 | 48.278 | $50.993^{\circ}{ }^{-1}$ |
| 29 | 13.121 | 14.257 | . 16.047 | 17708 | 19.768 | 39.087 | 42.557 | 45.722 | 49.588 | 52.336 |
| 30 | 13.787 | 14.954 | 16.791: | 18.493 | 20.599 | F0256 | 743.773 | 46.979 | 50.892 | 33.672. |
| 40 | 20.707 | 22.164 | 24.433 | 26.509 | 29.051 | 51.805 | 55.758 | 59.342 | 63.691 | 66.766 |
| 50 | 27.991. | 29.707. | $32.357 \%$ | 34.764 | 137.689 | 63.167. | 67.505 | 714420: | 761.54 | 79:490 |
| 61 | 35.534 | 37.485 | 40.482 | 43.188 | 46.459 | 74.397 | 79.082 | 83.298 | 88.3 | 91.952 |
| 70 | 43.275 | 45.442* | 48.758 | 511739 | 15,329: | 85:527. | $\bigcirc 90.531$ | 595:023 | 100.425. | 104.215: |
| 80 | 51.172 | 53.540 | 57.153 | 60.391. | 64.278 | 96.578 | 101.879 | 106.629 | 112 | 321 |
| $90:$ | 59.196 | 61754. | 65,647 | 69.126 | 73.291 | 107.565 | 313145 | T8.136. | 124.116 | 128.299: |
| 100 | 67.328 | 70.065 | 74.222 | 77.929 | 82.358 | 118.498 | 124.342 | 129.561 | 135.807 | 140.169 |

## L-3/T-2 $\quad$ B. Sc. Engineering Examinations 2016-2017

## Sub : IPE 315 (Operations Management)

Full Marks: 210
Time : 3 Hours
USE SEPARATE SCRIPTS FOR EACH SECTION
The figures in the margin indicate full marks.

## SECTION-A

There are FOUR questions in this section. Answer any THREE questions.
Assume any missing data.

1. (a) Time study and Standard element time are two different techniques to calculate standard time. Which one of these two techniques is more accurate and why?
(b) How can you distinguish Pull system from Push system? Provide example for both types of system with respect to sector in Bangladesh.
(c) Aggregate planning is often termed as "Rolling planning horizon" - why?
(d) Do you think that all the raw materials in the warehouse are kept in the same way? If not, what are the principles to be followed to store raw materials? Explain.
(e) For the following table of produced components in an hour time, calculate standard time with a performance rating of 1.25 using an allowance of $12 \%$ of normal time:

| Worker | A | B | C | D | E | F | G | H |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| no of parts | 15 | 18 | 14 | 17 | 16 | 13 | 18 | 16 |

2. (a) How can you distinguish back order in demand option from inventory in capacity option for aggregate planning? Provide examples for both.
(b) New and matured products are alternative to each other - why?
(c) EOQ may or may not pass through the intersection point of holding cost and ordering cost - how?
(d) Briefly describe the working principle of "Kanbam" system in a fast food chain.
(e) For the following order table, decide the sequence of jobs to be processed based on Johnson's Rule. Also show the jobs' duration in a time frame.

Processing Time (days)

| Job | $\frac{\text { Station 1 }}{}$ | $\underline{S t a t i o n ~ 2 ~}$ |  | Station 3 |
| :---: | :---: | :---: | :---: | :---: |
| A | 7 | 2 | 3 |  |
| B | 6 | 4 | 2 |  |
| C | 8 | 5 | 4 |  |
| D | 9 | 2 | 5 |  |
| E | 10 | 3 | 7 |  |

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$$

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3. (a) Briefly describe three different factors in determining capacity alternatives with examples.
(b) Master production schedule (MPS) is opposite to Aggregate Planning - Justify.
(c) Based on the following data, select the best machine to purchase without permitting any loss and meeting custom demand:

Demand $=1500 \sim 2500$ units
Revenue $=187$ BDT/unit $\quad$ Variable cost $=170$ BDT/unit

| Machine | Fixed Cost (BDT) |  | Capacity (units) |
| :---: | :---: | :---: | :---: |
| A | 16,000 |  | 1,000 |
| B | 30,000 |  | 2,000 |
| C | 42,000 |  | 3,000 |

Which steps should you take if none of the machines found suitable to be purchased?
4. (a) How can you distinguish efficiency from productivity?
(b) Work measurement is a vital input for budgeting and scheduling - how?
(c) Long term and short term capacity requirements can be related to two different forecasting patterns. Discuss both with appropriate example.
(d) Calculate EOQ for the following data:

| Annual demand $=$ | 800 units |
| ---: | :--- |
| Ordering cost $=$ | $\$ 9 /$ order |
| Holding cost $=$ | $\$ 3 /$ unit/year |
| Cost per unit $=$ | $\$ 18$ for lot size $1 \sim 49$ |
|  | $\$ 17.75$ for lot size $50 \sim 99$ |
|  | $\$ 17.5$ for lot size $100 \sim 149$ |
|  | $\$ 17.25$ for lot size $150 \sim 199$ |
|  | $\$ 17$ for lot size $200 \sim$ up |

(e) For the following order table, select the best sequence of jobs to be processed based on SPT and EDD rules with logic behind your selection:

| Job | processing Time (days) | Due date (days) |
| :---: | :---: | :---: |
| A | 3 | 4 |
| B | 5 | 7 |
| C | 4 | 8 |
| D | 6 | 9 |
| E | 2 | 5 |

$$
=3=
$$

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## SECTION-B

There are FOUR questions in this section. Answer any THREE questions.
5. (a) A computer software firm has experienced the following demand for its "Personal Finance" software package.

| Months | Unit |
| :--- | :---: |
| September, 2017 | 56 |
| October, 2017 | 61 |
| November, 2017 | 55 |
| December, 2017 | 70 |
| January, 2018 | 66 |

Develop a regression analysis to forecast the demand and find the forecast for the month of January 2019.
(b) Actual demand of a product of certain company has been given for four quarters and forecasts have been estimated by 4 different methods (method1, method2, method3, method4). Using MAD, find the appropriate method of forecasting among the following 4 methods.

| Quarter | Actual Demand | Method1 | Method2 | Method3 | Method4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 105 | 100 | 110 | 120 | 100 |
| 2 | 150 | 120 | 140 | 140 | 140 |
| 3 | 93 | 125 | 130 | 125 | 110 |
| 4 | 100 | 110 | 120 | 120 | 99 |

(c) Discuss different issues in facility location in detail.
6. Brown and Brown Electronics manufacture a line of digital audiotape (DAT) players. The bill of materials, showing the number of each item required is shown below:


Data for A: Gross requirements is 100 units on $9^{\text {th }}$ week, Lead time is 2 weeks, Lot for lot
Data for C: Lead time is 1 week, Lot for lot
Data for D : Lead time is 2 weeks, schedule receipt is 30 on $1^{\text {st }}$ week, lot size 170 units
Data for F: Lead time is 1 week, schedule receipt is 60 on $1^{\text {st }}$ week, on hand inventory is 15 , lot for lot
Data for G: Lead time is 1 week, schedule receipt is 100 on $1^{\text {st }}$ week, on hand inventory is 50 , lot for lot
Data for H : Lead time is 1 week, schedule receipt is 50 on $1^{\text {st }}$ week, lot size 200
Data for I: Lead time is 1 week, schedule receipt is 60 on $1^{\text {st }}$ week, on hand inventory is 15 , lot for lot
Prepare a MRP schedule to satisfy demand.

## IPE 315

7. (a) For the machine-part matrix shown below, form cells using Direct Clustering Algorithm (DCA) and, if conflicts exist, propose alternative approaches for resolving the conflicts.

|  | Machine \# |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Part \# | 1 | 2 | 3 | 4 | 5 |
| 1 | 1 |  | 1 |  |  |
| 2 | 1 |  |  | 1 | 1 |
| 3 |  | 1 |  | 1 |  |
| 4 | 1 |  | 1 |  |  |
| 5 |  | 1 |  | 1 | 1 |
| 6 |  |  |  | 1 |  |

(b) Briefly describe the different types Facility layout with their relative advantages.
8. (a) What is the basic concept of aggregation in planning? What is the main scope of Aggregate Planning?
(b) How can a robust capacity plan affect the life of a manager? What is the consequence of poor capacity plan planning?
(c) Complete the following two production plans, calculate total cost for each plan and select the best plan out of the two with justification.

| Month | Jan | Feb | Mar | Apr | May | Jun | Total |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Beginning inventory | 350 |  |  |  |  |  |  |
| Demand Forecast | 1500 | 1300 | 900 | 900 | 1000 | 1400 |  |
| Safety Stock (0.25 $\times$ Demand |  |  |  |  |  |  |  |
| Production Requirement |  |  |  |  |  |  |  |
| Working days per month | 22 | 19 | 21 | 21 | 22 | 20 |  |
| Ending Inventory |  |  |  |  |  |  |  |



## BANGLADESH UNIVERSITY OF ENGINEERING AND TECHNOLOGY, DHAKA

L-3/T-2 B. Sc. Engineering Examinations 2016-2017
Sub: IPE 329 (Numerical Analysis)
Full Marks: 210
Time: 3 Hours
USE SEPARATE SCRIPTS FOR EACH SECTION
The figures in the margin indicate full marks.

## SECTION - A

There are FOUR questions in this section. Answer any THREE questions.

1. (a) Two distances are required to specify the location of a point relative to an origin in two-dimensional space (Fig. la):


Fig. $1 a$
(i) The horizontal and vertical distances $(x, y)$ in Cartesian coordinates
(ii) The radius and angle $(r, \theta)$ in radial coordinates.

It is relatively straightforward to compute Cartesian coordinates $(x, y)$ on the basis of polar coordinates $(r, \theta)$. The reverse process is not so simple. The radius can be computed by the following formula:
$r=\sqrt{\left(x^{2}+y^{2}\right)}$
If the coordinates lie within the first and forth coordinates (i.e.; $x>0$ ), then a simple formula can be used to compute $\theta$.
$\theta=\tan ^{-1}\left(\frac{y}{x}\right)$
The difficulty arises for the other cases. The following table summarizes the possibilities:

| $\boldsymbol{x}$ | $\boldsymbol{y}$ | $\boldsymbol{\theta}$ |
| :---: | :---: | :---: |
| $<0$ | $>0$ | $\tan ^{-1}(\mathrm{y} / \mathrm{x})+\pi$ |
| $<0$ | $<0$ | $\tan ^{-1}(\mathrm{y} / \mathrm{x})-\pi$ |
| $<0$ | $=0$ | $\pi$ |
| $=0$ | $>0$ | $\pi / 2$ |
| $=0$ | $<0$ | $-\pi / 2$ |
| $=0$ | $=0$ | 0 |

Write a well-structured flowchart for a subroutine procedure to calculate $r$ and $\theta$ as a function of $x$ and $y$. Express the final results for $\theta$ in degrees.

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$$

IPE 329
(b) In solving the free-falling bungee jumper problem, we generally assume that the acceleration due to gravity is a constant value of $9.81 \mathrm{~m} / \mathrm{s}^{2}$. Although this is a decent approximation when we are examining falling objects near the surface of the earth, the gravitational force decreases as we move above sea level. A more general representation based on Newton's inverse square law of gravitational attraction can be written as

$$
g(x)=g(0) \frac{R^{2}}{(R+x)^{2}}
$$

where $g(x)=$ gravitational acceleration at altitude $x$ (in $m$ ) measured upward from the earth's surface $\left(\mathrm{m} / \mathrm{s}^{2}\right), g(0)=$ gravitational acceleration at the earth's surface $(\cong 9.81$ $\mathrm{m} / \mathrm{s}^{2}$ ), and $R=$ the earth's radius ( $\cong 6.37 \times 10^{6} \mathrm{~m}$ ).
(i) Use a force balance to derive a differential equation for velocity as a function of time that utilizes this more complete representation of gravitation. However, for this derivation, assume that upward velocity is positive.
(ii) For the case where drag is negligible, use the chain rule to express the differential equation as a function of altitude rather than time. Recall that the chain rule is

$$
\frac{d v}{d t}=\frac{d v}{d x} \frac{d x}{d t}
$$

(iii) Use calculus to obtain the closed form solution where $v=v_{0}$ at $x=0$.
(iv) Use Euler's method to obtain a numerical solution from $x=0$ to $50,000 \mathrm{~m}$ using a step of $10,000 \mathrm{~m}$ where the initial velocity is $1500 \mathrm{~m} / \mathrm{s}$ upward. Compare your result with the analytical solution.
(c) Discuss some aspects of floating-point representation that have significance regarding computer round-off errors.
2. (a) Prove that the optimal step size for the finite-difference approximation can be expressed as $h_{o p t}=\sqrt[3]{\frac{3 \varepsilon}{M}}$, where $\varepsilon$ is the upper bound of the absolute value of each component of the round-off error and $M$ is the maximum absolute value of the third derivative.
(b) Discuss a procedure for approximating the error in $f(x)$ given derivative of a function and an estimate of the error in the independent variable. Use appropriate sketches.
(c) Manning's formula for a rectangular channel can be written as

$$
Q=\frac{1}{n} \frac{(B H)^{5 / 3}}{(B+2 H)^{2 / 3}} \sqrt{S}
$$

## IPE 329

## Contd... O. No. 2(c)

where $Q=$ flow $\left(\mathrm{m}^{3} / \mathrm{s}\right), n=$ a roughness coefficient, $B=$ width (m), $H=\operatorname{depth}(\mathrm{m})$, and $S=$ slope. You are applying this formula to a stream where you know that the width $=$ 20 m and the depth $=0.3 \mathrm{~m}$. Unfortunately, you know the roughness and the slope to only a $\pm 10 \%$ precision. That is, you know that the roughness is about 0.03 with a range from 0.027 to 0.033 and the slope is 0.0003 with a range from 0.00027 to 0.00033 . Use a first-order error analysis to determine the sensitivity of the flow prediction to each of these two factors. Which one should you attempt to measure with more precision?
3. (a) Three masses are suspended vertically by a series of identical springs where mass 1 is at the top and mass 3 is at the bottom. If $g=9.81 \mathrm{~m} / \mathrm{s}^{2}, \mathrm{~m}_{1}=2 \mathrm{~kg}, \mathrm{~m}_{2}=3 \mathrm{~kg}$, $\mathrm{m}_{3}=2.5 \mathrm{~kg}$, and $k^{\prime} \mathrm{s}=10 \mathrm{~kg} / \mathrm{s}^{2}$, solve for the displacements $x$.
(b) (i) Show that the Gauss-Jordan method requires

$$
\begin{equation*}
\frac{n^{3}}{2}+n^{2}-\frac{n}{2} \text { multiplication/divisions } \tag{20}
\end{equation*}
$$

and
$\frac{n^{3}}{2}-\frac{n}{2}$ additions/subtractions.
(ii) Make a table comparing the required operations for the Gauss-Jordan and Gaussian elimination methods for $n=3,10,50,100$. Which method requires less computation?
4. (a) Write a pseudocode to generate the matrix inverse using $L U$ decomposition.
(b) Prove that the local truncation error for the Euler's method is proportional to the square of the step size and the first derivative of the differential equation.
(c) Solve the following problem over the interval from $t=0$ to 2 using a step size of 0.5
where $y(0)=1$. Display all your results on the same graph and then compare them.

$$
\begin{equation*}
\frac{d y}{d t}=-2 y+t^{2} \tag{15}
\end{equation*}
$$

Obtain your solutions with (i) Heun's method without iterating the corrector, (ii) Heun's method with iterating the corrector until $\varepsilon_{\mathrm{s}}<0.1 \%$, (iii) midpoint method, and (iv) Ralston's method.

## SECTION-B

There are FOUR questions in this section. Answer any THREE.
5. (a) Two positive real roots for the polynomial $f(x)=x^{4}+x^{2}-2$ are $x=1$ and $x=-1$.

Find the other two roots using Muller's method.

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## IPE 329

## Contd... Q. No. 5

(b) Draw the graph of a single function $f$ that satisfies all of the following:
(i) For all $x$, function $f$ is defined and differentiable;
(ii) There is a unique root $a>0$;
(iii) Newton's method will coverage for any $x_{0}>a$;
(iv) Newton's method will diverge for all $x_{0}<0$.
(c) Briefly explain a shortcoming of bisection method and how you will overcome it.
6. (a) The pressure drop in a section of pipe can be calculated as
$\Delta p=f \frac{L \rho V^{2}}{2 D}$
where $\Delta p=$ the pressure $\operatorname{drop}(\mathrm{Pa}), f=$ the friction factor, $L=$ the length of pipe $(\mathrm{m})$, $\rho=$ density $\left(\mathrm{kg} / \mathrm{m}^{3}\right), V=\operatorname{velocity}(\mathrm{m} / \mathrm{s})$ and $D=$ diameter $(\mathrm{m})$. For turbulent flow, the Colebrook equation provides a means to calculate the friction factor,
$\frac{1}{\sqrt{f}}=-2.0 \log \left(\frac{\varepsilon}{3.7 D}+\frac{2.51}{\operatorname{Re} \sqrt{f}}\right)$
where $\varepsilon=$ the roughness (m), and $\operatorname{Re}=$ the Reynolds number
$\operatorname{Re}=\frac{\rho V D}{\mu}$
where $\mu=$ dynamic viscocity $\left(\mathrm{Ns} / \mathrm{m}^{2}\right)$.
$\Delta p$ for a $0.20-\mathrm{m}$-long horizontal stretch of smooth drawn tubing given $\rho=1.23\left(\mathrm{~kg} / \mathrm{m}^{3}\right), \mu=1.79 \times 10^{-5}\left(\mathrm{Ns} / \mathrm{m}^{2}\right), D=0.005(\mathrm{~m}), V=40(\mathrm{~m} / \mathrm{s})$, and $\varepsilon=0.0015(\mathrm{~mm})$. Use a numerical method to determine the friction factor. Note that smooth pipes with $\mathrm{Re}<10^{5}$, a good initial guess can be obtained using the Blasius formula, $f=0.316 / \operatorname{Re}^{0.25}$.
(b) A particle starts at rest on a smooth inclined plane whose angle $\theta$ is changing at a constant rate
$\frac{d \theta}{d t}=\omega<0$
At the end of $t$ seconds, the position of the object is given by
$x(t)=-\frac{g}{2 \omega^{2}}\left(\frac{e^{\omega t}-e^{-\omega t}}{2}-\sin \omega t\right)$
Suppose the particle has moved 1.7 ft in 1 s . Find, to within $10^{-5}$, the rate $\omega$ at which $\theta$ changes.
Assume that $g=32.17\left(\mathrm{ft} / \mathrm{s}^{2}\right)$.
7. (a) The data in the following table gives the actual thermal conductivity data for the element mercury.

| Temperature $\left({ }^{\circ} \mathrm{K}\right)$ | 300 | 400 | 500 | 600 | 700 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Conductivity $\left(\mathrm{W} / \mathrm{cm}{ }^{\circ} \mathrm{K}\right)$ | 0.084 | 0.098 | 0.109 | 0.12 | 0.127 |

$$
=5=
$$

## IPE 329

## Contd...' $\mathbf{Q}$. No. 7(a)

(i) Use Newton interpolation and the data for $300 \mathrm{~K}, 500 \mathrm{~K}$, and 700 K to construct a quadratic interpolate for this data.
(ii) How well does it predict the values at 400 K and 600 K ?
(iii) Estimate the error for the third-order polynomial interpolation.
(b) Consider the following integral

$$
\int_{0}^{2} 1-e^{-x} d x
$$

(i) If the composite trapezoidal rule is to be used to compute this integral, how many intervals will you need if you want to limit the approximate truncation error at $3 \times 10^{-2}$ ?
(ii) Based on the calculation done in (i), show that the approximate truncation error does not exceed the given limit.
8. (a) Evaluate the following integral:
$\int_{-2}^{4}\left(1-x-4 x^{3}+2 x^{5}\right) d x$
Use,
(i) Composite trapezoidal rule, with $n=2$;
(ii) Single application of Simpson's $1 / 3$ rule;
(iii) Multiple application of Simpson's $1 / 3$ rule with $n=4$;
(iv) Simpson's $3 / 8$ rule;
(v) Simpson's $1 / 3$ rule in conjunction with Simpson's $3 / 8$ rule for $n=5$.

In each case, compute the true error and indicate which approach provides the highest accuracy.
(b) Graphically depict the convergence and divergence in simple fixed-point iteration. Prove that the convergence in simple fixed point iteration occurs if the magnitude of the slope of $g(x)$ is less than the slope of the line $f(x)=x$.

# BANGLADESH UNIVERSITY OF ENGINEERING AND TECHNOLOGY, DHAKA 

L-3/T-2 B. Sc. Engineering Examinations 2016-2017
Sub : IPE 311 (Material Handling and Maintenance Management)
Full Marks: 210 Time : 3 Hours
USE SEPARATE SCRIPTS FOR EACH SECTION
The figures in the margin indicate full marks.

## SECTION - A

There are FOUR questions in this section. Answer any THREE questions.
Assume reasonable values for any missing data.

1. (a) What is Industry 4.0 ? What is its implication in industrial maintenance?
(b) Explain third generation maintenance philosophy with neat sketches.
(c) Consider a parallel system made up of two identical units. For system success, at least one unit must operate normally. The system fails when both the units fail. Repair or corrective maintenance begins as soon as a unit fails to return to its operating state. Declare the required assumptions, and parameters/variables to apply the Markov method for the system. Draw the system-state space diagram. Develop the differential equations for the system using the Markov method. Interpret the equations.
2. (a) (i) Construct a fault tree diagram (FTD) for the electric motor circuit shown in Figure for Question 2(a). The top event is defined as 'The motor fails to operate'. The other events are defined as follows.

| Event | Description | Probability of occurrence |
| :---: | :--- | :---: |
| P1 | Defect in motor | 0.01 |
| P2 | Wire failure (open) | 0.01 |
| P3 | Power supply failure | 0.01 |
| P4 | Switch fails open | 0.01 |
| P5 | Fuse failure under normal conditions (open) | 0.01 |
| P6 | Wire failure (shorted) | 0.01 |
| P7 | Power failure (surge) | 0.01 |
| S1 | Switch opened erroneously | 0.001 |
| C1 | Fuse fails open | 0.50 |

Note that the overload in the circuit may be caused either by a short or a power surge, both of which are primary (i.e. basic) events.
(ii) Calculate the probability of occurrence of the top event.


Figure for Question 2(a)

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=2=
$$

IPE 311
Contd... Q. No. 5(b)
(b) Given the following information, show material flows between machines on a from-to-chart.

| Component | Production quantity/day | Routing |
| :---: | :---: | :---: |
| 1 | 30 | A-C-B-D-E |
| 2 | 12 | A-B-D-E |
| 3 | 7 | A-C-D-B-E |

## Additional information:

Component 1 and 2 have the same size. Component 3 is almost 3 is almost twice as large. Therefore, moving two units of components 1 or 2 equivalent to moving one unit of component 3 .
3. (a) List some elements of preventive maintenance (PM). What are the benefits of PM?
(b) A piece of equipment has 30 parts of a specific type with a failure rate of 20 failures per million hours of operation. Assume that the equipment is operated continuously throughout the day and night and the spares are restocked every 4 months. Calculate the probability of having a spare part available when required, if only 4 spare parts are carried in inventory.
(c) An aircraft maintenance project has the following information.

| Activity | Successor | Time estimates (week) |
| :---: | :---: | :---: |
| A | D | 4 |
| B | E, F | 7 |
| C | G | 3 |
| D | I | 6 |
| E | H | 4 |
| F | J | 7 |
| G | J | 6 |
| H | K | 10 |
| I | K | 3 |
| J | - | 4 |
| K | - | 2 |

## Required:

(i) Draw the network diagram. Display all required information on each activity.
(ii) What are the critical activities?
(iii) What are the significance of identifying the critical activities for the maintenance project?
4. (a) Define three key performance indicators that can be used for evaluating performance of maintenance activities of an organization.
(b) How can you apply fuzzy logic/fuzzy set theory for machine health condition monitoring?
(c) List the pillars of Total Productive Maintenance (TPM). Which pillar should be considered first to start TPM program in an organization? Detail your suggested pillar. $(\mathbf{4}+\mathbf{1 0}=\mathbf{1 4})$
(d) How can you establish optimum preventive maintenance policies for a manufacturing organization? Show the necessary computations.

## IPE 311

## SECTION-B

There are FOUR questions in this section. Answer any THREE questions.
5. (a) What are the characteristics required in the pulling member of a conveyor? Differentiate among belt, chain and ropes as pulling members used in different types of conveyors.
(b) Write down the purposes of using take up devices in conveyors? Discuss about the applications, advantages and disadvantages of different types of take-up devices.
(c) What are the required properties of conveyor belt? Discuss the function of rubber and fabric plies in rubberized textile belt.
6. (a) With neat sketches, show the following types of drives.
(i) Drives with snub pulley
(ii) Drives with pressure belt
(b) Show the components of a screw conveyor with a neat sketch.
(c) Mention the benefits and difficulties faced with screw conveyors.
(d) For an unpowered roller conveyor, derive the equation of resistance to motion factor.
(e) An unpowered roller conveyor having a length of 8 m is designed to carry 20 kg of total resistance to motion per meter of length and employed to convey unit loads. Roller diameter is 8 cm , journal diameter is 2.5 cm , weight of roller is $1 \mathrm{~kg}, \mathrm{~K}=85 \%$, $\mu=0.15$ and $\mathrm{k}=0.005 \mathrm{~m}$. If there remains total 80 rollers and 3 rollers can carry each load, find the maximum weight of each unit load.
7. (a) Suppose, a bucket elevator is necessary to elevate charcoals in a factory. For this purpose suggest appropriate type of bucket, bucket arrangement, speed, method of charging and discharging with justification.
(b) A flanged apron conveyor (Fig. 7b) is designed to deliver iron cylinders of a diameter 500 mm , a height of 270 mm and a piece weight $\mathrm{G}=250 \mathrm{~kg}$. The conveyor capacity Z is 250 pieces per hour with an irregularity factor $\mathrm{K}^{\prime}=2.5$. If apron width is $750 \mathrm{~mm}, \mathrm{~A}=150$, minimum load spacing $\mathrm{a}=900 \mathrm{~mm}, \mathrm{~K}=1.08$ and resistance to motion factor, $\omega^{\prime}=0.13$, find the tensions at different points. Here, $\mathrm{H}=4.0 \mathrm{~m}$ and $\alpha=20^{\circ}$.

$$
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$$

## IPE 311


8. (a) Suppose, you are studying a system comprised of two machines and monitoring the state of the system every hour. A given machine operating at time $n$ has probability $p$ of failing before the next observation at time $n+1$. A machine that was in a failed condition at time $n$ has probability $r$ of being repaired by time $n+1$, independent of how long the machine has been in a failed state. The machine's failures and repairs are mutually independent events. Let $X_{n}$ be the number of machines in operation at time $n$. The process $X_{n}, n=0,1, \ldots$ is a discrete time homogenous Markov chain with state space
$I=0,1,2$.
(i) Determine the system's transition probability matrix.
(ii) Obtain the steady state probability vector, if it exists.
(b) How can you apply Hollier algorithm to establish ordering of machines for minimizing backtrack material flows? Illustrate with a numerical example.

